# MANAGEMENT APPLICATIONS in 



Edited by
EPHRAIM R.MCLEAN and JAMES W. SCHENCK


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and
JAMES W. SCHENCK

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COMPUTERS AND INFORMATION SYSTEMS RESEARCH PROGRAM
Graduate School of Management University of California
Los Angeles, California 90024

## TABLE OF CONTENTS

## TITLE

PAGE
1.0 Program Overview . . . . . . . . . . . . . . . . . . . . . . . 1
2.0 Program Participants . . . . . . . . . . . . . . . . . . . . . . 7
3.0 Participants' APL Applications. . . . . . . . . . . . . . . . . . 9
3.1 Armitage, Howard $\begin{aligned} & \text { "The Accounting Cycle". . . . . . . . . . . . . . . . . . . } 11\end{aligned}$
3.2 Baker, Dennis
"Simulation of the Birth and Death of Firms in a Competitive Industry". . . . . . . . . . . . . . . . . 21
3.3 Brown, Lawrence D.
"Single Asset Depreciation Methods" . . . . . . . . . . . . 41
3.4 Case, Fred
"Real Estate Valuation Using the Direct Capitalization Method"47

3.5 Chai, John

"Simulation of Random Samples and Sampling
Distributions of Various Statistics". ..... 55
3.6 Dauner, Jack
"Setting the Size of the Sales Force" ..... 67
3.7 Harpell, John L. Jr.
"Simulation of a 3-Stage Order-Shipment System" ..... 71
3.8 Hickman, Edgar
"Multivariate T-Square Test". ..... 81
3.9 Mason, R. Harold
"Circulation of Disability Settlement Awards" ..... 87
3.10 Miller, Ronald D.
"Linear Programming with Mixed Constraints" ..... 95
3.11 Park, John
"Interactive Effects of the Marginal Propensity to Consume and the Investment Accelerator on the Production of Income" ..... 107
3.12 Sanford, Donald G."Network Analysis".115
3.13 Schriber, Thomas
"Interactive Optimization of a Production System" ..... 127
3.14 Sprague, Ralph H. Jr.
"Interactive Inventory Simulator" ..... 155
3.15 Stricklin, Wilma
"Financial Ratio Calculations" ..... 173
3.16 Thielges, Bernard
"Computation of a Price Index by the Method of the Weighted Geometric Mean" ..... 177
4.0 UCLA APL Library Functions ..... 185
5.0 Outline of the Course ..... 201
5.1 Class Schedule and Reading Assignments ..... 203
5.2 Class Handouts ..... 213
5.2.1 A Guide to Writing APL Programs ..... 215
5.2.2 Signing-On to the UCLA APL System ..... 221
5.2.3 An APL Bibliography ..... 227
5.2.4 "Things Go Better with APL" Claire Stegmann, Think, May/June 1975 ..... 255
5.3 APL Programming Assignment Instructions. ..... 261
6.0 Program Administration and Promotional Materials ..... 265
6.1 Program Announcement Brochure. ..... 267
6.2 Invitation Letter to Business School Deans ..... 273
6.3 Publicity ..... 277
6.4 Application Questionnaire and Cover Letter ..... 281
6.5 Letter of Acceptance ..... 291
6.6 Program Evaluation Questionnaire ..... 297
6.7 Post Conference Follow-Up Letter ..... 303

In recognition of the growing importance of interactive computing in support of management education, the IBM Corporation agreed to sponsor a two-week program on the subject in the summer of 1975. Modelled after the highly successful program at the University of Michigan, which introduced business school educators to the use of FORTRAN, this program was aimed at accomplishing the same goal, this time with the interactive computer language APL. Approximately two dozen management school professors were to be invited to come to the Graduate School of Management (GSM) at UCLA and to be involved in an intensive learning experience.

Basically, the class had two objectives. The first was to gain some familiarity and confidence in the use of the computer and APL. The second was to write a substantial program in APL that would be useful in teaching each faculty member's own discipline (e.g., accounting, finance, production, etc.). The programs that comprise a major part of this book are the results of this second objective.

Naturally, some of these programs are more comprehensive than others; and, in fact, there were a few of the participants that set such ambitious goals for themselves that they were unable to complete their programs in the two-week time period. Then, when they returned home, the press of other activities crowded out their ability to finish their programs. This explains why a few of the participants' programs are missing from this book. However, given the fact that most of the faculty members had never written a computer program before beginning the course, the programs that do appear in the following pages are an impressive testimonial to their hard work and commitment.

Because a great deal of planning and arrangements went into the conduct of the course, it might be of interest to the reader to have a chronology of the events leading up to its offering.

Upon receiving notification of IBM's decision to support the program on Interactive Computing for Management Educators in December of 1974, plans were begun immediately for the conduct of the program. In January of 1975, announcement brochures were prepared (See Section 6.1), describing the program in detail and calling for interested parties to apply for
admission. The contents of this brochure were patterned very closely after the description of the program included in the original grant request proposal sent to IBM. This brochure was then sent to the deans of all of the member schools of the American Assembly of Collegiate Schools of Business (AACSB). It was accompanied by an individually typed cover letter (Section 6.2) which was personally signed by GSM Dean Harold Williams. This more personalized approach was taken to assure that the letter, and the brochure, received a careful reading. In all, slightly over 500 letters were mailed out, each one containing at least two brochures (so that the dean receiving them could circulate them to two groups within the school at the same time).

The response to this mailing -- and to some publicity in the Computing Newsletter for Schools of Business (Section 6.3) -- was nothing short of phenomenal. By the time of the March 15 th deadline stated in the brochure, 197 requests for applications had been received for the 24 openings in the program. Several more requests were received after the deadine, particularly from abroad, which are not included in this total.

To provide a basis for selection -- and, quite frankly, to weed out the idle curious -- a detailed six-page questionnaire (Section 6.4) was prepared and mailed to each of those expressing interest in attending. From this mailing, 105 completed questionnaires were received, representing a wide cross-section of schools, geographical distribution, and academic ranks. With only one opening for every four applicants, the selection process was quite difficult, and a second or third offering could have easily been filled with qualified individuals. Of particular interest is the fact that, of those applying, over 60 came from schools that either already had APL installed and running on their campus computer or were planning its installation within the coming year -- an impressive indication of the spread of APL.

After much careful study, 24 individuals were selected and notified (See Program Participants, Section 2.0). Those who could not be accommodated were also notified at the same time, thanking them for their interest and promising to contact them personally if another offering were to be held.

These 24 faculty members were from schools large and small, public and private. Two were from Canada and two were women (one a nun). All academic ranks were represented, and most areas of specialization within the field of business (e.g., accounting, economics, finance, marketing, production, etc.). Also of interest is the fact that while many people consider APL to be a uniquely IBM product, nearly half of the schools ( 9 out of 21) were running APL on other than IBM equipment.

Upon arrival, the participants were housed in the Holiday Inn of Westwood which allowed them the option of either taking their evening meals at the motel or in one of the many restaurants in nearby Westwood Village. This arrangement proved to be particularly well received, as was the opening reception and dinner which served as an important get-acquainted function. Breakfasts were at the Holiday Inn and lunches at the UCLA Faculty Center. Because the first Friday of the two-week program fell on July 4th, an Independence Day barbecue was held; and, with the exception of one or two individuals who had made previous commitments, it was attended by all of the participants and by the program faculty and staff.

In terms of the conduct of the course itself, the program was split into two groups, A and B. Although it was hoped that all of the participants would be of approximately the same skill level and background, the vagaries of selection were such that some of the attendees were able to move through the course material faster than others. Thus Group B became somewhat the "fast track" and Group A, the "slow track." The reading assignments, class schedule, class handouts, and programming assignments are shown in Sections 5.1, 5.2, and 5.3.

As might be expected, a certain amount of anxiety was caused by the requirement that each person was expected to produce a working, documented program of reasonable complexity by the end of the two weeks. These programs were of their own choosing, and the finished results are published in this monograph. Most of the participants were able to accomplish this task, although a few individuals undertook projects which were really too ambitious: However, even for those who failed to complete their programs, it is felt that the exercise still contributed markedly to their understanding of APL
and interactive computing.
At the end of the program, a three-page questionnaire (Section 6.6) was passed out to each of the participants, asking them their comments and opinions on various parts of the program. So that frank reactions could be obtained, they were not required to sign the questionnaire or otherwise identify themselves; however, most chose to do so. Fourteen questionnaires were returned (and others gave their views orally) and the general reactions were highly favorable. On the key question "Your overall evaluation of the program as a whole -- (Poor) $1 \quad 2 \quad 3 \quad 4 \quad 5 \quad 6 \quad 7$ (Outstanding)," the median response was 6 . The following were typical comments:
"Great! I feel that I was really pressed into learning a great deal in a short time. I am enthused about APL and will begin to use it at my school."
"Outstanding."
"The program was extremely worth while to me. While the work was ample, I feel that's what we were here for so there should be no complaints in that regard. The program was well structured and very well presented."

Of particular interest are the comments (quoted in full) of Dr. Thomas Schriber of the University of Michigan, who for several years conducted the previously mentioned IBM-sponsored program on FORTRAN:
"Excellent, on a variety of counts:

1. Personal-professional (total immersion is the way to get on top of a highly detailed subject like this)
2. Personal-personal (a pleasure to work hard with intelligent, dedicated people, and to get to know these people)
3. Home curriculum (will be upgraded as a result of this course -APL will get into our curriculum faster than otherwise) 4. Schools of Business overall (will get into the APL generation much sooner than otherwise; why not lead instead of lag?)"
Naturally, there were some specific suggestions about particular aspects of the course, the accommodations, or other administrative details, but they were mostly minor. By and large, both the written and oral comments were extremely positive.

As a final wrap-up to the program, a follow-up letter (Section 6.7) was sent to all participants, thanking them for their diligence and offering our assistance to those who had not yet completed their programs.

In the preparation of this monograph, every effort has been made to ensure that the APL programs, as submitted by the participants, are correct and "bug" free and will work as the sample output indicates. However, it is possible that some errors do still exist. If, in using the programs, such errors are encountered, it would be appreciated if the author of the program would be notified directly, with a copy of the correspondence sent to me here at UCLA.

In closing, I would like to acknowledge and thank the several individuals who made this program a success. On the instructional staff, Dr . Kenneth Siler, a fellow member of the GSM faculty, shared equally in the teaching load. James Schenck, a member of the staff of the GSM computing facility, assisted the participants in a number of ways and helped prepare the final versions of the programs for inclusion here. Dr. William Bergquist of IBM also was in attendance during much of the program, first as an observer and later as an assistant in the computer lab. Finally, Bill DeLone and Janice Durbin, graduate students in GSM helped in the preparation of the final manuscript. To all of these individuals, I extend my thanks and deep appreciation.

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June 1980
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PARTICIPANTS' APL APPLICATIONS

## THE ACCOUNTING CYCLE:

 An Interactive ApproachHoward M. Armitage Assistant Professor in Accounting School of Business and Economics Wilfrid Laurier University Waterloo, Ontario Canada

## DESCRIPTION

## Introduction

In many respects, accounting is a highly repetitive process. In fact, the system that a student learns to follow at the outset of his accounting education consists mainly of the following steps:

- Journalizing
- Posting
- Trial Balance Preparation
- Adjustments
- Adjusted Trial Balance Preparation
- Statement Preparation
- Closing Entries

This sequence of steps is known as the accounting cycle and the user learns very early that the effect of any set of transactions on the final statements can be determined by following the above format.

Once this system has been illustrated and used and the student has grasped the repetitive nature of the cycle, further work with hand written accounting systems seems time consuming and only marginally useful. It is clearly advantageous to introduce a student to a system which, once the original entries have been made, can take over the repetitive tasks of posting,
ensuring equality, classifying items into revenue and capital accounts, and preparing final reports. This program has been written in response to such a need.

## Instructions for Use

The user should specify his account names by using the function CNAMES. He must also establish a numbered set of accounts to correspond to the account titles. This should be done by using the function, INIT. INIT, when executed, requests that you enter the account numbers to be used. You should respond by typing the desired accounts separated by at least one blank. For example, 101102103104201202203301 etc.

If you are unable to fit all the account numbers desired on a single line, just enter what will fit on the line and then strike the return key. The INIT function will then ask if you have any more accounts to enter. If you answer YES, INIT will request that you enter the remaining group. INIT will continue requesting more accounts until you respond NO to the question, ANY MORE? At this time, the two needed global variables will be created.

For each entry, the user will be asked to enter an account number, debit or credit, and dollar amount. After each transaction, the equality of the input can be checked by typing NEXT. If the debits do not equal the credits, the system will respond by printing out the last transaction, indicating where the error lies. When the transactions have been completed, a final equality check can be made by typing out.

The program will then take over and print out an UNADJUSTED TRIAL BALANCE. The user will be asked if he has any adjustments to make, following which the system will print out an ADJUSTED TRIAL BALANCE, INCOME STATEMENT, and BALANCE SHEET for the period
covered by the transactions. The revenue and expense accounts will automatically be set back to zero.

The program can be used for illustrating the accounts of a service, merchandising, or manufacturing enterprise whose inventory accounts are kept on a perpetual basis. With slight modifications the system can accomodate periodic inventory systems.

At the end of each iteration, an updated balance sheet will be printed out. Should the user wish to start anew, he can employ the function $Z E R O$ which will reduce the balances in all his accounts to zero. The user can also begin the cycle with any opening balance he wishes by debiting the asset accounts by the desired amount and similarly crediting the liability and equity accounts. When the command OUT is typed, the system will return the desired opening position.

In the following section is an example of program output which has resulted from a small number of transaction data. The amount of detail produced in these reports depends solely on the number of accounts set up and the extent to which these accounts are utilized during the accounting period.

In addition to the functions listed in the Program Listing Section, the program also utilizes a number of public functions. Specifically these are as follows: AKI, AYN, CENTER, COLNAMES, $\triangle E M T$, and IPI.

## PROGRAM USAGE

$A C T$

```
DO YOU NEED INSTRUCTIONS Y
ENTER THE ACCOUNT NUMBER, THE DEBIT OR CREDIT, AND THE AMOUNT FOR EACH
FART OF A TRANSACTION.
WHEN yOU HAVE COMPLETED THE TRANSACTION ENTER NEXT
WHEN YOU HAVE COMFLETED ALL THE TRANSACTIONS ENTER OUT
the system will resfond by printing out a trial balance.
yOU WILL BE ASKED IF YOU HAVE ANY ADJUSTMENTS TO MAKE.
FOLLOWING THESE ADJUSTMENTS, AN ADJUSTED TRIAL BALANCE, INCOME STATEMENT, AND
BALANCE WILL BE PRINTED.
IF YOU WISH TO STOF THE PROGRAM ENTER STOP UNDER ACCOUNT NUMBER.
ACCOUNT NUMBER?
\square:
        102
DEBIT OR CREDIT?
D
AMOUNT?
\square:
    3000
ACCOUNT NUMBER?
\square:
        201
DEBIT OR CREDIT?
C
AMOUNT?
\square:
    2000
ACCOUNT NUMBER?
\square:
    aUT
DEBITS DO NOT EQUAL CREDITS
ACCT DB CR
    102 3000 0
    201 0 2000
ACCOUNT NUMBER?
\square:
    201
DEBIT OR CREDIT?
C
AMOUNT?
\square:
    1000
ACCOUNT NUMBER?
\square:
    aUT
UNADJUSTED TRIAL BALANCE
```

```
UNADJUSTED TRIAL BALANCE
    MATRIX
    ACCTS DEBITS CREDITS
    101 16900.00 0.00
    102 12000.00 0.00
    103 5000.00
    104 10000.00
    105 0.00
    201
    202
    203
    204
    205
    206
    301
    4 0 1
    402
    4 0 3
    404
    405
        0.00
        0.0
        0.0
        0.0
            0.00 20000.00
            0.00 20000.00
            0.00 11000.00
        1000.00 0.00
        100.00 0.00
    6000.00 0.00
        500.00 0.00
            0.00 0.00
        11000.00
        1000.00
        400.00
        100.00
        8000.00
        0.00
    - }\overline{51500.00}\overline{53900.00
DO YOU HAVE ANY ADJUSTMENTS TO MAKE? N
DO YOU WISH A PRINT OUT OF THE ADJUSTED TRIAL BALANCE? N
->
PLEASE ANSWER YES OR NO: N
DO YOU WISH A PRINT OUT OF THE ADJUSTED TRIAL BALANCE? Y
```

| REVENUES |  |
| :--- | ---: |
| SALES REVENUE | 11000.00 |
|  |  |
| EXPENSES | 11000.00 |
| DEPRECIATION EXPENSE | 1000.00 |
| INTEREST EXPENSE | 100.00 |
| SUPPLIES EXPENSE | 6000.00 |
| SALARIES EXPENSE | 500.00 |
|  | 7600.00 |

NET INCOME

BALANCE SHEET

ASSETS

| CASH | 16900.00 |
| :--- | ---: |
| ACCOUNTS RECEIVABLE | 12000.00 |
| SUPPLIES | 5000.00 |
| OFEICE AND EQUIPMENT | 10000.00 |

LIABILITIES AND OWNERS EQUITY

| ACCOUNTS PAYABLE | 11000.00 |
| :--- | ---: |
| SALARIES PAYABLE | 400.00 |
| INTEFEST PAYABLE | 100.00 |
| LONG TERM LIABILITIES | 8000.00 |
| CONTRIBUTED CAPITAL | 20000.00 |
| RETAINED EARNINGS | 3400.00 |

## PROGRAM DESCRIPTION

```
    \nabla ACT
[1] ค TO INITIALIZE VARIABLES
[2] ATHIS FUNCTION REQUIRES THE FOLLOWING FUNCTIONS:
[3] AAYN, CENTEF, COLNAMES, \triangleFMT, AND INC
[4] NEXT+5*7
[5] STOP*10*10
[6] OUT+7*5
[7] +LO1\times2~AYN 'DO YOU NEED INSTRUCTIONS'
[8] 'ENTEF THE ACCOUNT NUMBER, THE DEBIT OR CREDIT, AND THE AMOUNT FOR EACH'
[9] 'PART OF A TRANSACTTON.'
[10] 'WHEN YOU HAVE COMPLETED THE TRANSACTION ENTER NEXT*
[11] 'WHEN YOU HAVE COMPLETED ALL THE TRANSACTIONS ENTER OUT'
[12] 'THE SYSTEM WILL RESPOND BY PRINTING OUT A TRIAL BALANCE.'
[13] !
[14] YOU WILL BE ASKED IF YOU HAVE ANY ADJUSTMENTS TO MAKE.'
[15] 'FOLLOWING THESE ADJUSTMENTS, AN ADJUSTED TRIAL BALANCE, INCOME STATEMENT
        , AND'
[16] 'BALANCE WILL BE PRINTED.'
[17], IF YOU WISH TO STOP THE PROGRAM ENTER STOP UNDER ACCOUNT NUMBER.
        '
[18] LO1:
[19] UN*'UN'
[20] START:TEMPM&TEMP*10
[21] L1:'ACCOUNT NUMBER?'
[22] ACTN+\square
[23] ^ TO CHECK IF (A)THE TRANSACTION HAS BEEN COMPLETED, (B)THE CYCLE HAS BEEN
[24] MCOMPLETED, (C)THE EXIT SYMBOL HAS BEEN CALLED, AND (D)A VALID ACCOUNT
[25] คNUMBER HAS BEEN ENTERED.
[26] }->AGAIN\times!ACTN=NEX
[27] }->FINISH\times1ACTN=OU
[28] }->0\times1ACTN=STO
[29] ->L2\timesı(pMATRIX[;1])>IN+MATRIX[;1]ıACTN
[30] 'INVALID ACCOUNT NUMBER'
[31] }->L
[32] L2:'DEBIT OR CFEDIT?'
[33] CHG*[!
[34] ค TO CHECK FOR DEBIT OR CREDIT RESPONSES.
[35j ->L3\times1v/WW+('D'=1\uparrowCHG),( 'C' =1\uparrowCHG)
[36] }->L
[37] [3:'AMOUNT?'
[38] AMT*,\square
[39] ค TO ENSURE THAT THE VARIABLES NEXT,STOP, AND OUT ARE NOT EXECUTED AND THA
        T THE INPUT IS A SINGLE ENTRY.
[40v] +L3\times1^/NEXT=AMT
[41] +L3\times\imath^/OUT=AMT
[42] }->L3\times1^/STOP=AM
[43] }->L4\times11=\rhoAM
[44] 'ENTER ONLY ONE NUMBER'
[45] +L3
[46] L4:TEMP+TEMP,ACTN,WW\timesAMT
[47 j & ENTERS THE DEBITS AND CREDITS AGAINST THEIR APPROPRIATE ACCOUNT NUMBERS.
[48] MATRIX[IN; 2 3]+MATEIX[IN; 2 3]]WW\timesAMT
[49] }->[
```

```
[50] CHECKS FOR EQUALITY OF DEBITS AND CREDITS ON COMPLETION OF THE trANSACTI
    ON.
[51] AGAIN:TEMPM+(((\rhoTEMP)\div3),3)\rhoTEMP
[52] ->START\times10=-/1\downarrow+&TEMPM
[53] 'DEBITS DO NOT EqUAL CREDITS'
[54] 'ACCT DB CR
[55] TEMPM
[56] ->L1
[57] & CHECKS FOR EqUALITY OF DEBITS AND CREDITS ON COMPLETTON OF THE CYCLE.
[58] FINISH:TEMPM+(((\rhoTEMP)\div3),3)\rhoTEMP
[59] ->COMPLETE\times10=-/1\downarrow++TEMPM
[60] ->AGAIN
[61] & PRINTS OUT UNADJUSTED AND ADJUSTED TRIAL BALANCES.
[62] COMPLETE:UN,'ADJUSTED TRIAL BALANCE'
[63] UN+' '
[64] FS+'I6,X3,2F10.2'
[65] FS CENTER 'MATRIX'
[66] FS COLNAMES '/ACCTS/DEBITS/CREDITS'
[67] FS \triangleFMT(MATRIX)
[68] '
[69] FS }\triangle\overline{FMT}(1 3 \overline{\rho0,+7MATR}I\overline{X[; 2 3.]}
[70] ''
71] ''
[72] }->L1\times1AYN 'DO YOU HAVE ANY ADJUSTMENTS TO MAKE?'
[73] ->LADJX\imath~AYN 'DO YOU WISH A PRINT OUT OF THE ADJUSTED TRIAL BALANCE?'
[74] ' ADJUSTED TRIAL BALANCE'
[75] FS+'I6,X3,2F10.2'
[76] FS CENTER 'MATRIX'
[77] FS COLNAMES '/ACCTS/DEBITS/CREDITS'
[78] FS \triangleFMT(MATRIX)
[79] ,
[80] FS \triangleFMT(1 3 \overline{0,++MATRIX[; 2 3])}
[81] a GOES ON TO INCOME STATEMENT FuNCTION.
[82] LADJ:INC
        \nabla
    \nablaINC[D]
    \nabla INC;MA;NM;FS;TR;TE;NI
[1] a IsOLAtING the revenue accounts, Netting them out, and printing them.
[2] RTHIS FUNCTION REQUIRES HE FOLLOWING FUNCTIONS:
[3] RBSHEET, CENTER, AND \triangleFMT
[4] MA+(.(ACCTN>300)^ACCTN<400)+MATRIX
[5] MA[;3]+-/MA[; 3 2]
[6] NM+((MA[;3])\not=0)\not&MA
[7] FS*'30A1,X10,F12.2'
[8] , '
[9] , ,
[10] ',
[11],
[12] Fs CENTER 'INCOME STATEMENT'
[13] , '
[14] ' REVENUES'
[15] , '
[16] FS \triangleFMT(NAMES[((,ACCTN) INM[;1]);];NM[;3])
[17] (40\rho' '),12\rho'-'
```

```
[18] 'X40,F12.2' \triangleFMT(TR++/NM[;3])
[19]
[20] ' EXPENSES'
[21] , '
[22] aIsolating the expense accounts. Netting them out, and printing them.
[23] MA*(.(ACCTN>400)^ACCTN<500)+MATRIX
[24] MA[;2]+-/MA[; 2 3]
[25] NM+((MA[;2])\not=0)fMA
[26] FS \triangleFMT(NAMES[((,ACCTN) INM[;1]);];NM[;2])
[27] (40\rho' '),12\rho'-'
[28] 'X40,F12.2' \triangleFMT(TE++/NM[;2])
[29] (40\rho','),12\rho'.'
[30] A ARKIVING AT THE NET INCOME FIGURE AND PRINTING IT.
[31] 'X10, [NET INCOMED,X30,F12.2' \triangleFMT(NI+TR-TE)
[32] (52\rho' '),10\rho',
[33] & RETURNING THE NET INCOME FIGURE TO RETAINED EARNINGS.
[34] MATRIX[((,ACCTN)1206);3]+NI
[35] & GOES ON TO THE BALANCE SHEET FUNCTION.
[36] BSHEET
    \nabla
        \nablaBSHEET[D]\nabla
    \nabla BSHEET;MA;NM;ES;TA;TLE
    A Isolating the asset accounts,Netting them out, and Printing them.
[2] aTHIS FUNCTION REQUIRES THE FOLLOWING FUNCTIONS:
[3] ACENTER AND \triangleFMT
[4] MA+(,(ACCTN>100)^ACCTN<200)+MATRIX
[5] MA[;2]+-/MA[; 2 3]
[6] NM+((MA[;2])\geq0)+MA
[7] FS+'30A1,X10,E12.2'
[8j , '
[9] , ,
[10] , ,
[11] , '
[12] FS CENTER 'BALANCE SHEET'
[13] ,'
[14] ' ASSETS'
[15] ',
[16] ES \triangleFMT(NAMES[((,ACCTN) וNM[;1]);];NM[;2])
[17] (400', ),120.'.
[18] 'X40,F12.2'\triangleFMT(TA&+/NM[;2])
[19] ' '
[20] ' LIABILITIES AND OWNERS EQUITY'
[21] ',
[22j q IsOLATING tHE LIABILITY AND EQUITY ACCOUNTS. NETTING them aut and printi
    NG THEM.
[23] MA&(,(ACCTN\geq200)^ACCTN<300)&MATRIX
[24] MA[;3]*-/MA[; 3 2]
[25] NM+((MA[;3])\geq0)+MA
[26] FS \triangleFMT(NAMES[((,ACCTN) INM[;1]);];NM[;3])
[27] (40 ' '),12\rho' '
[28] 'X40,F12.2' \triangleF MT(TLE++/NM[;3])
[29] (40\rho''),12\rho'_'
    \nabla
```

```
    \nabla CNAMES
[1] & THIS ALLOWS THE USER TO ADD, CHANGE, OR DELETE ACCOUNTS.
[.2] ATHIS FUNCTION REQUIRES THE FOLLOWING FUNCTIONS:
[3] คAKI AND IPI
[4] N1:->((1+1+\rhoNAMES)>L\leftarrow(,ACCTN) וI&1\uparrowIPI 'ENTER ACCOUNT NUMBER')/GO
[5] 'NOT A VALID ACCTI, TRY AGAIN'
[6] }->
[7] GO:NAMES[L;]+30^AKI 'ENTER TITLE:'
[8] }->N
    \nabla
    \nabla ZERO
[1] A THIS ALLOWS THE USER TO SET ALL HIS ACCOUNTS TO 2ERO
[2] MATRIX[;2]+MATRIX[;3]\leftarrow0
\nabla
```

SIMULATION OF THE BIRTH AND DEATH OF FIRMS IN A COMPETITIVE INDUSTRY

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## DESCRIPTION

## Introduction

The program described in this paper is an APL simulation of the birth and death of firms in a competitive industry. In summary, the model operates as follows:

1. Three firms begin production in period one.
2. Production is calculated for each firm.
3. An industry price is calculated.
4. Costs and profits are calculated for each firm.
5. Any firm with a net loss disappears from the industry.
6. If the total industry profit for the current period is equal to or greater than some minimum value, one new firm enters the industry in the next period; otherwise, a new firm does not enter.
7. When these determinations have been completed, time, the number of producing firms in the industry, and the total number that have entered the industry are updated.
8. The program then returns to 2 above until the maximum number of time periods has elapsed.

The program facilitates study of the effects of two variables, FACTR and AMULT, separately and in combination, on (1) the average industry production per time period, (2) the life of the firms that are in the industry, and (3) the industry price. These variables are described in the subsequent pages.

In an attempt to conform to the economic theory of competition, the model is constructed under the following assumptions:

1. Competition is imperfect; that is, buyers and sellers do not have complete knowledge (i.e., if one firm obtains a technological breakthrough, others in the industry do not necessarily know of it immediately).
2. Firms are in business to maximize profits.
3. Each firm cannot individually influence input prices, but all working together can cause the prices of inputs to change.
4. No one firm can affect the industry price.
5. In the long run, the increase in the number of firms causes the industry supply curve to shift; and, with a given demand curve, the market price of the product will fall.
6. As new firms enter the industry, there is an effect on the costs of inputs.
7. The assumption of a "spaceless economy" is relaxed and factors such as location are allowed to affect a firm's cost function and possibly cause the death of a firm.

This simulation is an extension of Problem 6-5 described in Naylor, et al. 1 Thus, the output of each firm is determined by the following decision rule: each firm assumes that its competitors will not change their output in the following period. Each firm then produces at the optimum level for each period, based on its cost function and the industry demand function (in which output of competitors is held constant). Consequently, assumption 2 above is met. To meet assumption 1 , parameters $A$ and $C$ (in Problem 6-5) are changed to exogenous variables (i.e., stochastic variates with given expected values, variances, and probability distributions).

Assumptions 3 and 6 are met by adding to $B$ the product of $B$ and $B B$, an exogenous variable. If the number of firms in the industry in period $t$ is greater than the number in period $t-1$, then a "percentage-of-increase-in-input-costs" (BB) is calculated. Assumption 7 enters the model in the following manner: the environment (in which the industry operates) generates an "incident" at some point in time. The time at which the incident occurs (e.g., four time periods since the last incident) is a stochastic variate with given expected value, variance, and probability distribution. A test is made comparing the life of every firm in the industry at a given time period with a variable (VA in the program) generated for "number of years between the current incident and the immediately preceding one." The firm whose life at the point of the test exceeds "between-incident-years" is subjected to the consequences of the environment-generated event.

One way to effect a net loss for the selected firm would be to alter the revenue of that firm; and, if the net profit of the firm were negative, a "death" would result. However, this approach

[^1]would violate assumption 4 in that if the price of one firm is affected, the price of all firms would be affected also because the industry price is the firm price.

Thus, because no one firm should be able to affect price, the shock is directed at the cost function of the firm selected. The program variable FACTR increments the costs of this firm; depending upon the "severity" of the incident (i.e., the magnitude of FACTR), the firm may or may not experience a net loss for the period and thus may or may not exit the industry. One note of caution: a new firm is allowed to enter the industry (in the model) if the total industry profit for the previous period does not fall below some arbitrarily selected amount (VALUE in the program). Therefore, it is important to note that the magnitude assigned to FACTR not only affects the costs of one firm, but also the profit of the total industry, with possible consequent effects on the entrance of a new firm. Thus, if FACTR is very high, the large loss for the firm subjected to environmental shock may be large enough to produce a total industry loss less than the amount of VALUE, in which case another firm would not enter the industry in the subsequent time period.

A second way in which one firm could influence the industry price (and therefore violate assumption 4) is created automatically with the birth of a new firm. This possibility occurs because a higher current period total production would be subtracted from the constant, $D$, in the industry price equation. To counter this possibility, the variable TERM is incorporated into the model. The basic model price equation for any period subtracts from $D$ the quantity, "E x Current total production." To restore most of the original industry price (as determined in period one), TERM adds back to $D$ (and the industry price) the quantity, "E $x$ (total production in period $t$ - total production in period 1)." Although two additional terms are also subtracted from $D$ in the price
calculation, the weight of these terms, .20 and. 03 , does not affect price as much as $E$ which has a value of .50 .

Another variable, AMULT, was created to facilitate control of the impact of TERM. In the modified price equation, AMULT is multiplied times TERM. When AMULT $=1$, the full impact of TERM flows through to the industry price. As AMULT decreases below 1, the impact of TERM diminishes; that is, PRICE in a period will be less than what it would have been because less is "added back" in the price equation. Thus, by decreasing the value of AMULT, one can move into the long run situation described in assumption 5, where the market price of the product will fall because of a supply curve shift resulting from an increase in the number of firms in the industry.

Variables, parameters, and operating characteristics for the model are as follows:

## Exogenous Variables

$U \quad=\quad$ a stochastic variate with a given expected value, variance, and uniform distribution.
$\mathrm{V} \quad=\quad$ a stochastic variate with a given expected value, variance, and uniform distribution.

A $\quad=\quad$ a stochastic variate with a given expected value, standard deviation, and normal distribution.
$B B \quad=\quad$ a stochastic variate with a given expected value, standard deviation, and normal distribution.

C = a stochastic variate with a given expected value, standard deviation, and normal distribution.
VA $\quad=\quad$ a stochastic variate with a given expected value, standard deviation, and normal distribution.

```
FACTR = multiple by which a selected firm's production
        cost is enlarged.
AMULT = amount of impact on PRICE from the variable
        TERM.
```


## Parameters

| B | $=$ a technological parameter |
| ---: | :--- |
| $\mathrm{D}, \mathrm{E}, \mathrm{F}, \mathrm{G}=$ | constants |
| $\mathrm{QLES2}=$ | amount of total industry production two |
|  | periods prior to period one of the simulation. |
| VALUE $=$ | lowest total industry loss level at which |
|  | a new firm can enter the industry. |
| NBEGF $=$ | number of firms in the industry in period |
|  | one. |
| PLES1 $=$ | production for first firm one period prior |
|  | to period one of the simulation. |
| PLES2 $=$ | production for second firm one period prior |
|  | to period one. |
| PLES3 = | production for third firm one period prior |
|  | to period one. |

## Endogenous Variables

PROD = matrix of quantitites of units produced by firms in the industry (rows) in each time period (columns).
COST = matrix of the total cost of production for firms in the industry for each time period.

PRICE $=$ vector of industry price in each time period.
PRFT $=$ matrix of the net profits for firms in the industry for each time period.

Operating Characteristics
$\operatorname{COST}_{i t}=\left(\operatorname{PROD}_{i t}-A_{i}\right)^{2}+B A_{i}^{2}+C+U_{i t}$

where

$$
\begin{aligned}
i= & i^{t h} \text { firm } \\
t= & \text { period } t \\
S_{t}= & \text { quantity of industry output supplied and } \\
& \text { demanded in period } t
\end{aligned}
$$

Potential users of this simulation include undergraduate and graduate students in economics, management science, and information systems courses. For example, application of the program may include instruction in sensitivity analysis, detailed analysis of production and financial statistics for each firm, and modification and further enhancement of the simulation itself.

## Instructions for Use

Entering the word DATAENTRY at the terminal activates the function by that name. This function requests the user to enter fourteen (14) values for the exogenous variables and eleven (11) values for the parameters listed above. The final entry is the number of periods to be simulated. In the present version of the simulation, the number of firms in the industry in period one (NBEGF) must equal three and the number of time periods (NN) must satisfy the relationship, $1 \leq N N \leq 10$. The twenty-six variables and their definitions for the function DATAENTRY are listed in the Explanation section. Note that values for QLES2, PLES1, PLES2, and PLES3 may be either computer or non-computer simulated or may
be assigned by the user, subject to certain initial conditions.
Setting the number of firms in the industry in the initial period equal to three introduces bias in the following manner. According to the cost equation, any firm's cost is roughly equal to $\operatorname{PROD}^{2}$ (i.e., the values of $A, B, C$ and $U$ are small relative to the value of PROD). Therefore, assuming that each firm produces 200 units in period one, the cost of production for each firm is about $200^{2}$, or 40,000 . Price is roughly equal to $D-E S_{t}-F S_{t-1}$ or 1000 (value of the constant D) - .5(600) - .2(580) where $600=3 \times$ production of 200 for each firm and $580=$ the input value for the first period preceding period one of the simulation. Thus price would be about 1000-300-116, or 584.

One consequence of these initial conditions is a net profit of approximately 76,000 ( $(200$ units $\left.\times 584)-200^{2}\right)$. This profit margin relates directly to the minimum level at which FACTR can be set to remove a firm from the industry and yet not produce a total industry loss below VALUE which would then block the entrance of a new firm into the industry. A net profit of 76,000 provides a buffer against "death" and indicates that FACTR would have to be about 2.9 to generate a net loss and the death of a firm (i.e., $(200$ units $\left.\times 584)-\left(2.9 \times 200^{2}\right)=0\right)$ and also not effect a reduction in industry profit from production by other firms. Therefore, when the effects of changes in FACTR on various simulation outputs are being investigated, one should recognize that the initial conditions of three firms produce a measurable "margin against death." Thus, because each simulation run is biased by its initial conditions, the experimenter should make use of his a priori information about the system under study and the purposes of the simulation to select initial conditions with a bias which will support the purposes of this study.

A second consequence of initial conditions is that PRICE is determined by the actions of the three firms, and it is this price
generated in period one that is maintained or approached in the computation of TERM. Finally, besides the number of firms in period one, another condition is the setting of $B B=0$ (i.e., the percentage of increase in input costs in period one is zero).

The function REPORT provides two outputs: the production matrix PROD and the average industry production per time period. The PROD output is the set of time paths of unit quantitites produced by all firms. Time of entry into, and exit from, the industry are displayed. For example, if firm $m$ (row $m$ of the matrix PROD) enters the industry in period 5 and exits in period 8, row m will contain values only in columns five through eight.

In addition to the two outputs described above, modification of the function REPORT would facilitate the outputing of other financial and statistical information. Other financial results available include the industry price for each period (PRICE) and the revenue, cost, and profit for each firm in all time periods (i.e., the variables REV, COST, and PRFT). Firm statistics available include the number of producing firms in the industry for each period (NFRMS) and the life of each firm (ILIFE).

Experiments designed to test the effects of changes in values of FACTR and AMULT on different variables (e.g., COST, ILIFE) include the following:

| Experiment No. | FACTR | AMULT | Purposes |
| :---: | :---: | :---: | :---: |
| 1 | 9.0 | 1 | To test effects of |
| 2 | 5.0 | 1 | decreases in FACTR |
| 3 | 2.0 | 1 |  |
| 4 | 9.0 | . 7 | To test effects of |
| 5 | 9.0 | . 5 | decreases in AMULT |
| 6 | 9.0 | . 3 |  |
| 7 | 5.0 | . 7 | To test joint effec decreases in FACTR |

The input of typical data requested by the function DATAENTRY and typical outputs of the function REPORT are shown in the Sample Use section. For purposes of illustration, experiment No. 1 (above) was used. Data values were entered to test this experiment. (See the symbol table in the following section for the definitions of all of the variables.)

## Program Explanation

Public functions necessary for the successful execution of REPORT include CENTER, RWTD, and $\triangle E M T$. Logical segments of the simulation appear as separate functions. Consequently, execution proceeds through the functions in the following order: DATAENTRY, INITIALIZE, PRODUCTION, COSTREV, UPDATE, and REPORT. Because two or more functions must modify the value of a given variable, all variables are global. APL code for the random number generators, RANDU and RANDN, was prepared by Dr. J. L. Politzer of the Pennsylvania State University Computation Center Staff and made available to Computing Services, University of Alberta, Edmonton.

Special features of the code are the creation of the variables $P$ and RF. When first created in the function, INITIALIZE, $P$ is a production indicator matrix where the $(i, j)^{\text {th }}$ cell value $=1$ signifies that the $i^{\text {th }}$ firm, unless removed from the industry, will produce in the $j^{\text {th }}$ time period. To record the exit of a firm from the industry, $P$ is multiplied in the function UPDATE by RF, a matrix of zeros and ones where a zero indicates removal of a firm and a one permits continued existence of a firm. Therefore, in the subsequent time period, PROD (in the function PRODUCTION) is multiplied by the modified $P$.

Variables first assigned in the functions DATAENTRY, INITIALIZE, PRODUCTION, COSTREV, and UPDATE and their definitions, in order of appearance, are as follows:

| Function | Variable | Definition |
| :---: | :---: | :---: |
| DATAENTRY | B | a technological parameter. |
| " | D, E, F,G | constants |
| " | EXVA1 | expected value of $V$. |
| " | VAR1 | variance of $V$. |
| " | EXVA2 | expected value of $U$. |
| " | VAR2 | variance of $U$. |
| " | QLES2 | amount of total industry production two periods prior to period one of the simulation. |
| " | VALUE | lowest total industry loss level at which a new firm can enter the industry. |
| " | NBEGF | number of firms in the industry in period one. |
| " | PLES 1 | production for first firm one period prior to period one of the simulation. |
| " | PLES2 | production for second firm one period prior to period one of the simulation. |
| " | PLES3 | production for third firm one period prior to period one of the simulation. |
| " | STDA | standard deviation of $A$. |
| " | EVA | expected value of $A$. |
| " | STDB | standard deviation of BB. |
| " | EVB | expected value of BB. |
| " | STDC | standard deviation of $C$ |
| " | EVC | expected value of $C$. |
| " | FACTR | multiple by which a selected firm's production cost is enlarged. |
| 1 | AMULT | amount of impact on PRICE from the variable TERM. |
| " | STDV | standard deviation of VA. |
| 1 | EVV | expected value of VA. |
| " | NN | number of time periods to be simulated. |


| Function | Variable | Definition |
| :---: | :---: | :---: |
| INITIALIZE | T | current time period. |
| " | TT | index for columns of PROD in which production in period $T$ will be recorded. |
| " | MM | maximum number of producing firms (also the number of rows the columns in PROD). |
| " | IN | column numbers of PROD to be assigned to $P$. |
| 1 | P | production indicator matrix. |
| " | ILIFE | vector of lives of firms (value of element $i=1$ life of firm i). |
| " | BB | percentage of increase in input costs. |
| " | NADD | vector of number of firms added to the industry in period T (value will equal zero or one). |
| " | NDROP | vector of number of firms dropped in period $T$. |
| 1 | PRICE | vector of the industry price for each time period. |
| " | EXP | sum of production in period T-1 weighted by $F$ plus sum of production in period $T-2$ weighted by $G$, at any time period T . |
| 11 | v | a stochastic variate with a given expected value, variance, and uniform distribution. |
| " | TNFRM | total number of firms that have entered the industry up to and including a given time period. |
| " | NFRMS | the number of firms producing in the industry in a given time period. |
| " | REV | matrix of revenues for firms in the industry for each time period. |
| " | PRFT | matrix of the net profits for the firms in the industry for each time period. |


| Function | Variable | Definition |
| :---: | :---: | :---: |
| INITIALIZE | COST | matrix of the total cost of production for the firms in the industry for each time period. |
| " | U | a stochastic variate with a given expected value, variance, and uniform distribution. |
| " | VA | a stochastic variate with a given expected value, standard deviation, and normal distribution. |
| " | C | a stochastic variate with a given expected value, standard deviation, and normal distribution. |
| " | A | a stochastic variate with a given expected value, standard deviation, and normal distribution. |
| 1 | DIV | the divisor in the production equation. |
| " | ALPH 1 | lower bound of the range over which $V$ will be distributed. |
| " | BETAI | upper bound of the range over which $V$ will be distributed. |
| " | ALPH2 | lower bound of the range over which $U$ will be distributed. |
| " | BETA2 | upper bound of the range over which $U$ will be distributed. |
| PRODUCTION | VV | reshaping of $V$ into a vector for use in calculating PROD. |
| 11 | EEXP | reshaping of EXP into a vector for use in calculating PROD. |
| " | PP | vector whose $i^{\text {th }}$ element is total production in period $T-1$ minus production of firm i in T-1. |
| " | PROD | quantities produced by each firm in the industry in period $T$. |


| Function | Variable | Definition |
| :---: | :---: | :---: |
| COSTREV | LIFE1 | firms at time $T$ with age $\leq V A$. |
| " | LIFE2 | firms at time $T$ with age > VA. |
| " | CST | costs for firms at time $T$ with age $\leq V A$. |
| " | CST2 | costs for firms at time T with age > VA. |
| " | COST | matrix of the total cost of production for firms in the industry for each time period. |
| " | TERM | E $\times$ (production in period $T$ production in period 1). |
| UPDATE | FIRMDROP | vector indexing firms to be dropped from the industry. |
| 11 | XX | vector of column numbers of $P$ to be adjusted for firms exiting the industry. |
| 1 | RF | matrix of zeros and ones where a zero indicates removal of a firm and a one permits continued existence of a frim. |
| " | IZ | period T-7. |

## PROGRAM USAGE

```
    DATAENTEY
ENTEF THE VALUES FOR B, D, E, F AND G;
INSERT ONE SPACE BETWEEN EACH NUMEER.
\square:
    2 1000 0.5 0.2 0.03
ENTEK THE VALUES FOF EXVA1, VAK1, EXVA2, VAK2,
QLES2 AND VALUE; INSERT ONE SPACE BETWEEN EACH NUMBER.
L:
    0}0.50015500 300
ENTEKK THE VALUES FOK NBEGF, PLES1, PLES2 AND FLES3
(LEAVE ONE SPACE BETNEEN EACH NUMBER)
\square:
    3 200 300 80
ENTEF THE VALUES FOR STDA, EVA, STDB, EVB, STDC, EVC
(LEAVE ONE SPACE BETWEEN EACH NUMBER)
L:
    0.1 2 0.005 0.04 1.333 24
ENTE'K THE VALUES FOR FACTK, AMULT, STDV AND EVV
(LEAVE ONE SPACE BETWEEN EACH NUMBER)
\square:
    910.6667 5
ENTEF NN; NN MUST BE AN INTEGER WITH VALUE 1\leqNN\leq10
\square:
    10
CALL THE SIMULATOK BY TYPING THE WORD INITIALIZE
    INITIALIZE
```

aVEkage production for each of the 10 periods is:


## PROGRAM DESCRIPTION

```
    \nabla INITIALIZE
1] a THIS FUNCTION INITIALIZES VAKIUUS AEKAYS AND PAFAMETERS
[2] & AND SETS VALUES EOF DIV, ALPH1, BETA1, ALPH2 AND BETA2
[3] T&SE゙TLINKI20
[4] T+1
[5] TT+T+2
[6] MM+LC+2
[7] NN+DE
[8] PKOD+(וMN)\circ.\leq }M
[9] IN+2+iNN
[10] P&PKOL[;IN]
[11] PROD[1;1]+D2[5]
[12] }\operatorname{PROD[11 2 3 ;2] [D3[[2 3 4}
[13] b LD1[1]
[14] E+D1[3]
[15] E*D1[4]
[16] G+D1[5]
17] ILIEE\leftarrow(3\rho1),(MM-3)\rho0
[18] V 
[19] NFKMS+TNFKM+D3[1],((NN-1)\rho0)
[20] A&C+VA+U+COST+PRPT+REV+(MM,NN)\rho0
[21] D}~MM\rhoD1[2
[22] DIV 4MM\rho(2+2\timesE)
[23] ALPH14D2[1]-0.5*3\times[2[2]
[24] BETA1+(2\timesD2[1])-ALPH1
[25] ALPH2\leftarrowD2[3]-0.5*3*D2[4]
[26] EETA2+(2\timesL2[3])-ALPH2
[27] PKODUCTION
v
\nabla ProdUCTION
[1] a THIS EUNCTION CALCULATES THE UNIT PFODUCTION EUK
[2] a EACH FIKM IN EXISTENCE IN THE CUKFENT TIME PEEIOD
[3] VV+MM\rhoV[T]+ALPH1+(BETA1-ALPH1)\timesZ+KANDU 1
[4] EEXP+MM\rhoEXP[T]+(Ex+APKOL[;(TT-1)])+(G\times++FEKOD[;(IT-2)])
[5] A[;T]<MM\rhoZZ&D4[1] FANDN D4[2]
[6] AEACH FIKM ASSUMES THAT THE ONLY CHANGES IN OUTPUT FOK THE
[7] aINDUSTFY IN THE NEXT PEFIOD (OVEF THE PREVIOUS pEKIOD)
[8] GNILL BE ATTKIBUTEV ONLY TO ITS CHANGES IN OUTPUT AND
[9] aNO THAT OF ITS COMPETITOKS. NOW, FOR E゙ACH FIKM, CALCULATE
[10] aTHE TOTAL pkODUCTION OF ALL OTEEE FIEMS IN THE PREVIOUS
[11] &PERIOD bY SUBTRACTIONG EACH FIKM'S PRODUCTION FROM THE TOTAL
[12] aINDUSTKY PKODUC'TION.
[13] PF+(MNO(++HKOD[;(TT-1)]))-FKOD[;(TT-1)]
[14] a DETERMINE PKODUCTION FOR THE CURRENT PERIOU; IF THE
[15] a PKODUCTION INDICATOR mATKIX P CONTAINS A CELL VALUE
[16] a OF 2EKO, thIS INDICATES THE dEATH OE A FIKM IN THE
[17] a PKEVIOUS TIME FEKIOD AND TAEKEFOEE NO PKODUCTION
[18] a FOK THIS FIFM IN THE CURFENT FERIOD.
[1g] PKOD[;TT]+(((VV+D+2\timesA[;T])-((E\timesPP)+EEXP)) ×P[;T])\divDIV
[20] a UPDATE THE LIFE OF THE EIRMS IN EXISTENCE bY ONE TIME PERIOD
[21] ILIEE-ILIFE+(PKOD[;TT]>0)
[22] COSTREV
\nabla
```

```
    \nabla K+A CENTER B
[1]
    A++/\times/ 0 2 +RWTD A
    K+(1,A) \rhoA\uparrow((\Gamma0.5\times0\ulcornerA-\rhoB)\uparrow'''),B+,B
    \nabla
    \nabla costREV
[1] a ThIS fulvCTION dETEAMINES THE COST OF PRODUCTION FOR
[2] a EIKMS WHOSE PRESENT AGE IS \leqOK > THE KANDOM VARIABLE
[3] A VG; TOTAL COST FOK EACH FIKM, UNIT PRICE IN PERIOD T
[4] a AND fEVENUE AND PKOFIT FOR EIRMS IN THE CUKRENT PERIOD
[5] A AKE THEN DETERMINEL.
[6] U[;T]+ALPH2+(EETA2-ALPH2)\timesU[;T]+KANUNI 1
[7] VA[;T]+D5[3] RANDOK D5[4]
[8] C[;T]+D4[5] RANDOR D4[6]
[9] & IDENTIFY FIRMS WITH PRESENT AGE\leqVA
[10] LIFE'1+ILIFESVA[;T]
[11] A IDENTIFY EIKMS WITH PRESENT AGE>VA
[12] LIFE2+ILIFE'>VA[;T]
[13] CST 2+CST 1+(MM,NN)p0
[14] CST1[;T]+P[;T]\timesLIFE1\timesC[;T]+U[;T] ( 
[15] CST2[;T]*F[;T]\timesLIFE2\timesD5[1]\timesC[;T]+U[;T]+(B\times(A[;T]*2))+((PKOD[;TT]-A[;T])*2)
[16] COST[;T]+CST1[;T]+CST2[;T]
[17] TEKM+E\times((++PKOD[;TT])-(+APKOD[;3]))
[18] EKICE[T]+(D1[2]+(TEKM\timesD5[2])\divV[T])-(EXP[T]+(D1[3]\times(+APKOD[;TT])))
[19] }->(PKICE[T]\geq0)/H
[20] PKICE[T]+0
[21] P1:KEV[;T]+PKICE[T]\timesFKOD[;TT]
[22] PKFT[;T]+KEV[;T]-COST[;T]
[23] UPDATE
\nabla
    D DATAENTRY
    'enter the values fof b, D, E', F' AND G;'
[1] INTER THE VALUES FOK B, D, E, F AND G;'
[3] D1+]
[4] 'ENTE'R THE'VALUES FOR EXVA1,VAF1, EXVA2,VAK2,'
[5] 'QLES2 AND VALUE; INSERT ONE SFACE BETWEEN EACH NUMBER.'
[6] D2+\overline{]}
[7] 'ENTEK THE valuES FOR NEEGE, PLES1, PLES2 aND PLES3'
[8] '(LEAVE ONE SPACE' BETWEEN EACH NUMBER)'
[9] D3*\square
[10] 'entef the values for stda, eva, stdb, evb, stdC, evC'
[11] '(LEAVE ONE SPACE BETWEEN EACH NUMBER)'
[12] D4+[
[13] 'ENTEF THE VALUES FOR FACTR, AMULT, STDV AND EVV'
[14] '(LEAVE ONE SPACE BETWEEN EACH NUMBER)'
[15] D5+[J
[16] 'ENTER NN; NN MUST BE AN INTEGER WITH VALUE 1\leqNN\leq10'
[17] D6+[
[18] 'CALL THE SIMULATOK BY TYPING THE WORD INITIALIZE'
\nabla
```

```
    \nabla UPDATE
[1] a THIS FUNCTION DROPS AND/OR ADDS EIFMS TO THE
[2] a INDUSTRY, UPDATES TIME PERIODS AND CALCULATES
[3] a THE CHANGE, IF ANY, IN THE PAKAMETER B.
[4] a COUNT THE NUMBER OF FIRMS TO BE DROPPED.
[5] NDROP[T] + +f(PKFT[;T]<0)
[6] a DETERMINE THOSE FIKMS TO BE DROPFED EROM THE INDUSTRY.
[7] ->((T-NN)\geq0)/UP5
[8] a INDEX FIRMS WHICH WILL EXIT THE INDUSTRY.
[9] FIRMDROP+(PFET[;T]<0)\pi(MM\rho1)
[10] XX+T+iNN-T
[11] RF+Q((\rhoXX),MM)\rhoFIKMDROP
[12] a KECOFD ZEROS IN PRODUCTION INDICATOR MATKIX P FOR FIRMS
[13] a that haVE EXITED THE INDUSTRY
[14] P[;XX]-RF\timesP[;XX]
[15] a If TOTAL INDUSTRY PROFIT + VALUE(D2[6]) IS s 0, DO NOT
[16] ค ADD A FIRM TO THE INDUSTRY; OTHERWISE, ADD ONE FIRM
[17] UP5:->(((++PRFT[;T])+D2[6])\leq0)/UP1
[18] NADD[T]+NADD[T]+1
[19] }->((T-NN)\geq0)/KE
[20] ->NEXTPERIOD
[21] UP1:->((T-NN)\geq0)/REP
[22] }P[(3+T);]+
[23] NEXTPEKIOD:T*T+1
[24] TT~TT+1
[25] & IF NUMBEK OG FIFMS IN NEW PERIOD IS > NUMBEK IN PEFIOD
[26] a T-1, ADJUST PAKAMETER B.
[27] IZ+T-1
[28] NFRMS[T]+(NFRMS[IZ]+NADD[IZ])-NDKOP[IZ]
[29] TNFKM[T]+TNFRM[IZ]+NADD[IZ]
[30] }->((NFFMS[T]-NFKMS[IZ])\leq0)/UP
[31] E+B+B\timesBB[T]+D4[3] RANDN D4[4]
[32] PKODUCTION
[33] }->
[34] UP3:BB[T]+0
[35] PRODUCTION
[36] ->0
[37] REP:REPOKT
    \nabla
```

```
    V 2Z+SIG KANDN MU
[1]
        2Z-MU+SIG\times-6 +(+/- 1+?120178956970)\div178956969
    \nabla
```

    \(\nabla 2 Z \leftarrow S I G\) RANDOK MU
        \(X \leftarrow 1\)
    [2] $2 Z+M M \rho 0$
[3] $Z Z[X]+M U+S I G \times^{-} 6+\left(+/^{-} 1+? M M \rho 178956970\right) \div 178956969$
[4] $\rightarrow(M M<X+X+1) / 0$
$[5] \rightarrow 3$
$\nabla$
V $Z+$ RANDU $X$
$Z \leftarrow X \times\left({ }^{-1} 1+? 2147483647\right) \div 2147483646$
$\nabla$
$\nabla R U \leftarrow K A N U N I X$
$K U+X \times(-1+? M M \rho 2147483647) \div 2147483646$
$\nabla$
$\nabla K E P O K T$

[2] THE PKODUCTION MATKIX FOF THE FREVIOUS ';MM-NN; ' PEKIODS AND THE'
[3] ' SIMULATED ';NN;' TIME PERIODS IS:';3pCㅡㄹ
[4] FORMAT CENTER'TIME PERIODS'; 4 PCㅡR
[5] (, ('X9, ', $\left.\left.K P,^{\prime} I 8^{\prime}\right) \triangle F M T(1, M M) \rho^{-} 2+1 M M\right), 2 \rho \underline{C} \underline{R}$
[6] FOKMAT $\triangle F M T(1 M M ; P K O D) ; 8 \rho \underline{C} \underline{R}$
[7] 'AVEKAGE EKODUCTION FOK EACH OF THE' ';NN;' PERIODS IS: '; $3 \rho \underline{(1)}$
[8] 'I4,5X1,F8.1' $\triangle E M T(1 N N ;((+\not \subset P R O D[;(2+1 N N)]) \div N F K M S[T]))$
[9] $\rightarrow 0$
$\nabla$
$\checkmark$ TESTDATA
[1] $D 1 \leftarrow 21000 \quad 0.5 \quad 0.2 \quad 0.03$
[2] $\quad 02 \leftarrow 0 \quad 0.5 \quad 0 \quad 1500 \quad 3000$
[3] D3 $\quad 3 \quad 200 \quad 300 \quad 80$
$[4] \quad D 4 \leftarrow 0.1 \quad 2 \quad 0.005 \quad 0.04 \quad 1.33324$
[5] $\quad D 5 \leftarrow 910.66675$
[6] $D 6+10$
[7] INITIALIZE
$\nabla$

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## DESCRIPTION


#### Abstract

The primary purpose of this program, entitled DEPRECIATE, is to aid management educators in teaching single asset depreciation methods to beginning and intermediate financial accounting students. The program can be used for drill and practice, homework assignments, or in the classroom. It enables the user to choose any of the following depreciation methods: 1. Straight Line (SL) 2. Sum-of-the-years Digits (SYD) 3. Declining Balance (DB) 4. Double Declining Balance (DDB) 5. Sinking Fund (SF) 6. Annuity (AN)


## Usage Instructions

The user is initially asked to respond to the following four questions:

1. Historical cost of asset?
2. Expected net salvage value of asset?
3. Expected life of asset (in years)?
4. Depreciation method desired: SL, SYD, DB, DDB, SF, or AN?

The Historical Cost (HC) can be any positive number less than one trillion. The Net Salvage Value (NSV) can be any positive number less than the historical cost of the asset. The Expected Asset Life ( $N$ ) can be any integer between one and nine hundred ninety-nine. If any of these constraints are violated, asterisks will be printed out in the depreciation table in lieu of numbers.

One of the mnemonics representing the six depreciation methods identified above must be entered in response to question 4. If the user does not input one of these available depreciation methods, he will receive an error message and will be asked question 4 again.

After these four questions are answered satisfactorily, the user obtains a depreciation table containing Annual Depreciation Expense (DE) Accumulated Depreciation (ACC), and Book Value (BV). The user is then given the option to plot depreciation expense over time. He is next asked whether or not he desires to use the same data for a different depreciation method. If he responds YES, he is reasked question 4 above. If he answers NO, he is asked if he wants to enter new data. An affirmative answer results in question 1 being asked again. A negative response yields the message, COODBYE FOR NOW, and exits the user from the program.

In addition to the function $D E P R E C I A T E$, the following public functions are also required: AKI, AYN, NIP, PLOT, and VS. In addition, Scientific Time Sharing Corporations CENTER, COLNAVES, and $\triangle F M T$ are also needed in order to execute the program successfully.

## PROGRAM USAGE

```
    DEPRECIATE
HISTORICAL COST OF ASSET?: 25000
EXPECTED NET SALVAGE VALUE OF ASSET?: 5000
EXPECTED LIFE OF ASSET (IN YEARS)?: 13
DEPRECIATION METHOD DESIRED: SL,SYD,DB,DDB,SF,OR AN?
DDB
TABLE OF ASSET DEPRECIATION
\begin{tabular}{rrrr}
\(Y E A R\) & \(D E P E X P\) & \(A C C D E P\) & \(B O O K V A L U E\) \\
1 & 3846.15 & 3846.15 & 21153.85 \\
2 & 3254.44 & 7100.59 & 17899.41 \\
3 & 2753.76 & 9854.35 & 15145.65 \\
4 & 2330.10 & 12184.45 & 12815.55 \\
5 & 1971.62 & 14156.07 & 10843.93 \\
6 & 1668.30 & 15824.37 & 9175.63 \\
7 & 1411.64 & 17236.00 & 7764.00 \\
8 & 1194.46 & 18430.46 & 6569.54 \\
9 & 1010.70 & 19441.16 & 5558.84 \\
10 & 558.84 & 20000.00 & 5000.00 \\
11 & 0.00 & 20000.00 & 5000.00 \\
12 & 0.00 & 20000.00 & 5000.00 \\
13 & 0.00 & 20000.00 & 5000.00
\end{tabular}
DO YOU W.ANT A PLOT OF DEPRECIATION EXPENSE VERSUS TIME?: Y
PLEASE ANSWER YES OR NO: YES
```



```
DO YOU WANT TO USE THE SAME DATA TO CALCULATE DEPRECIATION EXPENSE, ACCUMULATED DEPRECIATION AND BOOK VALUE USING A DIFFERENT DEPRECIATION METHOD? YES DEPRECIATION METHOD DESIRED: SL,SYD,DB,DDB,SF,OR AN?
SF
WHAT INTEREST RATE DO YOU WISH TO APPLY TO THIS ASSET? (0 \(\leq\) INT RATE \(\leq 100\) ): 11
```


## TABLE OF ASSET DEPRECIATION

```
YEAR DEP EXP ACC DEP BOOK VALUE
    763.02
    1609.97 23390.03
    2550.09 22449.91
    3593.62 21406.38
    4751.94 20248.06
    6037.67 18962.33
    7464.83 17535.17
    9048.98 15951.02
    10807.39 14192.61
    12759.22 12240.78
    14925.76 10074.24
    17330.61 7669.39
    20000.00 5000.00
DO YOU WANT A PLOT OF DEPRECIATION EXPENSE VERSUS TIME?: YES
```



```
DO YOU WANT TO USE THE SAME DATA TO CALCULATE DEPRECIATION EXPENSE,
ACCUMULATED DEPRECIATION AND BOOK VALUE USING A DIFFERENT DEPRECIATION METHOD? NO
DO YOU WANT TO ENTER NEW DATA? NO
GOODBYE FOR NOW
```


## PROGRAM DESCRIPTION

```
    \(\nabla\) DEPRECIATE
[1] คTHIS FUNCTION REGUIRES THE FOLLOWING OTHER FUNCTIONS:
[2] \(A K K I, A Y N, I P I, N I P, ~ O U T P U T, ~ P L O T, ~ A N D V S\)
[3] L2: \(-L 3 x_{1} 0<H C+N I P\) 'HISTORICAL COST OF ASSET?: '
[4] 'HISTORICAL COST MUST BE GREATEF THAN ZERO: \(\diamond \leqslant \rightarrow L 2\)
[5] L3: \(-L 4 \times 10 \leq N S V \leftarrow N I P\) 'EXPECTED NET SALVAGE VALUE OF ASSET?: *
[6] 'EXPECTED NET SALVAGE VALUE OF ASSET MUST BE POSITIVE: \(~ \diamond ~+L 3\)
[7] \(\quad L 4:+(N S V<H C) / L 5\)
[8] 'HISTORICAL COST MUST EXCEED NET SALVAGE VALUE: * ○ \(\rightarrow\) L3
[9] L5: + L6 \(\mathrm{K}_{1} 1<N+I P I\) 'EXPECTED LIFE OF ASSET (IN YEARS)?:
[10] 'EXPECTED LIFE OF ASSET MUST EXCEED ONE: \(\widehat{\text { O }}+L 5\)
[11] L6:'DEPRECIATION METHOD DESIRED: SL,SYD,DB,DDB,SF,OR AN?'
[12] \(\rightarrow(S L, S Y D, D B, D D B, S F, A N, E R R)[' L Y B D F N ' 11+2 \uparrow, \eta]\)
[13] ERR: 'YOU MADE AN ERROR. THE ONLY PERMISSIBLE DEPRECIATION'
[14] 'METHODS \(A R E \quad S L, S Y D, D B, D D B, S E, A N D \quad A N: \quad\), \(0 \rightarrow L 6\)
[15] \(S L:+L 9, C V+H C-A C C+(1 N) \times D E+N \rho(H C-N S V) \div N\)
[16] SYD: \(+L 9, C V \leftarrow H C-A C C \leftarrow+\backslash D E+(\phi 1 N) \times 2 \times(H C-N S V) \div N \times N+1\)
[17] \(D B: C V \leftarrow H C-A C C \leftarrow+\backslash D E+H C \times((1-F R A C) \star((1 N)-1)) \times F R A C+1-(N S V \div H C) \star \div N \bigcirc \rightarrow L 9\)
\([18] \quad D D B: C V \leftarrow H C-A C C \leftarrow+\backslash D E \leftarrow H C \times((1-F F A C) *((1 N)-1)) \times F R A C \leftarrow 2 \div N\)
[19] \(D E+A C C-0,{ }^{-1} 1+A C C+H C-C V+C V\lceil N S V \diamond \rightarrow L 9\)
[20] SF: \(+L 7 \times_{1} 1>I N T+0.01 \times I N T+N I P\) WHAT INTEREST RATE DO YOU WISH TO APPLY TO THI
    S ASSET? ( \(0 \leq I N T\) RATE \(\leq 100\) ): ;
[21] 'INTEREST RATE CANNOT EXCEED ONE HUNDRED.' 仑 \(\rightarrow\) SF
[22] \(L 7: C V+H C-A C C \leftarrow+\backslash D E+(H C-N S V) \times(I N T \div(((1+I N T) * N)-1)) \times(1+I N T) *(1 N)-1 \leqslant+L 9\)
[23] AN: \(\rightarrow\left[8 \times_{1} 1>I N T \leftarrow 0.01 \times I N T \leftarrow N I P\right.\) WHAT INTEREST RATE DO YOU WISH TO APPLY TO THI
    SASSET? ( \(0 \leq\) INT RATE \(\leq 100\) ): ,
[24] 'INTEREST RATE CANNOT EXCEED ONE HUNDRED.' \(\leqslant \rightarrow A N\)
[25] \(L 8: D E+N \rho(H C-(N S V \times(1 \div(1+I N T) \star N))) \div(1-(1 \div(1+I N T) \star N)) \div I N T\)
[26] \(C V \leftarrow H C-A C C \leftarrow+\backslash(H C-N S V) \times(I N T \div(((1+I N T) * N)-1)) \times(1+I N T) *(1 N)-1<+L 9\)
[27] L9: OUTPUT
[28] \(+L 11 \times 2 R+A Y N\) 'DO YOU WANT A PLOT OF DEPRECIATION EXPENSE VERSUS TIME?:
[29] L10: 'DO YOU WANT TO USE THE SAME DATA TO CALCULATE DEPRECIATION EXPENSE,'
\([30]+L 6 \times 1 R+A Y N\) ACCUMULATED DEPRECIATION AND BOOK VALUE USING A DIFFERENT DEP
        RECIATION METHOD?
[31] \(\rightarrow L 2 \times 1 R \leftarrow A Y N\) 'DO YOU WANT TO ENTER NEW DATA?
[32] 'GOODBYE FOR NOW' \(\bigcirc+0\)
[33] L11: 3060 PLOT DE VSiN \(\bigcirc \rightarrow L 10\)
    \(\nabla\)
    \(\nabla\) ouTPUT
[1] ATHIS FUNCTION REQUIRES THE FOLLOWING OTHER FUNCTIONS:
[2] คCENTER, COLNAMES, AND \(\triangle F M T\)
[3] \(F S \leftarrow^{\prime} I 4,3 F 17.2^{\prime}\)
[4] ,
[5] FS CENTER 'TABLE OF ASSET DEPRECIATION'
[6] •
[7] FS COLNAMES '/YEAR/DEP EXP/ACC DEP/BOOK VALUE/'
[8] \(K \nleftarrow i N\)
\([9] \quad E S \quad \triangle F M T(R ; D E ; A C C ; C V)\)
```

$\nabla$

REAL ESTATE VALUATION USING THE DIRECT CAPITALIZATION METHOD

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DESCRIPTION
Introduction

The value of income-producing real estate may be calculated by one of two methods: the present worth of a stream of future benefits or by the direct capitalization method. The most commonly used -- and most conservative -- is the latter, and it is this method which is used in this program. The basic formula is $V=N Y \div C F$, where $V$ is value, $N Y$ is the net income, and CF is the capitalization factor. Depending upon the data available, the building residual method, the land residual method, or the property residual method can be used. The accompanying program, DIRCAL, is designed to perform each of these calculations.

This program can be used by anyone wanting to understand the fundamentals of the direct method of capitalization and to calculate the value for any type of income-producing property for which data are available. The program is useful in both undergraduate and graduate courses in real estate economics, valuation, finance, and investments.

## Use of the Program

To use the function, the user provides the information requested and is then supplied with the answers. Basically, the user must supply data on gross scheduled income; a vacancy and
collection loss percentage; operating expenses, both fixed and reserved, expressed as a percentage of gross scheduled income; property taxes as a percent of the property market value; anticipated earnings rate; and anticipated earnings period or economic life. Then, depending upon the data which are available, estimates are required on the land value; the building value; and the expected residual value of the property at the end of the investment period.

In entering data, a few words of explanation are in order. The following are some of the input prompts, accompanied by a more detailed explanation of what they mean.

ENTER GROSS SCHEDULED INCOME (GSY)
Gross scheduled income refers only to scheduled rents, not to other forms of income.

ENTER OPERATING EXPENSES (OE) AS A
PERCENTAGE OF GROSS SCHEDULED INCOME
Operating expenses are not total expenses; total expenses include operating expenses ( $O E$ ), reserve expenses (RE), fixed expenses (FE), and property taxes (TE).

ENTER RESERVE EXPENSE PERCENTAGE (RE)
Reserve expenses are cash outlays which occur in one year which relate to more than one year of operation. To obtain the figure for reserve expenses, divide each reserve expense by the number of years over which it is to be allocated. For example, roof repairs might cost $\$ 1000$ in one year but be expected to last for ten years. Dividing $\$ 1000$ by 10 would yield an annual cost of $\$ 100$. All these annualized expenses should then be totalled and expressed as a percentage of the gross operating income. Reserve expenses are not made for the purpose of increasing the rents but merely to maintain the scheduled rents.

Fixed expenses include such things as fire insurance, fees, licenses, and similar types of costs whose amounts are determined externally and are not a function of the level of operation.

ENTER MARKET VALUE OF THE PROPERTY (MV)
The market value is either the original purchase price or the current estimated market value, whichever is most appropriate. If neither are available, use the assessed value, adjusted to approximate the market value.

Each of the above should be entered separately. If they are not available directly, they should be derived from the assessed values.

The remaining requests for input are fairly straightforward. When all inputs have been completed, the program will print out the resultant value estimations. These are calculated according to the building residual method, the land residual method, and the property residual method. If the user wishes to run the program again, retyping DIRCAL will cause it to restart.

All data must be entered each time calculations are run. However, the user can vary the data each time according to his needs. The sample session provides an illustration of the kinds of data asked for and the output produced, given the data provided.

## PROGRAM USAGE

DIFCAL

```
ENTER ALL PERCENTAGE FIGURES AS DECIMAL FRACTIONS, E.G.,
8 PERCENT WOULD BE ENTERED AS .08
IF YOU MAKE. A MISTAKE ENTERING DATA, START OVER.
ENTER GROSS SCHEDULED INCOME(GSY)
\Pi:
    30000
ENTER VACANCY AND COLLECTION LOSS (VCL) AS A PERCENTAGE OE
GROSS SCHEDULED INCOME.
П:
    .06
ENTER OPERATING EXPENSES (OE), AS A PERCENTAGE OF GROSS SCHEDULED INCOME.
\Gamma:
    . }1
ENTER RESERVE EXPENSE PERCENTAGE(RE)
\Gamma:
    .04
ENTER FIXED EXPENSE PERCENTAGE(FE)
\Gamma:
    .06
ENTER MAFKET VALUE OF THE PFOPERTY (MV)
\Gamma:
    190000
ENTER PFOFERTY TAX EXPENSES (TE) AS PERCENTAGE OF MARKET VALUE
\Pi:
    .025
ENTER LAND VALUE(LV)
\Gamma:
    70000
ENTER BUILDING VALUE(BV)
I:
    120000
ENTER INTEREST RATE OR EARNING RATE (EGR).
П:
    .08
FNTER EARNING PERIOD OR ECONOMIC LIFE, IN YEAES (ECL)
\Gamma:
    4 0
ENTER EXPECTED RESIDUAL VALUE (ERV) AT END OF EARNING PERIOD.
IF YOU CANNOT ESTIMATE RESIDUAL VALUE, JSE LAND VALUE(LV).
\Pi-
    70000
```

```
VALUE ESTIMATE CALCULATIONS USING THE BUILDING RESIDUAL METHOD
    LAND INCOMF (LVY) 5600
    BUILDING INCOME (FBY) 12210
    VALUE OF BUILDING (FRV) 116285.7143
    VALUE ESTIMATE DERIVED (BPV) 186285.7143
VALUE ESTIMATE CALCULATIONS USING THE LAND RESIDUAL MFTHOD
    BUILDING INCOME (BLY) 12600
    LAND INCOME (RLY) 5210
    LAND VALUE ESTIMATE (RLV) 65125
    VALUE ESTIMATE (RPV) 185125
VALUE ESTIMATE CALCULATIONS, DEFIVED USING THE PROPERTY RESIDUE METHOD
    PRESENT VALUE OF FUTURE NET INCOME STREAM (PVY) 169619.0476
    PRESENT VALUE OE ANY RESIDUAL PKOPERTY AT END OE INVESTMENT(DLV)
        3222.165331
    VALUE ESTIMATE DEFIVED (PRV) 172841.213
    ANNUAL PERCENT NET INCOME DECLINE WHILE PROTECTING EQUITY EARNING RATE
        0.01904761905
```

```
    \nabla DIRCAL
[17
[2] 'ENTER ALL PERCENTAGE FIGURES AS DECIMAL FRACTIONS, E.G.,'
[3] '8 EERCENT WOULD BE ENTERED AS .08'
[4] 'IF YOU MAKE A MISTAKE ENTERING DATA, START OVER.'
[5] ',
[6] 'ENTER GROSS SCHED|LED INCOME(GSY)'
[7] GSY+\Gamma
[8] 'ENTER VACANCY AND COLLECTION LOSS (VCL) AS A PERCENTAGE OF
    GROSS SCHEDULED INCOME.'
[9] VCL<\square
[10] 'ENTER OPERATING EXPENSES (OE), AS A PERCENTAGE OE GROSS SCHEDULED INCOME
[111] OE&\square
[12] 'ENTER RESERVE EXPENSE PEFCFNTAGF(FE)'
[13.] FE&[
[14] 'ENTER FIXED EXPENSE PERCENTAGE(EE)'
[15] }FE+
[16] 'ENTER MARKET VALUE OF THE PROPERTY (MV)'
[17] MV 
[18] 'ENTER PROPERTY TAX EXPENSES (TE) AS PERCENTAGE OF MARKET VALUE'
[19] TE&\square
[20] 'ENTER LAND VALUE(LV)'
[21.] LV&\square
[22] 'ENTER BUILDING VALUE(BV)'
[23] BV [
[24] 'ENTER INTEREST RATE OR EARNING RATE (EGR).'
[25] EGF4
[26] 'ENTER EARNING PERIOD OR ECONOMIC LIEE, IN YEAFS (ECL)'
[27] ECL<п
「28] 'ENTER EXPECTED RESIDUAL VALUE (ERV) AT END OF EARNING PERIOD.'
[29] 'IE YOU CANNOT ESTIMATE RESIDUAL VALUE, USE LAND VALUE(LV).'
[30] ERV + 
「31] GOY&GSY-(GSY\timesVCL)
[32] NY&GOY-(GOY\timesOE+RE+FE)+TE\timesMV
```



```
[34] RBY NY-LVY
[35] RRV+RBY\div(EGR+(1\divECL))
[36] }BPV\leftarrowLV+RB
[37] }BLY+BV\times(EGR+(1\divECL)
[38] RLY NY-BLY
[39] RLV+FLY\divEGR
[40] RPV +BV+RLV
[41] PVY+NY\div(EGR+(1\divECL))
[42] DLV+ERV\times(1\div(1+EGR)*ECL)
[43] PRV PVVY+DLV
[44] DEY+(EGR\times(1\divECL))\div(EGR+(1\divECL))
[45] ''
[46.] 'VALUE ESTIMATE CALCULATIONS USING THE BUILDING RESIDUAL METHOD'
```

```
[47] ' LAND INCOME (LVY) ;;LVY
[48] ' BUILDING INCOME (FBY) ';RBY
[49] , VALUE OF BUILDING (RBV) ';FBV
[50] , VALUE ESTIMATE DERIVED (BPV) ;BPV
[51] ''
[52] 'VALUE ESTIMATE CALCULATIONS USING THE LAND RESIDUAL METHOD'
[53] BUILDING INCOME (BLY) ';BLY
[54] ' LAND INCOME (RLY) ';RLY
[55] , LAND VALUE ESTIMATF (FLV) 'FLV
[56] VALUE ESTIMATE (RPV) ;RPV
[57] ''
[58] 'VALUE ESTIMATE CALCULATIONS, DERIVED IISING THE PPOEERTY RESIDUE METHOD'
[59] ' PRESENT VALUE OF FUTURE NET INCOME STREAM (PVY) ';PVY
[60] , PRESENT VALUE OF ANY RESIDUAL PROPERTY AT END OE INVESTMENT(DLV)
    ; ;DLV
[61] , VALUE ESTIMATE DERIVED (FFV) ;FFV
[62] , ANNUAL PEKCENT NET INCOME DECLINE WHILE PROTECTING EQUITY EARNING R
ATE ':DEY
\nabla
```

SIMULATION OF RANDOM SAMPLES
AND SAMPLING DISTRIBUTIONS OF VARIOUS STATISTICS
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## DESCRIPTION

## Introduction

This program is made up of three functions: (1) POPDIST, (2) SIMUSAMPLE, and (3) SAMPDIST. SIMUSAMPLE is the main function and the other two are subfunctions. The first function inputs a finite population and formulates the frequency (or probability) distribution with equal class intervals; the second function generates, from the input, simple random samples with replacement of a specified size for a specified number of replications; and the third function formulates the sampling distribution of a specified statistic such as sample mean, median, range, variance, and standard deviation. The program is designed primarily to teach students in a beginning applied statistics course (undergraduate and graduate levels) the concepts of simple random sampling from a finite population, the sampling distribution of a statistic, the central limit theorem, and the relationship between parameters and statistics. This program can also be used for a general simulation problem. The program is intended to be used in a flexible way in that the instructor may use it in a classroom as a teaching device or students may use it independently outside class as an exercise in statistical problems related to sampling distribution theory.

## Instructions for Use

It is assumed that the users know what a frequency for probability) distribution is; what simple random sampling without replacement is; what a sampling distribution is; what the central limit theorem is; and what relationship exists between the statistic involved and the parameters of the population under consideration. The data for input is a set of a finite population. Either a string of individual values (ungrouped data) of a population or a frequency distribution (grouped data) of a population can be entered. If a string of individual values is to be entered as input, the program asks a user to specify the parameters necessary for formulating the ungrouped data into a frequency distribution (i.e., the lower class limit value of the first class, the class interval, and the number of classes required). The program outputs the maximum and minimum values of the input for the user's convenience. If a user wants to input a frequency distribution, the program asks for the class midpoints and corresponding frequencies as input. The program also asks for the population size. If a user inputs a probability distribution, the program asks the user to convert the probabilities to absolute frequencies based on the population size. Then the program outputs a table and a graph showing the details of the population. The table shows lower and upper class limits, class midpoints, absolute and relative frequencies (probabilities), and absolute and relative cumulative frequencies. The graph is in the form of a histogram.

The program also outputs the values of population mean, median, range, variance, and standard deviation. The program then asks the user to input the size of the sample and the number of replications. Next, the program outputs the names of statistics for which sampling distributions can be developed and asks the user to designate one
statistic. The program outputs the maximum and minimum values of the statistic and asks the user to input the lower class limit value of the first class, class interval, and the number of classes required to formulate the sampling distribution. The program then outputs the sampling distribution in tabular and graphic forms, which are very much like the ones given for the population data. It also outputs the various parameters of the sampling distribution.

The program gives the user the option of respecifying the three parameter values necessary for formulating the frequency distribution of the population and the sampling distributions. It also provides the user with the option of continuing the program with a new statistic or a new population.

The constraints of the program are as follows. First, the population size is set to at least 100. This is an arbitrary number. In fact, one should be aware that the population size must be considerably larger than the sample size in order that the effect of the central limit theorem can be realized. On the other hand, one should be aware of workspace size limitations if a string of ungrouped data of a large size population is to be entered. In this case, one is advised to formulate a frequency distribution first and input it instead of inputting ungrouped data. Second, the sample size and the number of replications are also limited to a maximum of 99 and 50, respectively, in view of the workspace size limitation and the high cost of replications. Third, a user must select the lower class limit value of the first class to be slightly less than the minimum value in the data for formulating a frequency distribution of a population and for developing a sampling distribution, for the lower class limit values are not counted into the classes.

To use the program, the student merely needs to type SIMUSAMPLE. This first program then calls the others (POPDIST
and SAMPDIST). In addition to these functions, the public functions AKI, AYN, CENTER, COLNAMES, $\triangle F M T, ~ P L O T, ~ a n d ~ V S ~ a r e ~$ needed.

## PROGRAM USAGE

A POPULATION DATA TO BE ENTERED AS INPUT MAY BE IN THE FORM
OF A VECTOR OF IMDIVIDUAL VALUES (UNGROUPED DATA) OR IN THE FOFM
OF FREQUENCY (OR PRORAEILITY) DISTRUCTIONS. PLEASE FOLLOW THE INPUT
INSTRUCTIONS BELOW CAREFULLY
HAVE YOU ALREADY ENTEFED THE POPULATION DATA? TYPE YES OF NO. N
ENTER THE POPULATION SIZE. THE SIZE MUST BE AT LEAST 100:
ENTER $\stackrel{90}{T} H E$ POPULATION SIZE. THE SIZE MUST PE AT LEAST 100:
ㄴ:
500
IS YOUR DATA UNGROUPED? TYPE 'Y' OR 'N'. Y
ENTE? UNGROUPED DATA. TYPE ' , ' IF MORF SPACE IS NEEDED FOF ENTERING DATA.
‥ $\quad((1200)+200010), \Pi$
$(1300) \times 2+(? 300 \rho 10]$
SYNTAX EFROR
$(1300) \times 2+(? 300010]$
$\square:$
$(1300) \times 2+(? 300 \mathrm{p} 10)$

ARE ASKED TO SPECTFY THE LOWER CLASS LIMIT VALUE OF THE FIRST CLASS, WIDTH OF'CLASS, AND NUMEEF OF CLASSES, E.G., 520 10. ENTER THESE THREE VALUES:
6 600 6



 30004000

 SAMPLE SIZE MUST BE LESS THAN 100 AND NO. OF REPLICATIONS MUST BE NO GRE ATER THAN 50. 10956

TRY AGAIN.
ENTER THE SAMPLE SIZE AND THE NUMBER OF REPLICATIONS DESIRED, E.G., 2030 SAMPLE SIZE MUST BE LESS THAN 100 AND NO. OF FEPLICATIONS MUST BE BO GREATER THAN 50 . ㄱ:
-. 1020
NHE TARIE VARIABLE NAME OF ONE STATISTIC OF YOUR INTEREST
STATISTICS VAFIABLE

| MEAN | SMS |
| :--- | :--- |
| MEDIAN | $S M D S$ |
| RANGE | $S R S$ |
| VAFIANCE | $S V S$ |
| STAND DEV | SSDS |

[1:
SMS
信
PARAMETERS OF SAMPLING DISTRIBUTION

| MEAN | 744.00 |
| :--- | ---: |
| MEDIAN | 756.00 |
| RANGE | 780.00 |
| VARIANCE | 65276.00 |
| STAND DEV | 257.44 |

 SAMPLING DISTRIBUTION OF THE STATISTIC IS PRESENTED IN THE FORM
OF PKOBABILITY DISTRIBUTION AND GFAPH BELOW:
BUT EIRST, ENTER THE LOWEF CLASS LIMIT VALUE OF THE FIRST CLASS, CLASS WIDTH, AND NO. OF CLASSES YOU NEED FOR THE SAMPLING DISTRIBUTION, E.G., 05 10:
(MAXIMUM VALUE OF THE STATISTIC IS: 1146 THE MINIMUM IS: 366):
$\square:$
4002005
 SAMPLING DISTRIBUTION


 WOULD YOU LIKE TO DEVELOP THE SAMPLING DISTRIBUTION FOR A NEW STATISTIC? N WOULD YOU LIKE TO RESPECIFY SAMFLE SIZE AND/OR NO. OF REPLICATIONS? N

DO YOU LIKE TO CONTINUE EXERCISE WITH A NEW POPULATION? N

SIMUSAMPLE
A POPULATION DATA TO EE ENTERED AS INFUT MAY EE IN THE FOFM
OF A VECTOR OF INDIVIDUAL VALUES (UNGROUFED DATA) OR IN THE FORM
OF FREOUENCY (OR PROBABILITY) DISTRUCTIONS. FLEASE FOLLOW THE INPUT
INSTRUCTIONS BELOW CAREFULLY
HAVE' YOU ALREADY ENTERED THE FOPULATION DATA? TYPE YES OR NO. N
ENTEF THE POFULATION SIZE. THE SIZE MUST BE AT LEAST 100:
$\square:$
500
IS YOUR DATA UNGROUPED? TYPE 'Y' OR 'N'. N
ENTEK THE GROUPED DATA AS FOLLOWS: IF THEE DATA CONTAINS ABSOLUTE FREQUENCIES
ENTER THE EREQUENCIES. IF THE DATA CONTAINS FELATIVE FREDUENCIES OR PROBABILITIES, CONVERT THEM INTO ABSOLUTE FREQUENCIES AND ENTER THE ABSOLUTE FREQUENCIES:
 YOUR FREQUENCY DISTRIBUTION TABLE, I.E., 52010.
7 :
0116




 ENTER THE SAMPLE SIRE AND THE NUMBER OF REPLICATIONS DESIRED, E.G. 20.30.
SAMPLE SIZE MUST BE LESS THAN 100 AND NO. OE REPLICATIDNS MUST BE NO GREATER THAN 50 . ㄲ:

```
ENTER THE VARIABLE NAME OF ONE STATISTIC OF YOUR INTEREST
THE VARIABLE NAMES ARE AS FOLLOWS
                        STATISTICS VARIARLE
\begin{tabular}{ll} 
MEAN & SMS \\
MEDIAN & SMDS \\
RANGE & SRS \\
\(V A R I A N C E\) & \(S V S\)
\end{tabular}
    VARIANCE
    STAND DEV
        SMS
********************t************************************************************t*************
    PARAMETERS OF SAMPLING DISTRIBUTION
            MRS OF SAMPLING DISIRIBUTION
```



``` SAMPLING DISTRIBUTION OF THE STATISTIC IS PRESENTED IN THE FORM
OF PROBABILITY DISTRIBUTION AND GKAFH BELOW:
BUT, EIRST, ENTER THE LOWER CLASS LIMIT VALUE OF THE EIRST CLASS, CLASS WIDTH, AND NO. OF CLASSES YOU NEED EOR THE SAMPLING DISTRIBUTION, E.G., 0510 .
(MAXIMUM VALUE OF THE STATISTIC IS: 2.765665667 THE MINIMUM IS:• 0.9333333333):
I: 5.56
```


 0.50


WOULD YOU LIKE TO DEVELOP THE SAMPLING DISTRIBUTION FOR A NEW STATISTIC? N.
WOULD YOU LIKE TO RESPECIFY SAMPLE SIZE AND/OF NO. OF REPLICATIONS? N

DO YOU LIKE TO CONTINUE EXEFCISE WITH A NEW POPULATION? N

## PROGRAM DESCRIPTION

## $\nabla$ POPDIST; $X$; CW; $F$; FORM; $K$; $L C$; LCM; PARAMPM; PMD; PR; PV; PSD; RCF; RF; UC

[1]
[2] AAKI, CENTER, COLNAMES, $\triangle F M T, ~ P L O T, ~ A N D ~ V S . ~$
[3] TEst:'enter the population size. the size must be at least 100:'
[4] $P N+\square$
[5] $\rightarrow((P N<100), P N \geq 100) / T E S T, G O O D$
[6] GOOD: ANS $-A K I$ 'IS YOUR DATA UNGROUPED? TYPE $\cdot Y$ '. OR ''N'.'
[7] $\rightarrow\left(\left({ }^{\prime} Y ' \in A N S\right),\left(N^{\prime} \in A N S\right)\right) / L 1, L 2$
[8] L1:'ENTER UNGROUPED DATA. TYPE $\cdots, \square$ ' IF MORE SPACE IS NEEDED FOR ENTERING DA
[.9] $X+\square$
[10] '.
[11] 'MAXIMUM VALUE IS: '; $/$ /X;' MINIMUM VALUE IS: ; $\mathrm{L} / \mathrm{X}$
[12] 'IN ORDER TO SHAPE A FREQUENCY DISTRIBUTTON FOR THE UNGROUPED DATA'
[13] YOU ENTERED, YOU ARE ASKED TO SPECIFY THE LOWER CLASS LIMIT VALUE,
[14] 'OF THE FIRST CLASS, WIDTH OF CLASS, AND NUMBER OF CLASSES, E.G.:'
[15] , 520 10. ENTER THESE THREE VALUES:'
[16] $\quad P * \square$
$[17] \quad F^{+}+/(1 P[3]) \circ .=\Gamma(X-P[1]) \div P[2] 0 \rightarrow L 3$
[18] L2:'ENTER THE GROUPED DATA AS FOLLOWS: IF THE DATA CONTAINS ABSOLUTE,
[19] 'fREQUENCIES. ENTER the FREQUENCIES. IF the data contains relative'
[20] 'FREQUENCIES OR PROBABILITIES, CONVERT THEM INTO ABSOLUTE FREQUENCIES'
[21] 'AND ENTER tHE ABSOLUTE FREQUENCIES:'
[22] $F+\square$
[23] 'ENTER THE LOWER CLASS LIMIT OF THE FIRST CLASS.CLASS INTERVAL, AND'
[24] 'NUMBER of CLASSEs in your frequency distribution table, i.e.,'
$[25 \mathrm{j}$, 520 10.'
[26] $\quad P \leftarrow \square$
$[27] L 3: Y+(P[1]+0.5 \times P[2])+C W+(((1 P[3])-1) \times P[2])$
[28] $U C+P[2]+L C+P[1]+C W$
[29] $\quad F F+100 \times F \div P N$
[30] $R C F+100 \times((C F++/((\imath \rho F) \circ, \geq 1 \rho F) \times(2 \rho \rho F) \rho F) \div P N)$
[31] $P R+\Gamma / U C-L / L C$
[32] $P S D+(P V+(+/(Y-P M+(+/ Y \times F) \div P N) * 2) \div P N) * 0.5$
[33] $L C M+L C[K+1 \uparrow(50 \leq K C F) /(1 P[3])]$
[34] $\rightarrow((K=1), K>1) / M D 1, M D 2$
[35] $M D 1: P M D \leftarrow L C M+P[2] \times 50 \div F F[K]$
[36] $\rightarrow$ FORMAT
[37] $M D 2: P M D+L C M+P[2] \times(50-R C F[K-1]) \div R F[K]$
[38] FORMAT:FORM+'3F14.2,I 10,F14.2,I 10,F14.2'
[39] STAR+950'*.
[40] STAR
[41] $\cdots$
[42] FORM CENTER 'POPULATION DISTRIBUTION TABLE'
[43] FORM COLNAMES '/ LOWEF/ UPPER/ CLASS/ FREQ/ REL/ CUMUL/REL CUM/'
[44] FORM COLNAMES '/CL LMT/CL LMT/MID PT///FREQ/ FREQ/ FREG/' 0 ',
[45] FOKM $\triangle F M T(L C ; U C ; Y ; F ; R F ; C F ; R C F) \diamond$ • '

[47] '
[48] STAR
[49] $\mathrm{HS}+1$
[50] $\overline{P C} *]^{\prime}$
[51〕 20 40 PLOT RFVSY
[52] STAR
[53] PNAME ${ }^{\prime}$ MEAN MEDIAN RANGE VARIANCE STAND DEV'
[54] $P A R A M+P M, P M D, P R, P V, P S D$
[55] FORM CENTER 'PARAMETERS OF POPULATION'
[56] 'X20,9A1,F14.2' $\triangle$ FMT(5 9 คPNAME;PAR.AM)
[57] STAR
$\nabla$
$\nabla S .4 M P D I S T[\square] \nabla$
$\nabla$ SAMPDIST;FORM1;PROB;R;SCW;SLC;SDM; SDMD; SDF; SDV; SD SD; SDY; SUC; XX
[1]
[2] คAYN, CENTER, COLNMAES, AND $\triangle E M T$
[3] LOOP:'ENTER THE VARIABLE NAME OF ONE STATISTIC OF YOUR INTEREST.'
[4] 'THE VARIABLE NAMES AKE AS FOLLOWS:'
[5] 'X20,9A1,X12,9A1' COLNAMES '/STATISTICS/VARIABLE/' $\leqslant$ '

[7] $X X+\square$
[8] $S D S D \leftarrow(S D V \leftarrow(+/(X X-S D M \leftarrow(+/ X X) \div S[2]) \star 2) \div S[2]) \star 0.5$
[9] $S D M D+0.5 x+/ X X[(\Delta X X)[\mid r-0.5 \quad 0.5 \times 1+\rho X X]]$
[10] $S D F \leftarrow \Gamma / X X-L / X X$
[11] $S T A T S \leftarrow S D M, S D M D, S D R, S D V, S D S D$
[12] $S T A R$
[13] 'X10.9A1,F20.2' CENTER 'PAKAMETERS OF SAMPLING DISTRIBUTION'
[14] 'X10,9A1,F20.2' $\triangle F M T((59 \rho P N A M) ; S T A T S)$
[15] STAR
[16] 'SAMPLING DISTRIBUTION OF THE STATISTIC IS PRESENTED IN THE FORM'
[17] 'OF PROBABILITY DISTRIBUTION AND GKAPH BELOW: "
[18] BUT, FIRST, ENTER THE LOWER CLASS LIMIT VALUE OF THE FIRST CLASS, CLASS
WIDTH, AND NO. OF'
$[19 j \quad$ 'CLASSES YOU NEED FOR THE SAMPLING DISTRIBUTION, E.G., 0 5 $10:$ :

): "
[21] $F \leftarrow \square$
[22] $S D Y \leftarrow(R[1]+0.5 \times R[2])+S C W \leftarrow(((1 R[3])-1) \times R[2])$
$[23] \quad S U C+\pi[2]+S L C+R[1]+S C W$
$[24] \quad \operatorname{PROB} \leftarrow(+/(1 R[3]) \circ .=\Gamma(X X-K[1]) \div R[2]) \div S[2]$
[25] STAR
[26] FORM1 + X10,4F14.2'
[27] FORM1 CENTER 'SAMPLING DISTRIBUTION'
[28] FORM1 COLNAMES '/ LOWER/ UPPEF/ CLASS/ PROB/'
[29] FORM1 COLNAMES '/CL LMT/CL LMT/MID PT// /' © '
[30] FORM1 $\triangle F M T(S L C ; S U C ; S D Y ; P R O B) \diamond 1$.
[31] 'X47, ปTOTAL®,F14.2' $\triangle F M T(+/ P R O B)$
[32] STAR
[33] $\quad \mathrm{HS}+1$
[34] $\overline{P C}{ }^{*} \square^{\prime}$
[35] $20 \quad 40$ PLOT PROB VS SDY
[36] STAR
[37] + LOOP×,ANS $A Y N$ WOULD YOU LIKE TO DEVELOP THE SAMPLING DISTRIBUTION FOR A NEW STATISTIC?'
$\nabla$

```
    \nabla SIMUSAMPLE;ANS;CF;I;J;P;PN;PNAME;S;SAMPLE;SM;SMD;SR;SV;SSD;SMS;SMDS;SRS;
        SV S;SSDS;STAR;SY;Y
[1] qTHIS FUNCTION REQUIRES THE FUNCTIONS AKI, AYN, POPDIST, AND SAMPDIST.
[2] 'A POPULATION DATA TO BE ENTERED AS INPUT MAY BE IN THE FORM
    OF A VECTOR OF INDIVIDUAL VaLUES (UNGROUPED DATA) OR IN THE FORM
    of frequency (OR probability) distructions. Please follow the infut
    INSTRUCTIONS BELOW CAREFULLY'
[3] -SAM\times1ANS&AYN 'HAVE you alReady entered the population data? type yes or
    NO.'
[4] POP:POPDIST
[5] SAM:'ENTER THE SAMPLE SIZE AND THE NUMBER OF REPLICATIONS DESIRED, E.G., 2
        O 30.'
[6] 'SAMPLE SIZE MUST BE LESS thaN 100 AND NO. OF REPLICATIONS MUST BE NO GfE
    ATER THAN 50.'
[7] S+[
[8] ->DATA*(((S[1]<100)^S[2]\leq50)
[9] ' TRY AGAIN.'
[10] +SAM
[11] DATA:I+0
[12] SMS+SMDS+SRS+SVS+SSDS+10
[13] FEPL:I+I+1
[14] SAMPLE*10
[15] J*0
[16] SAMP:J+J+1
[17] FN+?S\rhoPN
[18] SY+Y[G+1+(RN[J;I]\leqCF)/(1P[3])]
[19] SAMPLE+SAMPLE,SY
[20] }+(J<S[1])/SAM
[21] SSD+(SV+(+/(SAMPLE-SM+(+/SAMPLE)\divS[1])*2)\divS[1]-1)*
    0.5
[22] SMD\leftarrow0.5x+/SAMPLE[(\triangleSAMPLE)[|f - 0.5 0.5 x + + SAMPLE]]
[23] SR+[/SAMPLE-L/SAMPLE
[24] SMS*SMS,SM
[25] SMDS+SMDS,SMD
[26] SRS+SRS,SR
[27] SVS+SVS,SV
[28] SSDS+SSDS.SSD
[29] +(I<S[2])/REPL
[30] SAMPDIST
[31] ->SAM\times1ANS+AYN 'WOULD YOU LIKE TO RESPECIFY SAMPLE SIZE AND/OR NO. OF REPL
    ICATIONS?'\diamond2 1 \rho' '
[32] ANS+AKI 'WOULD you LIKE TO CONTINUE EXERCISE WITH A NEW POPULATION?'
[33] }+(('Y'\inANS),'N'\inANS)/POP,
\nabla
```

- 


# SETTING THE SIZE OF THE SALES FORCE <br> Jack R. Dauner <br> Associate Professor of Marketing <br> College of Business Administration <br> The University of Akron <br> Akron, Ohio 

DESCRIPTION

This program facilitates the analysis and determination of the number of salesmen to employ in each sales district and hence in a company's entire sales force. The original mathematical model was developed by Professor Zarrel V. Lambert and published in the book Setting the Size for the Sales Force by the Center for Research of the College of Business Administration, The Pennsylvania State University (1968). The model is based on a case study which uses a company that manufactures and markets medical and industrial X-Ray equipment, accessories, and supplies.

The program SALESFORCE can be used to determine the number of salesmen and the estimated change in the company's gross profits where
$E C P=$ Estimated change in the company's gross profits less the change in personal selling costs including commissions.
$R=$ Salesmen's commission rate based on gross profits.
MUI $=$ Gross markup percentage on product cost in district.
PMI = Product mix ratio in district.
$P I=$ Selling price index in district.
SI = Number of Salesmen employed by the company in district.
$C=$ Average out-of-pocket costs per salesmen.
$N=$ Number of salesmen by which the sales force in the district is to be increased or decreased.

NLOW $=$ Minimum number of salesmen in district.
NMAX $=$ Maximum number of salesmen in the district.
To begin the use of the program, type SALESFORCE and then enter the inputs as requested. The number of values entered (e.g., the number of sales districts) must be the same for each of the questions or an error condition will result. In the sample shown in the following section, there were seven districts in the company, so seven values had to be entered for each question. In the last question, the number of salesmen to be evaluated is entered.

## PROGRAM USAGE

```
    SALESFORCE
ENTER SALESMAN COMMISSION RATE BASED ON GROSS PROFITS
\square:
    .05 .05 .05 .05 .05 .05 .05
ENTER GROSS MARKUP PERCENTAGE ON PRODUCT COST IN DISTRICT
[:
    9 13 12 10 9 4 12
ENTER PRODUCT MIX RATIO IN DISTRICT
\square:
    51.29 13.40 42.03 25.72 19.91 33.48 38.79
ENTER SELLING PRICE INDEX IN DISTRICT
[:
    109113 112 110 109 104 112
ENTER NUMBER OF SALESMEN EMPLOYED IN DISTRICT
]:
    6
ENTER AVERAGE OUT-OF-POCKET COSTS PER SALESMAN
\square:
    8269 8269 8269 8269 8269 8269 8269
ENTER RANGE OF SALESMEN TO TEST (ENTER MINIMUM AND MAXIMUM)
\square:
    110
```

| $N$ |  |  |  |  |  |  |  |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1 | 26779946.13 | 1581457.77 | 20216653.97 | 23562427.73 | 4940102.33 | 4564756.18 | 2190749.47 |
| 2 | 29731047.23 | 1975811.33 | 22809048.04 | 25384674.28 | 5692961.91 | 5259882.28 | 3006285.05 |
| 3 | 32603351.61 | 2348825.87 | 25322386.26 | 27171391.88 | 6418860.62 | 5930092.57 | 3763592.10 |
| 4 | 35407418.77 | 2705654.73 | 27768583.72 | 28926155.15 | 7122441.86 | 6579678.21 | 4480323.57 |
| 5 | 38151481.51 | 3049551.02 | 30156537.90 | 30651932.71 | 7807069.24 | 7211747.70 | 5166278.42 |
| 6 | 40842123.54 | 3382742.07 | 32493563.78 | 32351225.83 | 8475282.77 | 7828648.36 | 5827642.33 |
| 7 | 43484719.58 | 3706841.34 | 34784971.17 | 34026168.14 | 9129062.77 | 8432210.32 | 6468650.50 |
| 8 | 46083733.21 | 4023067.22 | 37035439.74 | 35678599.28 | 9769992.88 | 9023897.08 | 7092370.91 |
| 9 | 48642925.28 | 4332369.63 | 39248772.81 | 37310120.24 | 10399365.96 | 9604903.44 | 7701120.26 |
| 10 | 51165503.90 | 4635508.22 | 41428174.89 | 38922135.84 | 11018255.68 | 10176221.62 | 8296704.83 |

## PROGRAM DESCRIPTION

```
\nabla SALESFORCE;C;ECP;ECP1;ECP2;ECP3;ECP4;ECP5;MUI;N;NLOW;NMAX;PI;PMI;N;SI
[1] ^THIS PROGKAM REQUIRES THE PUBLIC EUNCTION \triangleFMT
[2] 'ENTER SALESMAN COMMISSION RATE BASED ON GROSS PROFITS' & R*口
[3] 'ENTER GKOSS MARKUP PERCENTAGE ON PRODUCT COST IN DISTRICT' 人 MUI*口
[4] 'ENTER PRODUCT MIX FATIO IN DISTRICT' « PMI\leftarrow\square
[5] 'ENTER SELLING PRICE INDEX IN DISTRICT* O PI*口
[6] 'ENTER NUMBER OF SALESMEN EMPLOYED IN DISTRICT' O SI&\square
[7] 'ENTER AVERAGE OUT-OF-POCKET COSTS PER SALESMAN' \diamond C+\square
[8] 'ENTER RANGE OF SALESMEN TO TEST (ENTER MINIMUM AND MAXIMUM)' < IN +\square
[9] NMAX+IN[2]
[10] N+IN[1]
[11] ECP+10
[12] A:ECP1\leftarrow409220750
[13] ECP2+PMI*1.169518
[14] ECP3*PI*-2.645349
[15] ECP4*(SI+N)*0.7847286
[16] ECP5*SI*0.7847286
[17] ECPG&((1-K)\timesMUI\timesECP1\timesECP2\timesECP3\timesECP4\timesECP5)-(C\timesN)
[18] ECP+ECP,N,ECP6
[19] N+N+1
[20] }+(N<(NMAX+1))/
[21] 'N ESTIMATED NET CHANGE IN PROFITS'
[22] ECP+(NM.AX,(1+\rhoR)) \rhoECP
```



```
\nabla
```


# SIMULATION OF A THREE STAGE ORDER/SHIPMENT SYSTEM <br> John L. Harpel1 <br> Assistant Professor of Management <br> West Virginia University <br> Morgantown, West Virginia 

DESCRIPTION

The accompanying function $\operatorname{INVNTRY}$ is a simple simulation exercise based upon the type of format used by Jay Forrester in his book Industrial Dynamics. The pincipal use of this program (or function) is to show the concept of simulation and the effects of manipulating decision rules to undergraduate business students. However, it is likely to be of interest to anyone desiring an understanding of simulation. While the program was developed during an introductory course in APL at UCLA, a strong attempt was made to keep the program independent of the UCLA system. Only the plotting ability is not self-contained and it can be ignored.

The system which is to be simulated is shown in Figure 1, where lags 1-3 represent delays from order placement to order shipment and lags $4-6$ represent delays from order shipment to order receipt.

Internal to the program are the following variables and relationships:

| $\frac{\text { YARS }}{N}$ | $\frac{\text { MEANING }}{\text { Number (period) }}$ | $\frac{\text { COMPUTATION }}{\text { Time period counter }}$ |
| :--- | :--- | :--- |
| BI | Beginning Inventory <br> = Ending inventory of preceding <br> period |  |
| DMND | Demand | Input data <br> SALES |
| Amount Sold Smaller of BI or DMND <br> BAL Balance in Stock | BI-SALES (or SHIP) |  |
| SHIP | Amount Shipped | Smaller of BI or Order Placed |


| $\frac{\text { YAR }}{\text { ORD }}$ |  | MEANING |
| :--- | :--- | :--- |
| Order Placed | COMPUTATION |  |
| REC | Amount Received | SHIP of LAG4,5, or 6 periods <br> prior |
| EI | Ending Inventory | BAL+REC |

*A somewhat arbitrary rule.
It is suggested that the first time the program is run, the user should ask for an explanation each time it is offered. This is done by typing a "2" when asked.


Figure 1

## PROGRAM USAGE

```
    INVNTRY
    FOR PROGRAM DESCRIPTION, SEE DESCRIBE FUNCTION
SET LAGS? (ENTER O FOR NO, 1 FOR YES, AND 2 FOR EXPLANATION.
\square:
ENTERING A 1 ALLOWS YOU TO CHANGE THE SIX DELAYS FOR THE ORDER
TO BE SHIPPED FROM A)PETAIL TO WHOLESALE, B)WHOLESALE TO FACTORY, AND
C)FACTORY WAREHOUSE AND WHOLESALE AND F)FACTORY AND FACTORY WAREHOUSE.
ENTER 1 FOR YES AND SIX RESPECTIVE NUMBERS (ENTER SPACES ONLY BETWEEN
THEM). IF YOU ENTER 2 FOR NO, THE DEEAULT IS 2 2 4 0 0 0
SET LAGS? (ENTER O FOR NO, 1 EOR YES, AND 2 FOR EXPLANATION.
\square:
ENTER 6 LAGS
\square:
    1}10144%141
ENTER NUMBER OF PERIODS FOR PROGRAM TO RUN.(SUGGEST 10 MAX FOR FIRST TRTAL.)
[]
    10
SELECT ONE OF THE FOLLOWING OPTIONS AND ENTER THE CORRESPONDING NUMBER:
    1 I WILL ENTER MY OWN SALES DATA.
    2 USE AN EQUALLY LIKELY RANDOM NUMBER GENERATOR TO
    CREATE SALES DATA.
    3 USE CONSTANT INCREASE/DECPEASE RANDOM NUMBER GENERATOR
    TO CREATE SALES DATA.
    4 WHAT ARE YOU TALKING ABOUT? (EXPLANATION)
\square:
4
```


## PROGRAM DESCRIPTION

－INVNTEY；LAG1；LAG2；LAG3；LAG4；LAG5；LAG6；FEAL；RBI；RDMND；REI；RORD；RREC；LAG； RSALES；SLSV；TDMND；TEACSHIP；TEEAL；TFBI；TFEI；TEPEC
[2] a this is the main pfogram.
[3] a the folloning variables may pe associaten hith the numbers used in the
[4] aMATRTX(M) COLUYNS AND TITH THE FLOTFORNAT CALLS:



[8] A $N N+21$ く FACSHIP+20
[9] a initialize lags (delays) in ordefs and shifnents---go to getlag function.
[10] XLAG+GETLAG
[11] LAG1+XLAG[1] © LAG2+XLAG[2] OLAG3+XLAG[3]
[12] LAG4+XLAG[4] © LAG5+XLAG[5] O LAGG+XLAG[6]
[13] a FIND MAXIMUM LAG.
[14] $L A G+\Gamma / X L A G$
[15] a INItialize matrix with steady state conditions.
[16] VINV + (LAG, 1) p 200
[17] VO5 $+(L A G, 5) \rho 100$
[18] VO4-(LAG,4) 100
[19] VINV2+(LAG,2)p200
[20] SSN $-1 \times(L A G, 1) \rho, L A G$
[21] M+VINV,VO5,VINV2,VO4,VINV2,VO4,VINV2,SSN
[22] $v+0$
[23] a MAIN PFOGRAV
[24] ENTEF NUMREF OF FFRIODS FOR PROGFAM TO RUN. (SUGGEST 10 MAX FOR GIRST TEI
AL.).
[25] LOOPS:K+NOPES $+\square$
[26] a GO TO SI'SALF FUNCTIOM AND FETUFM NITH SLSV (SALES VECTOR).
[27] SLSV+SIMSALE NOPES
[28] 2:T[MND+1ヶSLSV
[29] SLSV+1+SLSV
[30] a COMFUTE NEW PEFIOD valuFs.
[31] MOFFS $+N \cap P F S-1$

[33] TWSHIE $(((\operatorname{IAC} 1=0) \times T F O F D)+((\operatorname{LAG} 1 \times 0) \times M[L A G 1 ; 5])) L T W E I+M[1 ; 13]$
[34] TPFI + TPRAL + TRPEC $+((L A G 4=0) \times T W S H I P)+((L A G 4 \times 0) \times M[(1 「 L A G 4) ; 91)$
[35] TWOFL-01200-TWEAL4TWEI-TWSHIP
[36] TFSHIF+(((LAG2=0)×TWOFD)+((LAG2×0)×M[LAG2;11]))LTFEI+M[1; 19]
[37] TWEI T TWEAL+TWFEC+((LAC5=0) $\times$ TFSHIP $)+((L A G 5 \times 0) \times N[(1\lceil L A G 5) ; 15])$
[38] TFOFD+0「200-TFEAL-TFBI-TFSHIP
[39] TFACSHIP $+((\operatorname{LAG} 3=0) \times T F O R D)+(($ LAG 3 $\times 0) \times M[$ LAG $3 ; 17])$
$[40)$ TFEI + TFFAI + TEFEC $+(($ LAG6=0 $) \times$ TFACSHIF $)+(($ LAGG×0 $) \times M[(1\lceil L A G 6) ; 20])$
[41] N+N+1
[42] a fUT period values in a vector ald ado that vector to the matifx.
[43] AVROW1+(TRFI, TDMND, SALES, TFRAL,TROFD,TRFEC, TREI,TWRI, TWSHIP, TWBAL, TWOFD,
TAFEC,TWEI)
[44) AVFOW2+(TFFI, TFSHIP, TFRAL, TFOFD, TFFEC, TFEI, TFACSHIP,N)
[45] VFOW + (AVROW1, AVROW2)
[46] M+VRON,[1] M
[47] $\rightarrow($ NOPES $>0) / 2$
[48] a PRINT TARIE HFADING.
[49] | RETAILERS | WHOLESALEFS |
FACTOFY WAFEHOUSE I EACTORY.
[50] ,

[52] , N 1 FI PNND SALFS PAL OFD FEC EI 1 RI SHIP PAL OFD REC EI ।
RI SHIP PAL ORD DEC FI ISHIP N'
[53] a catfnate poth end colunens--flit matrix ovfe--print results.
[54] K+1K
[55] MPRTNT+ $\mathrm{AM}[K$; ]
[56] MPRINT[;211,MPPIMT
[57] SIMPLOT
$\nabla$

```
        \nablaGETLAG[口1\nabla
    \nabla XLAG+GFTLAG
[1] LLILI:LAG1+2 © LAS2+2< LAG3+4
[2] LAG4+LAG5-LAG6+0
[3] XLAG+LAG1,LAG2,IAG3,IAG4,IAG5,LAG6
[4] SI:'SET LAGS? (FHTEF 0 GOF NO, 1 FOF yES, AND 2 EOF fyplanation.'
[5] J.JJJ +[]
[6] ->(0^JJJJ\epsilon 0 1 2)/SL,
[7] }->(JJJJ=2)/EXPAI
[8] ->(JJJJJ=0)/0
[9] 'ENTER 6 LAGS.
[10] G5T:XLAG+[C
[11] }->(XIAG\in110)/
[12] 'GIVE 6 NUMBERS, EACH BETWFEN O AND 12.'
[13] ->GFT
[14] E
[15] fXPAIN:'ENTERING A 1 ALLOWS YOU TO CHANGE THE SIX DFLAYS FOR THE OFLER'
[16] 'TO RE SHIPPED FRON A)FETAII TO WHOLFSALE, FIWHOLESALE TO FACTOFY, AND'
[17] 'C)FACTORY WAFEHOUSE ANH WHOLESALF AND FIEACTORY AND FACTORY WAFEGOUSE.'
[18] 'enter 1 fog yes and Six respfctive nungers (futef spages only rethebn'
[19] THEM). IE YOU ENTPF 2 FOR NO, THE PFEAULTT IS 2 2 4 0 0 0,
[20] ->SL
    \nabla
    \nabla SLSV+SIMSALE NOPES;SLS
[1] a this gunction deternines and geEdS salfs data to main gunC'Ion(invntgy)
[2] blor:'SELECT ONE of the following options and enter the coffesponitng numb
        ER:'
[3]
[4] , , 1 I WILL ENTER NY OWN SALES DATA.'
```



```
[7] , CFEATE SALFS DATA.'
[8] ,,
[9] , 3 USE CONSTANm INCFFASE/DECREASE EANDOM NUMBEF GENERATOF'
[10] , TO CREATE SALES DATA.'
[11] ''' 4 4 ' What are you talking about? (Explanation)'
[13] ,'
[14] TYPESLS-D
[15] ->((TYPESLSG 1 2 3 4)\pi(0OTYPESLS=0:0):1GLOE
[16] }->(TYPESIS=4)/XXPLAINN
[1]] }->(TYPFSLS=3)/IDCRSE
[18] }->(TYPFSLS=2)/FLPAND
[19] BOOBOO:'ENTER SALES DATA FOR ';NOPFS;' PEFTODS.(F.G. 110 110 90 90 )'
「20] SLSV+[
[21] a CHFCK MANUALLY INPUT DATA.
[22] }->((NOPES<\rhoSLSV),(NOPFS=\rhoSLSV),(NOPFS>OSLSV))/L,1,L2,L3
[23] L1:'TOO MUCH DATA. TRY AGAIN..........'
[24] }->\mathrm{ BOOBOO
[25] L3:'TOO LITTLP DATA. GIVE IT AN\capTHFP TPY***********'
[26] }->\mathrm{ BOOBOO
[27] L2:->0
[28] ELPAND:SLSV+89+?NOPFSO21
[29] }->
〔30] IDCPSE:SLSV+100+(?NOPESO19)-?NOFES@19
[31] }->
[32] XXPLAINN:' EVERYTHTNG IN THIS PFOGFAM IS IMPLICIT EXCFPT FOF THF,
[33] 'CUSTOMFR DENAND. IN THF PAST THIS DEMAND LAS PEEN ]CO PEF FERIOD,'
[34] 'fESULTING IN AN FOUILIBFIU:1 CONDITION (OFTEN CALLFD THE STEADY STATE,
[35] 'CONDITION). TO THE EXTENT THAM UNH CHANGE THE IF'MAND FRON 100, YOU WIIL
```

```
[36] 'UPSET thIS EQUILIbRIUM. YoU HAVE SEVERAL optIonS fob dEtEPMINING the'
[37] 'CUSTOMEF DFMAND, NAMFIY:'
[38] ",
[39] , 1. IF yOU ENTFF A 1, THE PFOGFAM WILL FFQUIRE yOU TO FEED IN'
[40] ', THE DFNAND FIGURES FOF EACH OF THF PEFIODS. yOU MUST FNTER'
[4]] , A FOW OF EICUFES (SFPAFATFD EY SPACFS) FQUAL IN NUMEEF TO'
[42] , THE NUMRFP OF PFPTODS YOU HAVF ALREADY ENTEPRD.'
[43] , 2. IF YOU ENTEF A 2, THE COMPUTEF WILL GENERATF A FANDOM NUPBER'
FPOM A CONSTANT (OF EQUALLY LIKFLY) PFORABILITY DISTRIBUTION FO
    R' }\mp@subsup{}{}{\prime
[45] SALES RETWEE! 90 AND 110. TO CHANGE 90 AND 110 FIND THE PFOGRA
[46]
[4-7
[4?]
[48]
[49]
[50]
[51]
[52]
[53]
[53]
[54]
[55] ,'
[56] ->BLOR
    \nabla
    \nabla SIMPLOT
[1] AA:'DO YOU WANT to plOT ANY RESULTS? ENTER O FOP NO; 1 FOR YES; 2 GOR EXPL
    ANATION.'
[2] 224[1
[3] }->(1\not=2Z\epsilon0 1 2)/A
[4] A EXPLAMATION
[5] }->(ZZ=2)/EXPPL
[6] a NO
[]] ->(ZZ=0)/0
[8] AYES
[9] aUCLA
[10] NN+(1+(NOPES\leq60))\times0NOPFS
[11] YES:'HOW MANY VAFIABLES DO YOU WANT TO PLOT? (MAXIMMM OF 3)'
[12] NUMB + प
[13] }->(\rho:0\not=\rho\rhoNUMB)/YE
[14] ->(1×NUMR\in13)/YES
[15] 'THE PEPIOD NUMBEPS WILL BF ON THF HORIZONTAL AXIS UNLESS YOU CHOSE ONLY
    ONE VARIABLE.'
[16] ''
[17] "'
[18] ' USE THE COLUMN NUMPRFS IN THE PPFCFDING TABLE TO ENTER THE,
[19] 'VARIARLFS FOR THE HORIZONTAL AXIS (VFRTICAL AXIS IS ONLY ONE VARIABLE).'
[20] '(F.G. FOR PFTAIT PI, USE 1; FOP FACTORY WARFHOUSF,USE 19).'
[21] ''
[22] ,'
[23] ->(NUMR=1)/ONE
[24] }->(NUMB=2)/TW
```

```
「25
THREE: 'WHAT ARE THE THRFE VARIABLES? (ENTEF WITH SPACES ONLY EFTWFEN.)'
26] TROIS-\square
[2?] }->(3\not=TROIS)/THFE
[28] +(3z+/(TPOISE120))/THREE
[29] O+TPOIS[1] 介 H+TFOIS[2] 介 I+TFOIS[3]
[30] ค UCLA-NEXT EIVE LINES.
[31] 'O REPRESENTS ';G
[32] '* EEPRESENTS ';H
[33] '。REPPESENTS ';I
[34] 'PEAD THESE VAPIABLES ON THE LFET AXIS.'
[35] (20,NN) PLOT MPFINT[;G] AND MPRINT「;H] AND MPEINT「;I]VS NERINT「;
        21]
[36] }->
[37] TWO:'WHAT AFE THE TWO VARIARLE NUMBEFS? (LIST WTTH A SPACF ONLY EFTWEFN.)'
[38] DEUX+\square
[39] }->(2\not=\rhoDEUX)/TW
[40] }->(2x+/(DEUX\in120))/TW
[41] G+DEUX[1] © }H+DEUX[2]
[42] ค UCLA-NEXT EOUR ITNES
[43] 'O PEPFESENTS ';%
[44] '* REPFESENTS ; H
[45] 'PEAD THFSE VARIABLFS ON THE IFFT AYIS.'
[46] (20,NN) PLOT MPRINT[;G] AND MPFINT[;H] VS MPFINT[;21]
[4?] }->
[48] ONE:' FNTEF VAFIABLE NJMBFP TO BF FLOTTED ON HOFIZONTAL AXIS.'
[49] UNE+\square
[50] }->(1\pm\rhoUNE)/ON
[51] }->(1x+/(UNE\in120))/ON
[52] คUCLA
[53] ONE:PFFT&1
[54] a UCISA
[55] (20,NN) PLOT MPRINT「;UNE] AND MPRINT[;21]
[56] }->
15?] EXPLN:'THIS FUNCTION(SINPLOT) UTILIZES THE PLOTEOFMAT FOUTINF IN'
[58] 'LIBFAFY 1 AT UCLA. TO JSF, YOU WILL NEFD TO HAVE ALREADY IOADED THE'
[59] 'PLOTFORMAT FUNCTION INTO YOUR WOFKSPACE. YOU NAY RE AELE TO USE'
[60] 'FLOTFORMATS FROM OTHER LIBRARIES BY CALLING PFOGFAM LINES MAFKED BY A'
[61] '''UCI,A'' JUST ABOVE THEM.'
[62] }->A
\nabla
```


## MULTIVARIATE T-SQUARE TEST

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## DESCRIPTION

The program MULTEST is designed to test a hypothesis concerning a vector of means using Hotelling's $\mathrm{T}^{2}$ statistic. It is designed for instructional use in an intermediate or advanced level statistical methods course covering multivariate statistical methods.

The user is required to specify the hypothesis to be tested and to input the sample data. The program then computes and prints the sample variance-covariance matrix and its inverse. Finally the program computes and prints Hotelling's $\mathrm{T}^{2}$ statistic and the associated F value.

Numerical examples of the multivariate $\mathrm{T}^{2}$ test concerning means may be found in the following references:

Bolch, B. W. and Huang, C. J., Multivariate Statistical
Methods for Business and Economics, Englewood Cliffs:
Prentice-Ha11, Inc., 1974.
Cooley, W. W. and Lohnes, P. R., Multivariate Data
Analysis, New York: John Wiley and Sons, Inc., 1971.
Morrison, Donald F., Multivariate Statistical Methods, New York: McGraw-Hill Book Company, 1967.

## Instructions for Use

In order to use MULTEST the user must copy MULTEST into his workspace as well as the supporting functions COLNAMES, DATAMAT, INPUT, RWTD, and $\triangle F M T$. DATAMAT and INPUT are functions written especially for use with MULTEST and should always be saved in the
same library.
MULTEST is a niladic function which supplies instructions to the user at each step. Once the functions have been copied into the user's workspace, the function is activated by simply typing MULTEST and striking the return key.

## PROGRAM USAGE

MULTEST
THIS PROGRAM TESTS THE HYPOTHESIS THAT A VECTOR OF MEANS IS EQUAL TO A VECTOR OF CONSTANTS. FOR EXAMPLE:
$H O:[U(1)=100, U(2)=75, U(3)=543, \ldots, U(P)=25]$.
WHAT IS THE NUMBER OF VARIABLES FOR THIS PROBLEM?
$\square$ :

ENTER THE VALUES FOR YOUR NULL HYPOTHESIS BELOW - ONE VALUE ON EACH LINE. $U(1)=$
$\square$ :
$U(2)=$
$\square$ :
20
$U(3)=$
$\square:$
30
THE HYPOTHESIS YOU WISH TO TEST IS
$U(1)=10$
$U(2)=20$
$U(3)=30$
ENTER YOUR DATA WITH ONE OBSERVATION VECTOR ON EACH ROW. EACH ROW SHOULD CONTAIN 3 VARIABLES. BELOW THE LAST ROW TYPE: STOP
[:
151640
$\square:$
$14 \quad 1138$
$\square:$
18938
$\square:$
$1716 \quad 37$
$\square:$
141231
$\square:$
$9 \quad 15 \quad 37$
$\square:$
151639
$\square:$
$13 \quad 18 \quad 33$
$\square:$
161235
[]:
$18 \quad 11 \quad 38$
$\square:$
STOP

YOUR DATA MAMRIX CONTAINS 10 FOWS AND 3 COLUMNS. PLEASE CHECK TO SEE THAT IT IS COFFECT.

```
    1 15 16 40
    24411 38
    18 9 38
    17 16 37
    5 14 12 31
    9 15 37
    7 15 16 39
    8 13 18 33
    9}1612123
    10}1811
IE DATA MATRIX IS CORRECT TYPE: GOOD
    IF DATA MATRIX IS NOT CORRECT TYPE: CHANGE
CHANGE
WHAT IS THE NUMBER OE THE FOW YOU WISH TO CHANGE?
\square:
    6
ENTER THE CORRECT OBSERVATION FOR ROW 6
\square:
    10 15 38
DO YOU WISH TO CHANGE ANOTHER ROW?
NO
YOUF DATA MATRIX IS
    15 16 40
    14 11 38
    18 9 38
    17 16 37
    14 12 31
    10 15 38
    15 16 39
    13 18 33
    16 12 35
18 11 38
```

$\operatorname{MEAN}(1) \operatorname{MEAN}(2) \operatorname{MEAN}(3)$
$15.00 \quad 13.60 \quad 36.70$

THE SUMS OF SQUARES AND CROSS PFODUCTS ARE

| 2304 | 2010 | 5517 |
| ---: | ---: | ---: |
| 2010 | 1928 | 4990 |
| 5517 | 4990 | 13541 |

THE SAMPLE VARIANCE COVARIANCE MARTRIX IS
$-6$
-3. 333333333

1. 333333333
-3. 333333333
2. 333333333
$8.711111111 \quad$ - 0.1333333333
-0.1333333333
3. 011111111

THE INVERSE OE THE SAMPLE VARIANCE COVARIANCE MATRIX IS

| 0.2212789951 | 0.08413081272 | -0.03542844613 |
| :---: | :---: | :---: |
| 0.08413081272 | 0.1468119097 | 0.01155888295 |
| -03542844613 | 0.01155888295 | 0.1305308002 |
| $T_{-}-S Q U R E$ | $F-C O M P U T E D$ |  |
| 106.4 | 27.6 |  |

## PROGRAM DESCRIPTION

```
    \nabla R+MULTEST;C;COUNT;D;F;INDEX;INVERSE;KXX;S;SUMS;TSQ
[1] ค THIS PROGRAM REQUIRES THE USE OF FUNCTIONS: DATAMAT, COLNAMES,
[2j คINPUT, RWTD, AND \triangleFMT
[3] & THE VARIABLES N, X, MEAN, AND SS ARE GLOBAL VARIABLES SINCE THEY ARE
[4] ~REQUIRED IN BOTH DATAMAT AND MULTEST.
[5] 'THIS PROGFAM TESTS THE HYPOTHESIS THAT A VECTOR OF MEANS IS EQUAL TO'
[6] 'A VECTOR OF CONSTANTS. EOR EXAMPLE:'
[7] , HO: [U(1)=100, U(2)=75,U(3)=543, ... ,U(P)=25].'
[8] 'WHAT IS THE NUMBER OF VARIABLES FOR THIS PROBLEM?'
[9] P& [
[10] 'ENTER THE VALUES FOR YOUR NULL HYPOTHESIS BELOW - ONE VALUE ON EACH LIN
    E.'
[11] U&10
[12] COUNT+1
[13] ค THIS LOOP REQUESTS THE USEF TO INPUT THE HYPOTHETICAL VALUES FOR MU(1) T
    OMU(P). \triangleFMT IS REQUIRED.
[14] LOOP:U\leftarrowU,INPUT 'ロU(П,I2,\square)=\square' \triangleFMT(COUNT) \diamond COUNT\leftarrowCOUNT+1
[15] ->LOOP\times1 (COUNT\leqP)
[16] 'THE HYPOTHESIS YOU WISH TO TEST IS'
[17] 'U(1) =':1+U % NUMBER+2
[18] LP1:'U(';NUMBER;') =';1\uparrow(NUMBER-1)\phiU< NUMBER&NUMBER+1
[19] }->LE1\times1 (NUMBER\leqP
[20] DATAMAT
[21] SUMS+(+4X)
[22] C+MEANSO.xSUMS
[23] }KXX+SS-
[24j S\leftarrowKXX\div(N-1)
[25] , '
[26] 'THE SAMPLE VARIANCE COVARIANCE MARTRIX IS'
[27] ,
[28] S
[29] ,
[30] 'THE INVERSE OF THE SAMPLE VARIANCE COVARIANCE MATRIX IS'
[31] , '
```



```
[33] D\leftarrow(MEANS-U)
[34] TSQ 
[35] A THE FOLLOWING LINES FORMAT THE PRINTING OF THE VALUES FOR T-SQUARE AND F
[36] E\leftarrowTSQ\times(N-P):(N-1)\timesP
[37] FS*'2F12.1'
[38] ' '
[39] FS COLNAMES '/T-SQUARE/E-COMPUTED'
[40] '.
[41] FS \triangleFMT(TSQ;F)
\nabla
```

```
    \nabla R+DATAMAT;FS;H;INDEX;V
        - ENTER YOUR DATA WITH ONE OBSERVATION VECTOR ON EACH ROW. EACH ROW -
        'SHOULD CONTAIN ';P;' VARIABLES. BELOW THE LAST ROW TYPE: STOP'
    STOP+35.34758697821
    X+( 0,P)\rho0
    REPEAT:V+.\square
        +(STOP=1\uparrowV)/NEXT
        *(P=\rhoV)/ADD
        -ERROR'
    +REPEAT
10] ADD:X+X,[1](1,P) \rhoV
[11] ->REPEAT
[12] NEXT:N+1\uparrow(\rhoX)
[13] 'YOUR DATA MATRIX CONTAINS ';N;' ROWS AND ';P;' COLUMNS. PLEASE CHECK'
[14] 'TO SEE THAT IT IS CORRECT.'
[15] . .
[16] ((N,1)\rhoıN),X
[17] IF DATA MATRIX IS CORRECT TYPE: GOOD
            IF DATA MATRIX IS NOT CORRECT TYPE: CHANGE'
[18] CHECK+\square
[19] }->('GOOD'=4\uparrowCHECK)/PRODUC
[20] CHANGE:'WHAT IS the Number of the row you WISH to change?'
[21] INDEX+\square
[22] 'ENTER THE CORRECT OBSERVATION FOR ROW ;INDEX
[23] X[INDEX;]+\square
[24] 'DO YOU WISH tO CHANGE ANOTHER ROW?'
[25] ('YES'=3^[)/CHANGE
[26] 'YoUR DATA MATRIX IS'
[27] ' '
[28] X
[29] , ,
[30] PRODUCT:MEANS + (+\VarangleX)\div1\uparrow\rhoX
[31] SS+(QX)+.×X
[32] H+,'ワ/MEAN(■,I2,\)\boxtimes' \triangleFMT(ıP)
[33] ';
[34] ES&,'I2,MF10.2\' \triangleFMT P
[35] FS COLNAMESH
[36] FS \triangleFMT((1,P) pMEANS)
[37] ,
[38] 'THE SUMS OF SQUARES AND CROSS PRODUCTS ARE'
[39] , '
[40] SS
    \nabla
    \nabla R+INPUT PROM
[1] I1:PROM
[2] }->(1=\rhoR\leftarrow,0)/
[3] 'ENTER ONE VALUE ONLY'
[4] }->\mathrm{ I1
    \nabla
```

CALCULATION OF DISABILITY SETTLEMENT AWARDS

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DESCRIPTION

LUMPSUM is a program designed to discount future streams of income, medical costs, retirement annuities, etc., and reduce these to a lump sum payment in liability cases. For example, a person injured in an automobile accident may have:

1. Lost income between time of injury and settlement of a liability case.
2. Incurred uninsured medical costs during the same period.
3. Been permanently disabled to some degree and therefore lose future income, promotions, and retirement benefits and incur both uninsured maintenance medical costs and periodic uninsured major medical costs.

LUMPSUM will handle this problem and can be used by students, lawyers and economists who wish to calculate the net present value of medical costs and lost income due to the disability of an injured person.

LUMPSUM is a prompted program. The inputs required are:

1. Annual income of the injured person at the time of injury.
2. Age at the time of injury.
3. Present age.
4. Risk-free current interest rate (or some agreed upon interest rate acceptable to litigants), in percentage.
5. Long-run improvement in productivity (real percentage increase in per capita income).
6. Employer contribution to retirement annuity, in percentage of income at time of injury.
7. Age of the injured at the time of future promotions that the employer could have anticipated for the injured.
8. Each promotion as a percentage of income at that age.
9. Based upon current age, the remaining expected life, taken from mortality tables.
10. Continuing uninsured maintenance medical costs as a percentage of income at time of injury due to injury. (For example, the injured may require continuing physical therapy throughout his or her life.)
11. Major future uninsured medical costs: age when they are to be incurred and the dollar amounts. (For example, physicians may suggest the need for one or two major operations to correct the more serious physical aspects of the disability. If so, they should provide current dollar estimates which are then adjusted for inflation at a rate equal to the productivity factor.)
12. Lost income between the time of injury and the time of settlement resulting from the injury.
13. Uninsured medical costs incurred between the time of injury and the settlement.
14. Interest rates for each year of lost income or uninsured medical costs incurred between the time of injury and the settlement.
15. Degree of disability in percentage. (For example, physicians may estimate that the injured has lost $25 \%$ of his or her capacity to continue earning income and pursuing a career.)

The outputs are:

1. The discounted value of future income, including promotions.
2. The discounted value of employer contributions to retirement.
3. The discounted value of uninsured medical maintenance costs, adjusted for cost escalation.
4. The value of lost income and uninsured medical costs between the time of injury and the settlement, compounded by the past annual interest rate.
5. The discounted value of uninsured major medical costs, adjusted for cost escalation.
6. The value of the award, adjusted for the degree of continuing disability.

To illustrate the use of the program, suppose you have the following case:

1. Income at time of injury
$\$ 10,000$
2. Age at time of injury

30 yrs.
3. Present age 35 yrs.
4. Current interest rate ..... 6\%
5. Rate of productivity improvement ..... 3\%
6. Employer's contribution to retirement $12 \%$ of income
7. Anticipated promotions Age Percent of Income40 yrs. 10\%
45 ..... 8\%
50 ..... 6\%
55 ..... 5\%
60 ..... 4\%
8. Remaining life expectancy ..... 35 yrs.
9. Uninsured maintenance medical costs10. Future major medical costsAge10\% of income
40 yrs.Dollars
45 ..... \$250011. Lost income uninsured medical costs, and interestrates since injury.

| Age | Lost <br> Income | Uninsured <br> Medical Costs | Interest <br> Rate |
| :--- | :--- | :---: | :---: |
| 30 yrs. | $\$ 1200$ | $\$ 500$ | $5 \%$ |
| 31 | $\$ 1300$ | $\$ 600$ | $4 \%$ |
| 32 | $\$ 1500$ | $\$ 400$ | $6 \%$ |
| 33 | $\$ 1200$ | $\$ 600$ | $7 \%$ |
| 34 | $\$ 1300$ | $\$ 500$ | $6 \%$ |
| 35 | $\$ 1200$ | $\$ 600$ | $6 \%$ |

12. Degree of disability, in percentage ..... 25\%
Using these data, the following section shows a sample run.

## PROGRAM USAGE

```
    LUMPSUM
ENTER INCOME AT tIME OF INJURY
\square:
    10000
ENTER aGE AT TIME OF INJURY AND PRESENT AGE
\square:
    30 35
enter Current interest rate in percentage
\square:
    6
ENTEk productivity factor in percentage
\square:
    3
enter retirement anNuity in percentage of current income
[:
    12
enter age at promotiom, percentage promotion would be at then income
ENTER ALL PROMOTIONS AND WHEN DONE JUST HIT CARRIAGE RETURN
                            AGE PERCENT
ENTRY: 40 10
ENTRY: 45 8
ENTRY: 50 6
ENTRY: 55 5
ENTRY: 60 4
ENTRY:
BASED ON CUFRENT AGE, ENTER REMAINING YEARS OF LIFE EXPECTANCY FROM
MORTALITY TABLES
\square:
3
ENTER BASIC UNINSURRED MAINTENANCE MEDICAL COSTS AS PERCENT OF INCOME
AT TIME OF INJURY
\square:
1 0
ENTER EStimated age at InCurrence of future major medical costs and
ENTER DOLLAR ANNUAL AMOUNTS of COSTS VALUED IN PRESENT DOLLARS
WHEN ALL mAJOR MEDICAL COST OCCURENCES ARE ENTERED JUST HIT RETURN
    AGE DOLLARS
ENTRY: 40 3000
ENTRY: 45 2500
ENTRY:
FOR AGE INDICATED SINCE INJURY ENTER ANNUAL LOST INCOME, UNINSURED
medical costs in dollar values and interest rates in percent.
    LOST INCOME UNINSMED COSTSS INTEREST RATE
AGE: 30 1200 500 5
AGE: 31 1300 600 4
AGE: 32 1500 400 6
AGE: 33 1200 600 7
AGE: 34 1300 500 6
AGE: 35 1200 600 6
enter PERCENTAGE degree of disability
\square:
    25
```

THE DISCOUNT RATES ARE:

| 0.9708737864 | 0.9425959091 | 0.9151416594 | 0.8884870479 | 0.8626087844 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 0.9275363273 | 0.9005207061 | 0.8742919477 | 0.8488271337 | 0.8241040133 |
| 0.8674779087 | 0.8422115619 | 0.817681128 | 0.7938651728 | 0.7707428862 |
| 0.7945892951 | 0.7714371797 | 0.7489681356 | 0.7271535297 | 0.7059743007 |
| 0.7203819395 | 0.6993999413 | 0.6790290692 | 0.6592515235 | 0.6400500228 |
| 0.6465151746 | 0.6276846355 | 0.6094025587 | 0.5916529696 | 0.5744203589 |

THE DISCOUNTED VALUE OF FUTURE INCOME IS:238005.5728
THE DISCOUNTED VALUE OF THE RETIREMENT ANNUTTY IS:28560.66873
THE DISCOUNTED VALUE OF EXPECTED MAINTENANCE MEDICAL COSTS IS:22487. 22007
THE VALUE OF LOST INCOME AND MEDICAL COSTS SINCE INJURY PLUS INTEREST IS: 13299.63044

THE DISCOUNTED VALUE OF FUTURE MAJOR MEDICAL EXPENSES IS:4448.06114
THE AWARD IS:233425.7725

## PROGRAM DESCRIPTION

LUMPSUM
[1]
athis function requires thee use of public functions inp and ipi
[2] 'ENTER INCOME AT TIME OF INJURY' © INC + INP 1
[3] 'ENTER AGE AT TIME OF INJURY AND PRESENT AGE' \& AGE+INP 2
' ENTER CURRENT INTEREST RATE IN PERCENTAGE' © RATE $($ INP 1) $\div 100$
' ENTER PRODUCTIVITY FACTOR IN PERCENTAGE' \& PROD $+(\operatorname{INP} 1) \div 100$ 'enter retirement annuity in percentage of current income' $R E T+(I N P 1) \div 100$
PROM 20 po
'enter age at promotiom, percentage promotion would be at then income '
[10] 'ENTER aLL PROMOTIONS and WHEN done JUSt hit carriage return'
[11] , AGE PERCENT ,
[12] $L 0: \rightarrow(L 0+3) \times 1 \wedge / 0=I N+2+I P I$ 'ENTRY: '
[13] $P R O M+P R O M, I N$
[14] $\rightarrow$ LO
[15] 'based on current age, enter remaining years of life expectancy from'
[16] 'MORTALITY TABLES'
[17] $k L E+I N P 1$
[18] 'enter basic uninsurred maintenance medical costs as percent of income'
[19] 'AT TIME OF INJURY'
[20] MMC+(INP 1) $\div 100$
[21] MAJMED 20 po
[22] 'ENTER Estimated age at incurrence of future mador medical costs and'
[23] 'ENTER DOLLAR ANNUAL AMOUNTS OF COSTS VALUED in PRESENT DOLLARS'
[24] 'WHEN aLl major medical cost occurences are entered just hit return'
[25] ' $A G E$ DOLLARS '
[26] $L 1:+(L 1+3) \times_{1} \wedge / 0=I N+2 \uparrow I P I$ entry:'
[27] MAJMED 4 MAJMED.IN
[28] $\rightarrow$ L1
[29] MEDINC+ $3000 \leqslant T+A G E[1]$
[30] 'FOR AGE INDICATED SINCE INJURY ENTER ANNUAL LOST INCOME, UNINSURED'
[31] 'MEDICAL COSTS in dollar values and interest rates in percent.'
[32] LOST INCOME UNINSMED COSTS INTEREST RATE •
[33] L2:MEDINC+MEDINC,3+IPI 'AGE: ', ('0123456789'[1+10 10 TT]),'
[34] $\rightarrow L 2 \times 1 A G E[2] \geq T+T+1$
[35] 'ENTER PERCENTAGE DEGREE OF DISABILITY' 人 DIS+(100-INP 1) $\div 100$
[36] ELOSS+(N+66-AGE[2]) 1
[37] ELOSS[YRS]↔ELOSS[YRS\&PROM[1;]-AGE[2]-1]-PROM[2;]:100
[38] ELOSS $+E L O S S+(R A T E-P R O D)$
[39] EINC+INC $\mathrm{x}+/ E L O S S+\mathrm{x} \backslash \div E L O S S$
[40] RET 4 EINC×RET
[41] EMMC+(MMC×INC) $\times+1 \div(1+R A T E-P R O D) * 0,1 R L E$
[42] EMEDINC $\leftarrow(\operatorname{MEDINC}[1 ;]+\operatorname{MEDINC}[2 ;])+. \times \phi \times \backslash \div 1-\operatorname{MEDINC}[3 ;] \div 100$
[43] EMLOSS $\operatorname{MAJMED[2;]+.x\div (1+RATE-PROD)*MAJMED[1;]-AGE[2]~}$
[44] TOTAL $+E I N C+R E T+E M M C+E M L O S S$
[45] AWMRD + EMEDINC + TOTAL×DIS
[46] 'THE DISCOUNT RATES ARE:'
[47] , ;ELOSS
[48] 'THE DISCOUNTED VALUE OF FUTURE INCOME IS:';EINC
[49] 'THE DISCOUNTED VALUE OF THE RETIREMENT ANNUITY IS:';RET
[50] 'THE DISCOUNTED VALUE of EXPECTEd maintenance medical costs is:'; emme
[51] ' THE VALUE of LOST INCOME AND MEDICAL COSTS SINCE INJURY PLUS INTEREST IS :':EMEDINC
[52] 'THE DISCOUNTED VALUE OF FUTURE MAJOR MEDICAL EXPENSES IS:';EMLOSS
[53] 'THE AWARD IS:'; AWARD
$\nabla$

# LINEAR PROGRAMMING WITH MIXED CONSTRAINTS 

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DESCRIPTION

Linear programming is a mathematical technique for finding the best use of a firm's limited resources. The adjective "linear" is used to describe a relationship between two or more variables, a relationship which is directly and precisely proportional. For example, linear means that a 10 percent change in the number of productive hours used in some operation will cause a 10 percent change in output. "Programming" refers to the use of certain mathematical techniques to get the best solution to a problem involving limited resources.

The APL function which initiates these linear programming calculations is entitled SIMPLEX (after the name of the technique which is employed). A complete list of all of the functions which are required for successful operation are given.

| Function Name | Description <br> SIMPLEX |
| :--- | :--- |
| This function accepts and validates |  |
| User input. |  |


| Function Name | Description |
| :---: | :---: |
| SOLI | This function solves the matrix by the Barnes M Method. |
| PRINT | This function provides the printed output as well as the format features. |
| REASON | This function contains author information. |
| DECSLP | This function gives a brief verbal description of linear programming (similar to what is contained in this section) |
| SAMLP | This function contains a sample problem, as well as explanations and examples of data input. |
| These function rompts for the ed usage here nal and the fun request the da need not have mming in order | rehensive built-in instructions <br> so there is no need to explain their merely needs to type SIMPLEX at the rough a series of interactive questi to execute the program. Thus the experience with either APL or linear is series of functions. |

## PROGRAM USAGE

SIMPLEX
tukn carriage to position paper at start of new page, then press feturn.
lineak progkamming - MIXéd constifaints
dO YOU KNOW HOW TO USE THIS PKOGRAM? YES
enter a pkodect title if you wish. documentation run

IS THIS A MAXIMIZATION OF MINIMIZATION PROBLEM? REPLY MAXX OK MIN. MIN enter the number of constiaints, and the number of vaflables: 43

ENTER COEFFICIENTS OF SIMPLEX FFOBLEM, ONE FOW AT A TIME: $111=1000$ ENTEK NEXT CONSThAINT: $100 \leq 300$ ENTER NEXT CONSTRAINT: $010 \leq 150$ ENTER NEXT CONSTRAINT: $001 \geq 200$

ENTER PROEIT OK COST function COEFEICIENTS: 567
tukn cakriage to position paper at staft of new page, then pkess return.
lineak programming with mixed constkaints - minimization

DOCUMENTATION FUN

TABLEAU 1

| VAR | 2 | $\chi 1$ | $\chi 2$ | $\chi 3$ | $\chi 4$ | X 5 | $\chi 6$ | $\chi 7$ | X8 | X9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 4 | 1000.00 | 1.00 | 1.00 | 1.00 | 1.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| 5 | 300.00 | 1.00 | 0.00 | 0.00 | 0.00 | 1.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| 7 | 150.00 | 0.00 | 1.00 | 0.00 | 0.00 | 0.00 | 1.00 | 1.00 | -0.00 | 0.00 |
| 9 | 200.00 | 0.00 | 0.00 | 1.00 | 0.00 | 0.00 | 0.00 | 0.00 | -1.00 | 1.00 |
| 0 | 135000000.00 | 100000.00 | 200000.00 | 200000.00 | 100000.00 | $0.00^{-}$ | 0.00 | $100000.00^{-}$ | 00.00 | 100000.00 |

TABLEAU 2

| VAK | $850^{2}$ | ${ }^{11}{ }^{1}$ | ${ }_{0} \times 2$ | ${ }^{13}$ | ${ }^{1} 4$ | ${ }^{\chi 5}$ | ${ }^{X 6}$ | $x 7$ | ${ }^{18} 8$ | $x 9$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 850.00 | 1.00 | 0.00 | 1.00 | 1.00 | 0.00 | 1.00 | 1.00 | 0.00 | 0.00 |
| 5 | 300.00 | 1.00 | 0.00 | 0.00 | 0.00 | 1.00 | -0.00 | 0.00 | 0.00 | 0.00 |
| 2 | 150.00 | 0.00 | 1.00 | 0.00 | 0.00 | 0.00 | 1.00 | 1.00 | -0.00 | 0.00 |
| 9 | 200.00 | 0.00 | 0.00 | 1.00 | 0.00 | 0.00 | 0.00 | 0.00 | -1.00 | 1.00 |
| 0 | 105000900.00 | 100000.00 | 6.00 | 200000.00 | 100000.00 | 0.00 | 99994.00 | 4.00 | 00.00 | 100000.00 |


| $\begin{array}{r} V A K \\ 4 \\ 5 \\ 2 \\ 3 \\ 0 \end{array}$ | Z | X1 | $X 2$ | $\chi 3$ | $X 4$ | X 5 | X6 | - 87 | X8 | X9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 650.00 | 1.00 | 0.00 | 0.00 | 1.00 | 0.00 | 1.00 | -1.00 | 1.00 | 1.00 |
|  | 300.00 | 1.00 | 0.00 | 0.00 | 0.00 | 1.00 | -0.00 | 0.00 | 0.00 | 0.00 |
|  | 150.00 | , 0.00 | 1.00 | 0.00 | 0.00 | 0.00 | -1.00 | 1.00 | -0.00 | 0.00 |
|  | 200.00 | 0.00 | 0.00 | 1.00 | 10000.00 | 0.00 | 0.00 | 0.00 | -1.00 | 1.00 |
|  | 65002300.00 | 100000.00 | 6.00 | 7.00 | 100000.00 | 0.00 | 99994.00 | 99994.00 | 99993.00 | 99993.00 |
| TABLEAU 4 |  |  |  |  |  |  |  |  |  |  |
| $V A R$41230 | 2 | $X 1$ | $\chi 2$ | X3 | $X 4$ | - X5 | $X 6$ | - $\times 7$ | X8 | - X 9 |
|  | 350.00 | 0.00 | 0.00 | 0.00 | 1.00 | -1.00 |  | -1.00 | 1.00 | $-1.00$ |
|  | 300.00 | 1.00 | 0.00 | 0.00 | 0.00 | 1.00 | -0.00 | 0.00 | 0.00 | 0.00 |
|  | 150.00 | 0.00 | 1.00 | 0.00 | 0.00 | 0.00 | -1.00 | 1.00 | -0.00 | 0.00 |
|  | 200.00 | 0.00 | 0.00 | 1.00 | 0.00 | 0.00 | 0.00 | 0.00 | -1.00 | 1.00 |
|  | 35003800.00 | 5.00 | 6.00 | 7.00 | 100000.00 | 99995.00 | 99994.00 | 99994.00 | 99993.00 | 99993.00 |
| TABLEAU 5 |  |  |  |  |  |  |  |  |  |  |
| $\checkmark A R$ |  |  |  |  | X4 |  | ${ }^{16}$ |  | ${ }^{\chi 8}$ |  |
| 6 | 350.00 | 0.00 | 0.00 | 0.00 | 1.00 | -1.00 | 1.00 | $-1.00$ | 1.00 | -1.00 |
| 1 | 300.00 | 1.00 | 0.00 | 0.00 | 0.00 | -1.00 | 0.00 | 0.00 | 0.00 | -0.00 |
|  |  |  | $1 . 亡$ | u. | 1.0 | 1.6u | $\bigcirc . C C$ | 0.00 | -1.00 | 1.00 |
| 3 | 200.00 | 0.00 | 0.00 | 1.00 | 0.00 | -0.00 | 0.00 | 0.00 0.00 | -1.00 | 1.00 1.00 |
| 0 | 5900.00 | 5.00 | 6.00 | 7.00 | 6.00 | 1.00 | 0.00 | 0.00 | 1.00 | 1.00 |

OPTIMAL SOLUTION FOK MINIMIZATION

THE OPTIMUM VALUE OE Z IS 5900.00

| VAF | VALUE |
| :---: | :---: |
|  |  |
| 6 | 350.00 |
| 1 | 300.00 |
| 2 | 500.00 |
| 3 | 200.00 |

LINEAK PROGKAMMING COMPLETED

TUEN CARhIAGE TO POSITION PAPEF at STAKT OF NEW PAGE, THEN PRESS RETUEN.

```
lineak phogramming - mi_Xed CONSThaintS
LO YOU KNOW HOW TO USE THIS PKOGFAM? YES
ENTEF A PROJECT TITLE IF YOU WISH. DOCUMENTATION RUN
IS THIS A MAXIMIZATION OK MINIMIZATION PKOBLEM? REPLY MAX OK MIN. MAX
ENTER THE NUMBEK OF CONSTRAINTS, AND THE NUMBER OF VARIABLES: 2 2
ENTEK COEFFICIENTS OF SIMPLEX PKOBLEM, ONE FOW A'T A TIME: 4 2 \leq60
    ENTER NEXT CONSTRAINT: 2 4 \leq 48
ENTE'K EKOFIT OK COST FUNCTION COEFFICIENTS: }8
TUFN CAREIAGE TO POSITION EAPEK AT START OF NEW PAGE, THEN PRESS RETUKN.
linear PkOgRAmmIng with mIXED CONSTRAINTS - maXImIZATION
DOCUNENT'ATION KUN
```

| VAK | Z | $X 1$ | $X 2$ | $X 3$ | $X 4$ |
| ---: | ---: | ---: | ---: | ---: | ---: |
| 3 | 60.00 | 4.00 | 2.00 | 1.00 | 0.00 |
| 4 | 48.00 | 2.00 | 4.00 | 0.00 | 1.00 |
| 0 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |

$V A K$
1
4
0
2
15.00
120.00
120.00
$X 1$
1.00
0.00
8.00


| $X 3$ | $X 4$ |
| ---: | ---: |
| -0.25 | 0.00 |
| -.50 | 1.00 |
| 2.00 | 0.00 |

TABLEAU 3

| $V A R$ | 2 | $X 1$ | $X 2$ | $X 3$ | $X 4$ |
| ---: | ---: | :---: | :---: | :---: | :---: |
| 1 | 12.00 | 1.00 | 0.00 | -0.33 | 0.17 |
| 2 | 6.00 | 0.00 | 1.00 | 0.17 | 0.33 |
| 0 | 132.00 | 8.00 | 6.00 | 1.67 | 0.67 |

OETIMAL SOLUTION FOR MINIMIZATION
THE OFPIMUM VALUE OF 2 IS 132.00
VAF VALUE
$\begin{array}{lr}1 & 12.00 \\ 2 & 6.00\end{array}$

LINEAK EKOGKAMMIVG COMPLETEL

## PROGRAM DESCRIPTION

```
    \nablaREASON
[1]
    ,
[2] 'THE LINEAR PROGFAMMING APPLICATION THAT FOLLOWG HAS BEEN WRITTEN AS ONE
    IN'
[3] 'A SERIES OF PROGFAMS RESULTANT FROM:'
[4] '
[5] ' INTERACTIVE COMPUTING FOR MANAGEMENT EDUCATORS*
[6] ' JUNE 29 TO JULY 11. 1975'
[7] , GRADUATE SCHOOL OF MANAGEMENT'
[8] ' UNIVERSITY OF CALIFORNIA AT LOS ANGELES (UCLA)'
[9]
    !
[10] "THIS PROGKAM WAS AUTHORED BY:"
[11] ' '
[12] ' RONALD D.MILLER'
[13] , ASSISTANT DEAN OF SYSTEMS'
[14] ' COLLEGE OF BUSINESS AND PUBLIC SERVICE'
[15] ' GOVERNORS STATE UNIVERSITY'
[16] ' PARKFOREST SOUTH, ILLINOIS 60466'
[17]
    ,
    \nabla
PA: PLEASE SIGN OFF BY 1530 FOR A SYSTEM RESTART.
    \nabla DESCLP
[1] , 
[2] 'LINEAR PROGRAMMING IS A MATHEMATICAL TECHNIQUE FOR FINDING THE BEST USE
    [3j] 'OF A FIRM''S LIMITED FESOURCES. THE ADJECTIVE LINEAR IS USED TO'
[4] 'A RELATIONSHIP BETWEEN TWO OR MORE VARIABLES, A RELATIONSHIP WHICH IS'
[5] 'DIRECTLY AND PRECISELY PROPORTIONAL. FOR EXAMPLE, LINEAR MEANS'
[6] 'THAT A 10 PERCENT CHANGE IN THE NUMBEK OF PRODUCTIVE HOURS USED IN SOME'
[7] 'OPERATION WILL CAUSE A 10 PERCENT CHANGE IN OUTPUT. PROGRAMMING'
[8] 'REFERS TO THE USE OE CERTAIN MATHEMATICAL TECHNIQUES TO GET THE *
[9] 'BEST SOLUTION TO A PROBLEM INVOLVING LIMITED RESOURCES.'
[10]
```

$\nabla$ SIMPLEX
[1] คTHIS PROGRAM REQIRES THE FUNCTIONS DESCLP, REASON,
[2] คSAMLP, SEPERATE, AND SIMPLEX1; AND THE PUBLIC FUNCTIONS
[3] คAKI, $A Y N, A N D I P I$.
[4] $P G S \leftarrow A K I$;
TURN CARRIAGE TO POSITION PAPER AT START OF NEW PAGE, THEN PRESS RETURN.'
[5]
[6]
[7]
[8]
[9]
[10]
[111] $ค$
[12] ค
[13] $P G S \leftrightarrow A Y N$ 'DO YOU KNOW HOW TO USE THIS PROGRAM?'
$[14] \rightarrow(1=P G S) / L 1$
[15] REASON仑 DESCLP $\diamond S A M L P$
[16] L1:TITLE $A K I$ '
ENTER A PROJECT TITLE IF YOU WISH.'
[17] L111:''
[18] $K E P L Y \leftarrow A K I$,
IS THIS A MAXIMIZATION OR MINIMIZATION PROBLEM? REPLY MAX OR MIN. *
$\left.[19] \rightarrow\left({ }^{\prime} A^{\prime} \neq R E P L Y\right) \wedge\left(I^{\prime} I^{\prime} \mp R E P L Y \nleftarrow 1+R E P L Y \leftarrow{ }^{-} 2+R E P L Y\right)\right) / E R R 1$
[20] L112:''
[21] $V \leftarrow, I P I$.
ENTER THE NUMBER OF CONSTRAINTS, AND THE NUMBER OF VARIABLES:'
$[22] \rightarrow((2=\rho V), 2 \neq \rho V) / L 4, E R R 2$
[23] $L 4: C \leftarrow V[2] \diamond R+V[1]$
[24] $M A T+0 \rho 0 \diamond C 1+C+1 \diamond O P+0 \rho{ }^{\prime \prime}$
[25] ''
[26] L114:'
-
[27] PARM+AKI 'ENTER COEFFICIENTS OF SIMPLEX PROBLEM, ONE ROW AT A TIME:'
$[28] \rightarrow L P 2$
[29] LP:''
[30] PARM $-A K I$, ENTER NEXT CONSTRAINT: *
[31] LP2: SEPARATE PARM
[32] $A L P H \leftarrow, A L P H[1 ; 1]$
$[33] \rightarrow\left(1 \neq\left(A L P H \epsilon^{\prime}=\geq \leq^{\prime}\right)\right) / L P 14$
$[34] \rightarrow(((C+1)=\rho N U M) \wedge(1=\rho A L P H)) / L P 1$
$[35] \rightarrow L P 14+1$
[36] LP14:' SIGN ENTERED IN ERROR,'
[37] PARM AKI ' DATA ENTERED IN ERROR, REENTER LAST CONSTRAINT:'
$[38] \rightarrow L P 2$
[39] LP1:MAT MAT,NUM $\bigcirc O P \leftarrow O P, A L P H$
$[40] \rightarrow(((R \times C 1)>\rho M A T),((R \times C 1)<\rho M A T)) / L P, E R R^{4}$
[41] $\quad C J \leftarrow 0 \rho 0$
[42] $L 6: P A R M \leftarrow A K I$ '
ENTER PROFIT OR COST FUNCTION COEFEICIENTS: '
[43] SEPARATE PARM
[44] $+(C=\rho N U M) / L 160$
[45] 'INVALID ENTRY, PLEASE REENTER' ↔ $+L 6$
[46] L160:CJ CJ, NUM
$[47]+((C>\rho C J),(C<\rho C J)) / L 6, E R R 5$
[48] CODE*'123456789012345678901234567890"
[49] SIMPLEX1
[50] 'LINEAR PROGRAMMING COMPLETED'
$[51] \rightarrow 0$
[52] ERR1:'IHE REPLY MUST BE MAX OR MIN. PLEASE REENTER:' © $+L 111$
[53] ERR2: 'YOU SHOULD HAVE ENTERED TWO INTEGERS. PLEASE REENTER:' © $\rightarrow L 112$
[54] ERR4: 'YOU HAVE ENTER AN INCORRECT NUMBER OF COEFFICIENTS OR YOU HAVE FORGOTTEN TO ENTER THE ARITHMETIC OPERATOR(S). PLEASE REENTER.* 人 $+L 114$
[55] ERR5: YOU SHOULD HAVE ENTERED ONE PROFIT OR COST FUNCTION COEFFICIENT FOR EACH VARIABLE. PLEASE REENTER.' © $\rightarrow L 6$
[56] UNBD: '
THE OBJECTIVE FUNCTION IS NOT BOUNDED ABOVE X $=$ ' $\operatorname{COL} ;{ }^{\prime \prime}$
$\nabla$

[38] ' REPLY: YOU MUST ENTER THE NUMBER OF CONSTRAINTS THAT THE PROBLEM CONTAI NS. YOU WILL ALSO NEED TO'
[39] ' ENTER THE NUMBER OF VARIABLES (SUCH AS X Y Z). YOU MUST ENTER T WO INTEGERS WITH A SPACE BETWEEN'
[40] 1 EX.: 43
[41] ' PROMPT: ENTER COEFFICIENTS OF SIMPLEX PROBLEM, ONE ROW AT A TIME:'
[42] ' OR: ENTER NEXT CONSTRAINT:'
[43] ' REPLY: ENTER ONE ROW OF THE CONSTRAINTS AT A TIME, MAKING SURE THAT YOU ENTER THE VALUES AND THE'
[44] ' ARITHMETIC OPERATOR IN THE REFORMAT EXAMPLE GIVEN ABOVE. ONLY ( $=\geq \leq$ ) ARE VALID OPERATORS.'
[45] ' EX.: $111=1000$ (FIRST CONSTRAINT ENTRY)
[46] ' PROMPT: ENTER PROFIT OR COST FUNCTION COEFFICIENTS.'
[47] ' REPLY: ENTER THE PROFIT OR COST VALUES OF THE OBJECTIVE FUNCTION.'
[48] ' EX.: 567
[49] '
[50] 'PLEASE RETAIN THIS PRINTOUT FOR FUTURE REFERENCE.'
[51] '
$\nabla$

```
    \nabla SIMPLEX1
[1]
[2]
    turn carriage to position paper at start of new page, then press return.'
[3] PGS+\square
[4] M1+1+(REPLY='A')
[5] ->(M1=1)/L7
[6]
    LINEAR PROGRAMMING WITH MIXED CONSTRAINTS - maXIMIZATION
        ,
[7] OPTI*'OPTIMAL SOLUTION FOR MAXIMIZATION.
[8] }->\mathrm{ L7+1
[9] L7:'
    linear programming with mixed constraints - minimization
    ,
[10] OPTI+'OPTIMAL SOLUTION FOR MINIMIZATION'
[11] TITLE:'
    ,
[12] MHIGH*-
[13] MAT+MAT,0 仓 RC1+R,C1 & CNTR+0 & MAT+RC1OMAT
[14] 2EROS+R,(+/OPG'\geq')+\rhoOP\diamond MAT MAT,ZEROS\rhoO
[15] FC1+pMAT\diamond C1+1+RC1 \diamond C+C+1
[16] MAT[;C1]+MAT[;C]\diamond MAT[;C]+R\rho0
[17] PC+C\bigcircPR+1
[18] VIB+R\rho0 ○ ZJ+C1\rho0 < I I 1 O CJ+CJ, (C1-C)\rho0
[19] L13:+(OP[I]*'\geq')/L8\diamond МAT[PR;PC]+`1 & MAT[PR;PC+1]+1
[20] VIB[PF]+PC+1 < ->(2=M1)/L9
[21] CJ[PC+1]+PHIGHO O L9+1
[22] L9:CJ[PC+1]+MHIGH
[23] PC+PC+2 0 
[24] L8:MAT[PR;PC]+1 \diamond VIB[PR]+PC
[25] 
[26] CJ[PC]+MHIGH\diamond +L11+1
[27] L11:CJ[PC]<PHIGH
[28] PC+PC+1
[29] L10:PR<PR+1 < ->(R\geqI+I+1)/L13 人 C&C1-1
[30] VPT+VIB[1R]\diamond CJC+CJ[VPT]\diamondPRINT
[31] L12:+(M1=2)/L16
[32] }->((v/(CZ<0))\not=0)/L111
[33] SOLI
[34] ->0
[35] L117:COL+,CZ:(L/CZ) \diamond + L17
[36] L16:+((v/(CZ>0))\not=0)/L118
[37] SOLI
[38] ->0
[39] L118:COL\leftarrow,CZ:(Г/CZ)
[40j L17:+((+/(,MAT[;COL]>0))=0)/UNBD
[41] ANDED\leftarrow(ANDED>0)/\imath\rhoANDED\leftarrow,ANDED\leftarrow(MAT[;COL]>0)^(MAT[;C1]>0)
[42] REMAIN+,MAT[ANDED;C1]\divMAT[ANDED;COL]
[43] ROW+,REMAIN:(L/REMAIN) \diamondROW+ANDED[ROW]\diamondVIB[ROW]+COL \diamond CJC[ROW]+CJ[COL]
[44] MAT[ROW:]+MAT[ROW;]*MAT[ROW;COL] O I+1
[45] L18:PIV +MAT[I;COL] 
[46] MAT[I;]+MAT[I;]-.(PIV MMAT[ROW;])
[47] L19:+( F\geqI+I+1)/L18
[48] PRINT
[49] +L12
[50] UNBD:'
    the objective function is not bounded AbOVE X = ';COL;'
    \nabla
```

```
    \nabla PRINT
[1] aTHIS funCTION USES THE FOLLOWING SCIENTIFIC
[2] ATIME SHARING FUNCTIONS: CENTER, \triangleFNT, AND COLNAMES
[3] 2J+CJC+.\timesMAT
[4] CZ+CJ-ZJ[2C1-1]
    ,
[6] CNTR+CNTR+1
[7] FORM&TABLEAU ',CODE[CNTR]
[8] COLNM+'/X1 /X2 /X3 /X4 /X5 /X6 /X7 /X8 /X9 /X10/X11/X12/X13/X14/X15/X16/X
    17/X18'
[9] COLNM+'/VAR/Z ,,((C1-1)\times4)+COLNM
[10] ESTR+'I4,X1,F14.2,10F10.2'
[11] FSTR CENTER EORM
[12] ,
[13] FSTR COLNAMES COLNM
[14] ESTR \triangleFMT(VIB;MAT[;C1];MAT[1R;1C1-1])
[15] CC*1,C1-1
[16] CC+CCPl(C1-1)
[17] FSTR \triangleEMT(0;ZJ[C1];ZJ[CC])
```

THE INTERACTIVE EFFECTS OF THE MARGINAL PROPENSITY TO CONSUME AND THE INVESTMENT ACCELERATOR ON THE PRODUCTION OF INCOME<br>John Park<br>Chairman, Department of Economics and Business Administration Frostburg State College Frostburg, Maryland

## DESCRIPTION

This is a short, simple problem designed for use by undergraduate economic and business forecasting students to get them acquainted with an APL application in economics. The program attempts to generate a trend of national income (Gross National Product or "GNP"), based upon a set of assumptions. These assumptions are described in the program. Different combinations of assumptions would, of course, produce different income trends.

The object of the program is to attack a problem which is too tedious for hand calculation and solution. The project may be assigned to students as a homework assignment or for drill and practice. Outputs are printed out in a tabular form and, as an option, the trend of income (the last column in the table) can be plotted out on a chart.

To use the program, the student types ACTION and, when asked, enters the following values.

1. The autonomous investment (constant throughout the exercise)
2. The marginal propensity to consume (MPC)
3. The investment accelerator (alpha)
4. The number of periods the program is to run.

As an additional exercise, the instructor may wish to designate to students a particular shape (perhaps fluctuating) of income trends of the past and/or present as a starting point, and then ask them to suggest a particular combination of numerical figures for marginal propensity to consume and alpha which would bring the given initial trend of income to some planned or desired level.

## PROGRAM USAGE

```
        ACTION
DO YOU NEED INSTRUCTIONS?
YES
    HI ECONOMIST: I SEE THAT YOU ARE TRYING TO FOFECAST THE NATIONAL
INCOME TREND. WITH THE HELP OF APL, AND YOU MAY SUCCEED IN DOING SO
IN A JIFEY. LET US ASSUME THE FOLLOWING CONDITIONS:
1. AUTONOMOUS INVESTMENT (A) IS CONSTANT THOUGHOUT THE GIVEN PERIODS
    WE OBSEFVE.
2. INDUCED CONSUMPTION (C) OF A PERIOD IS THE NATIONAL INCOME OF THE
    PKEVIOUS PERIOD ADJUSTED BY YOUR MARGINAL PROPENSITY TO CONSUME (MPC).
3. INDUCED INVESTMENT (I) OF A PERIOD IS THE ABSOLUTE VALUE OE THE
    DIFEEFENCE BETWEN THE C OF THE PERIOD AND THE C OF THE IMMEDIATELY
    PRECEDING PERIOD, ADJUSTED BY YOUR ALPHA (I.E., MULTIPLIED BY THE
    GIVEN ALPHA).
4. TOTAL NATIONAL INCOME (Y) OF A FEFIOD IS THE SUMMATION OF A, C, AND I
    EOF THAT PERIOD.
5. THE TOTAL NUMBEF OF MULTIPLIER PERIODS (T'S) WE OBSERVE IS, SAY 20(I.E.,
    20 T'S).
ENTER AUTONOMOUS INVESTMENT (A)
\square:
    1000
ENTER MAFGINAL PROPENSITY TO CONSUME (MPC)
\square:
    .75
ENTEK ALPHA (.ACCELERATOK)
\square:
    2.7
ENTER NUMBER OF PEKIODS
[]:
    20
```

| MULTIPLIER PERTOD | AUTONOMOUS <br> INVESTMENT | INDUCED <br> CONSUMPTION | INDUCED <br> INVESTMENT | TOTAL NATIONAL INCOME |
| :---: | :---: | :---: | :---: | :---: |
| (T) | ( $A$ ) | (C) | ( $I$ ) | ( $Y$ ) |
| 1 | 1000 | 0 | 0 | 1,000 |
| 2 | 1000 | 750 | 2,025 | 3,775 |
| 3 | 1000 | 2,831 | 5,619 | 9,451 |
| 4 | 1000 | 7,088 | 11,493 | 19,581 |
| 5 | 1000 | 14,586 | 20,514 | 36,200 |
| 6 | 1000 | 27,150 | 33,653 | 61,803 |
| 7 | 1000 | 46,353 | 51,847 | 99,199 |
| 8 | 1000 | 74,400 | 75,727 | 151,128 |
| 9 | 1000 | 113,345 | 105,152 | 219,497 |
| 10 | 1000 | 164,623 | 138,450 | 304,073 |
| 11 | 1000 | 228,055 | 171,267 | 400, 321 |
| 12 | 1000 | 300,241 | 194,903 | 496,144 |
| 13 | 1000 | 372,108 | 194,041 | 567,149 |
| 14 | 1000 | 425,361 | 143,785 | 570,146 |
| 15 | 1000 | 427,609 | 6,070 | 434,679 |
| 16 | 1000 | 326,009 | 274,320 | 601,330 |
| 17 | 1000 | 450,997 | 337,467 | 789,464 |
| 18 | 1000 | 592,098 | 380,973 | 974,071 |
| 19 | 1000 | 730,553 | 373,828 | 1,105,381 |
| 20 | 1000 | 829,036 | 265,904 | 1,095,940 |

[^2]

## PROGRAM DESCRIPTION

```
\nabla DESCRIBEACTION
    'HI ECONOMIST: I SEE THAT YOU ARE TRYING TO FORECAST THE NATIONAL'
    'INCOME TREND. WITH THE HELP OF APL, AND YOU MAY SUCCEED IN DOING SO'
    'IN A JIFFY. LET US ASISUME THE EOLLOWING CONDITIONS:'
    1. AUTONOMOUS INVESTMENT (A) IS CONSTANT THOUGHOUT THE GIVEN PEKIODS'
    ' WE OBSERVE.'
    '"
    '2. INDUCED CONSUMPTION (C) OF A PEKIOD IS THE NATIONAL INCOME OF THE'
    C).'
[10] ',
[11] '3. TNDUCED INVESTMENT (I) OF A PERTOD IS THE ABSOLUTE VALUE OF THE'
[12] , DIEFERENCE BETWEN THE C OF THE PERIOD AND THE C OF THE IMMEDIATELY,
[13] , PRECEDING PERIOD, ADJUSTED BY YOUR ALPHA (I.E., MULTIPLIED BY THE'
[14] , GIVEN ALPHA).
[15] "'
[16] '4. TOTAL NATIONAL INCOME (Y) OF A PEFIOD IS THE SUMMATION OF A, C, AND
    I'
[17] , FOR THAT PERIOD.'
[18] ., FOR THAT PERIOD.
[18] *
[19] '5. THE TOTAL NUMBER OF MULTIPLIER PERIODS (T''S) WE OBSERVE IS, SAY 20
        (I.E..'
[20] ' 20 T''S).'
[21] ..
\nabla
```

```
    \nabla ACTION;A;ALPHA;C;CTR;EMT;I;MPC;N;T;Y
[1] aTHIS fuNCTION KEQUIRES THE FUNCTION DESCRIBEACTION, WHICH DESCRIBES
[2] atHE ASSUMPTIONS OF thE mODEL, AND thE PUBLIC EUNCTIONS COLNAMES.
[3] A \triangleFMT AND PLOT
[4] 'DO YOU NEED INSTRUCTIONS ?'
[5] ->L1\times71'N8'=14`
[6] DESCRIBEACTION
[7] L1:'ENTEF AUTONOMOUS INVESTMENT (A)'
[8] Y+,A+\square
[9] I+C+0
[10] 'ENTER MARGINAL PROPENSITY TO CONSUME (MPC)'
[11] MPC*D
[12] 'ENTER ALPHA (ACCELEKATOR)'
[13] ALPHA+\square
[14] 'ENTER NUMBER OF PERIODS'
[15] N<D
[16] CTR+2
[17] LOOP:C&C,MPC\timesY[CTR-1]
[18] I+I,ALPHA\times| C[CTR]-C[CTR-1]
[19] Y+Y,A+C[CTR]+I[CTR]
[20] CTR+CTR+1
[21] }->\mathrm{ LOOP×1 (CTR\N)
[22] }A+N\rho
[23] T+1N
[24] ''
[25] ,'
[26] FMT+'2I12,3CI17'
[27] FMT COLNAMES '/MULTIPLIER/AUTONOMOUS/INDUCED /INDUCED /TOTAL NATIONA
        L'
[28] FMT COLNAMES '/PERIOD /INVESTMENT/CONSUMPTION/INVESTMENT/INCOME
[29] ''
[30] FMT COLNAMES :/(T)/(A)/(C)/(I)/(Y)'
[31] '.
[32] EMT \triangleFMT(T;A;C; I;Y)
[33] ,'
[34] ''
[35] 'WOULD you likE a pLOT OF the abOVE DATA?'
[36] ->0\times1'N'=1+[]
[37] 60 80 PLOT Y
[38] ''
[39] '
    \nabla
```

NETWORK ANALYSIS
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## DESCRIPTION

This program is used to analyze Critical Path Method (CPM) and Program Evaluation and Review Technique (PERT) networks. Such networks are useful in planning, scheduling, and control of complex projects (such as research, development, and construction).

The program can be used to solve problems which would be too time consuming for hand calculation or to verify the results of manual calculations.

It was developed to be used in a junior year course in quantitative methods in business or by beginning graduate students in a prerequisite course in quantitative methods for an MBA program.

## Instructions for Use

Input instructions are contained within the program and are printed out to the user as needed.

It is assumed that the user has a basic understanding of network theory as presented in a basic text such as Quantitative Approaches to Management by Levin and Kirkpatrick.

The user desiring a description of the workspace should execute the niladic function NETINFO. The user then has the option of analyzing a network after having read the workspace description. Those not desiring a description should execute the niladic function NET1 directly in order to initiate a network
analysis. The input variables are:
PERT Networks CPM Networks
Beginning Event Beginning Event
Ending Event Ending Event
Optimistic Time Expected Time
Most Likely Time Latest Allowable Date
Latest Allowable Date
Completion Dates for
Probability Analysis
Outputs from the program include:
(1) List of input data
(2) Number of activities input
(3) Events listed in numerical order
(4) Starting and finish events listed
(5) Critical path
(6) Expected completion date
(7) Slack
(8) Z values for probability analysis (optional) -(PERT only)
(9) Complete event analysis (optional)

For each event:
Event numbers
Expected completion date
Latest date
Slack
Critical path indicator
(10) Complete activity analysis (optional)

For each activity:
To-From events
Expected time
Expected start date
Expected completion date
Latest start date
Latest completion date
Standard deviation (PERT only)
Critical path indicator

## Sample Use

In the next section the following uses are demonstrated:
(1) PERT Network
(2) CPM Network
(3) Error checking and recovery


Figure 1
The network shown in Figure 1 is used for these demonstrations. These data were used to illustrate that the critical path can change as the result of consideration of pessimistic or optimistic times, as is true with PERT analysis, while CPM considers only one time estimate.

## PROGRAM USAGE

NETINEO

## WOKKSFACE NETWORK

THIS WOKKSPACE CONTAINS THREE GUNCTIONS WHICH OPERATE TOGETHEK TO SOLVE FKOBLEMS IN NETWOKK ANALYSIS. IT IS ASSUMELC THAT THE USER IS FAMILIAR WITH NETWOFK THEORY.

THE USEK MAY SPECIFY CPM OR PEKT ANALYSIS. PROVISION IS MADE FOF THE USER TO SELECT ABBFEVIATED OR COMPLETE OUTPUT EESULTS.

FEATURES INCLUDE:
(1) SELF-CONTAINED INPUT INSTRUCTIONS
(2) EXIUNSIVE ERKOR CHECKING AND FECOVERY
(3) CAPABILITY OF CORRECTING DATA IN NETWOKK AFTEK IT HAS BEEN INPUT
(4) OPTIONAL COMPITATION OF 'Z' VALUES FOK PROBABILITY ANALYSIS WITH PERT NETWORKS

THE FUNCTIONS IN THIS WORKSPACE ARE DESCRIBED BELOW:
NETINFO - CONTAINS A DESCRIPTION OF THE FUNCTIONS. THE USEF HAS THE OPTION OF EXECUTING THE ANALYSIS OF A PEKT OR CPM NETWORK FKOM THIS FUNCTION BY CALLING EUNCTION NETI.

NET1 - HANDLES INPUT OF NETWORK DATA TO BE ANALYZED, ERKOF CHECKING, RECOVERY, AND NETWOKK ANALYSIS. CALLS FUNCTION NET2 FOR OUTPUT.

NET 2 - PFODUCES OUTPUT OF THE PEKT OR CPM NETWORK ANALYSIS. THE USER MAY SPECIFY SHOKT OR LONG OUTPUT FOKMAT.

DO YOU WANT TO INPUT A NETWORK TO BE ANALYZED? ANSWER YES OR NO.
YES
ENTER CPM OF PERT TO SPECIFY TYPE OF NETWORK TO BE ANALYZED
PERT

```
    NET1
ENTER CPM OR PERT TO SPECIFY TYPE OF NETWOKK TO BE ANALYZED
XYZ
ENTER CPM OR PERT TO SPECIFY TYPE OF NETWORK TO BE ANALYZED
PERT
ENTER PERT ACTIVITY DATA IN GROUPS OF FIVE: BEGINNING EVENT, ENDING
EVENT, OPTIMISTIC TIME, MOST LIKELY TIME, PESSIMISTIC TIME.
BEGINNING EVENT MUST BE A HIGHEF NUMBEK THAN ENDING EVENT FOR EACH ACTIVITY.
ENTEF 1 TO INDICATE THAT YOU HAVE NO MORE DATA.
\square:
1 2 6 7 8
2 3 8 9
INPUT MUST BE 5 ITEMS.
\square:
    2 3 8 9 10
]:
[. 34456
3 3 5 7 8 9
L: -
INPUT DATA
\begin{tabular}{llllr}
1 & 2 & 6 & 7 & 8 \\
2 & 3 & 8 & 9 & 10 \\
3 & 4 & 4 & 5 & 6 \\
3 & 5 & 7 & 8 & 9
\end{tabular}
DO YOU WISH TO CHANGE ANY DATA? ANSWER YES OR NO.
YES
ENTEK FOW NUMBER, COLUMN NUMBER, AND NEW VALUE.
\square:
    1
INPUT MUST BE 3 ITEMS.
ENTER ROW NUMBER, COLUMN NUMBER, AND NEW VALUE.
\square:
    10 10 8
ENTER ROW NUMBER, COLUMN NUMBER, AND NEW VALUE.
\square:
    1510
FEVISED DATA:
\begin{tabular}{rllll}
1 & 2 & 6 & 7 & 10 \\
2 & 3 & 8 & 9 & 10 \\
3 & 4 & 4 & 5 & 6 \\
3 & 5 & 7 & 8 & 9
\end{tabular}
DO YOU WISH TO CHANGE ANY DATA? ANSWER YES OR NO.
NO
```


## PROGRAM DESCRIPTION

```
\nabla NETINFO
```

```
[1] & THIS FUNCTION PROVIDES THE USER WITH A DESCRIPTION OF IHE CONTENTS OF
```

[1] \& THIS FUNCTION PROVIDES THE USER WITH A DESCRIPTION OF IHE CONTENTS OF
[2] ค THE WORKSPACE. THE USER MAY CALL THE FUNCTION WHICH PERFORMS THE
[2] ค THE WORKSPACE. THE USER MAY CALL THE FUNCTION WHICH PERFORMS THE
[3] ค NETWORK ANALYSIS AFTER READING THE DESCRIPTION OF THE WORKSPACE BY
[3] ค NETWORK ANALYSIS AFTER READING THE DESCRIPTION OF THE WORKSPACE BY
[4] A GIVING AN AFFIRMATIVE RESPONSE TO THE QUESTION. 'DO YOU WANT TO INPUT
[4] A GIVING AN AFFIRMATIVE RESPONSE TO THE QUESTION. 'DO YOU WANT TO INPUT
[5] A A NETWORK TO BE ANALYZED?'
[5] A A NETWORK TO BE ANALYZED?'
[6] *
[6] *
[7] , ,
[7] , ,
[8] , '
[8] , '
[9] , ,
[9] , ,
[10] ' WORKSPACE NETWORK'
[10] ' WORKSPACE NETWORK'
[11] ' '
[11] ' '
[12] , ,
[12] , ,
[13] 'THIS WORKSPACE CONTAINS THREE FUNCTIONS WHICH OPERATE'
[13] 'THIS WORKSPACE CONTAINS THREE FUNCTIONS WHICH OPERATE'
[14] TOGETHER TO SOLVE PROBLEMS IN NETWORK ANALYSIS. IT IS '
[14] TOGETHER TO SOLVE PROBLEMS IN NETWORK ANALYSIS. IT IS '
[15] 'ASSUMED THAT THE USER IS FAMILIAR WITH NETWORK THEORY.'
[15] 'ASSUMED THAT THE USER IS FAMILIAR WITH NETWORK THEORY.'
[16] ' '
[16] ' '
[17] , THE USER MAY SPECIFY CPM OR PERT ANALYSIS. PROVISION'
[17] , THE USER MAY SPECIFY CPM OR PERT ANALYSIS. PROVISION'
[18] 'IS MADE FOR THE USER TO SELECT ABBREVIATED OR COMPLETE'
[18] 'IS MADE FOR THE USER TO SELECT ABBREVIATED OR COMPLETE'
[19] 'OUTPUT RESULTS.'
[19] 'OUTPUT RESULTS.'
[20] '.
[20] '.
[21] , FEATURES INCLUDE:'
[21] , FEATURES INCLUDE:'
[22] , (1) SELF-CONTAINED INPUT INSTRUCTIONS'
[22] , (1) SELF-CONTAINED INPUT INSTRUCTIONS'
[23] (2) EXTENSIVE ERROF CHECKING AND RECOVERY'
[23] (2) EXTENSIVE ERROF CHECKING AND RECOVERY'
[24j , (3) CAPABILITY DF CORRECTING DATA IN ,
[24j , (3) CAPABILITY DF CORRECTING DATA IN ,
[25] ' NETWORK AFTER IT HAS BEEN INPUT'
[25] ' NETWORK AFTER IT HAS BEEN INPUT'
[26] (4) OPTIONAL COMPUTATION OF''Z''VALUES'
[26] (4) OPTIONAL COMPUTATION OF''Z''VALUES'
[27] ' FOR PROBABILITY ANALYSIS WITH PERT'
[27] ' FOR PROBABILITY ANALYSIS WITH PERT'
[28] ' NETWORKS'
[28] ' NETWORKS'
[29] ' '
[29] ' '
[30] ,
[30] ,
[31] , THE FUNCTIONS IN THIS WORKSPACE ARE DESCRIBED BELOW:"
[31] , THE FUNCTIONS IN THIS WORKSPACE ARE DESCRIBED BELOW:"
[32] , ,
[32] , ,
[33j, NETINFO - CONTAINS A DESCRIPTION OF THE FUNCTIONS.'
[33j, NETINFO - CONTAINS A DESCRIPTION OF THE FUNCTIONS.'
[34] THE USER HAS THE OPTION OF EXECUTING THE'
[34] THE USER HAS THE OPTION OF EXECUTING THE'
[35] , ANALYSIS OF A PERT OR CPM NETWORK FROM'
[35] , ANALYSIS OF A PERT OR CPM NETWORK FROM'
[36] , THIS FUNCTION BY CALLING FUNCTION NET1..
[36] , THIS FUNCTION BY CALLING FUNCTION NET1..
[37] , ,
[37] , ,
[38] , NET1 - HANDLES INPUT OF NETWORK DATA TO BE ANALYZED,'
[38] , NET1 - HANDLES INPUT OF NETWORK DATA TO BE ANALYZED,'
[39] , ERROR CHECKING, RECOVERY, AND NETWORK ANALYSIS.'
[39] , ERROR CHECKING, RECOVERY, AND NETWORK ANALYSIS.'
[40] , CALLS FUNCTION NET2 FOR OUTPUT.'
[40] , CALLS FUNCTION NET2 FOR OUTPUT.'
[41] . . [40] (4)
[41] . . [40] (4)
[42] , NET2 - PRODUCES OUTPUT OF THE PERT OR CPM NETWORK'
[42] , NET2 - PRODUCES OUTPUT OF THE PERT OR CPM NETWORK'
[43] , ANALYSIS. THE USER MAY SPECIFY SHORT OR'
[43] , ANALYSIS. THE USER MAY SPECIFY SHORT OR'
[44] ' LONG OUTPUT FORMAT.'
[44] ' LONG OUTPUT FORMAT.'
[45] ',
[45] ',
[46] ' '
[46] ' '
[47] , '
[47] , '
[48] QUES5:'DO YOU WANT TO INPUT A NETWORK TO BE ANALYZED? ANSWER YES OR NO.'
[48] QUES5:'DO YOU WANT TO INPUT A NETWORK TO BE ANALYZED? ANSWER YES OR NO.'
[49] ->(GOTO,O,QUES5)['YN',14, D]
[49] ->(GOTO,O,QUES5)['YN',14, D]
[50] M CALL FUNCTION NET1 IF THE USER WISHES TO PERFORM A NETWORK ANALYSIS
[50] M CALL FUNCTION NET1 IF THE USER WISHES TO PERFORM A NETWORK ANALYSIS
[51] GOTO:NET1
[51] GOTO:NET1
\nabla

```
    \nabla
```

$\nabla$ NET1; $A ; A C T ; B ; B 1 ; B 2 ; B 3 ; C ; C P A C ; C P E V ; C R I T ; D ; D A T A 1 ; D 1 ; D 2 ; E ; F L A G S ; F 1 ; F 2 ; G ; H ; J ;$ $K ; L A T E S T ; M ; N ; N A ; N E ; S T D E V ; 2$
[1] A THIS FUNCTION RECEIVES CPM OR PEFT NETWOKK DATA FROM THE USER AND
[2] A ANALYZES THE NETWOFK TO DETERMINE THE EXPECTED TIMES, EXPECTED START
[3] a and COMPLETION dates, LATEST START AND COMPLETION DATES, AND THE
[4] A CFITICAL PATH. IN ADDITION, ACTIVITY STANDAFD DEVIATIONS, NETWORK
[5] A STANDARD DEVIATION, AND 2 VALUES FOR SELECTED COMPLETION DATES ARE
[6] A COMPUTED FOR PEFT NETWORKS ONLY. IT IS ASSUMED THAT THE USER IS
[7] a FAMILIAR WITH NETWOFK THEORY. THE FUNCTION SHOULD BE USED TO ANALYZE
[8] A PROBLEMS WHICH ARE TOO COMPLEX FOR MANUAL CALCULATION or to CHECK the
[9] i RESULTS of manual calculations for classroom use.
[10] a INPUT INSTRUCTIONS ARE CONTAINED WITHIN THE PROGRAM.
[11] START:'ENTER CPM OF PERT TO SPECIFY TYPE OF NETWORK TO BE ANALYZED'
[12] $\rightarrow(C P M, P E R T, S T A F T)\left[' C P^{\prime} 11+, 0\right]$
[13] $C P M: Z+3$
[14] a INPUT DATA INSTRUCTIONS FOR CPM NETWORKS •
[15] 'ENTER CPM ACTIVITY DATA IN GROUPS OF THREE:'
[16] 'beginning event, ending event, expected time.'
[17] $\rightarrow G O 1$
[18] PERT: 2+5
[19] a input data instructions for pert networks
[20] ENTER PERT ACTIVITY DATA IN GROUPS OF FIVE: BEGINNING EVENT, ENDING'
[21] 'EVENT, OPTIMISTIC TIME, MOST LIKELY TIME, PESSIMISTIC TIME.'
[22] GO1:'bEGINNING EVENT MUST BE A HIGHER NUMBEF THAN ENDING EVENT FOR EACH AC TIVITY.'
[23] 'ENTER ${ }^{-1}$ to INDICATE THAT YOU HAVE NO MORE DATA.'
[24] $N A+0$
[25] $A C T+10$
[26] A NETWORK DATA READ IN HEFE
[27] FEADIN: $A+\square$
$[28] \rightarrow(N E X T, N O M O R E D A T A)[1+(1+A)<1]$
[29] a CHECK that the appropriate number of data items is entered (3 for cpm, 5 FOR PERT)
[30] NEXT: $\rightarrow(O K 1, E F R 1)[1+(\rho A) \neq Z]$
[31] A ERROR MESSAGE FOR INCORRECT NUMBER OF DATA ITEMS
[32] ERF1:'INPUT MUST BE ; Z;' ITEMS.'
[33] $\rightarrow$ FEADIN
[34] OK1: $\rightarrow(O K 2, E R R 2)[1+(A[1] \geq A[2])]$
[35] ERF2:'EVENTS MUST BE IN ASCENDING ORDEF.'
[36] $\rightarrow$ READIN
[37] OK2:NA $-N A+1$
[38] $A C T+A C T, A$
[39] $\rightarrow$ FEADIN
[40] NOMOREDATA: ACT+(NA,Z) DACT
[41] ' '
[42] ,
[43] a INPUT DATA IS DISPLAYED TO USER FOR CORRECTNESS
[44] 'INPUT DATA.
[45] 1
[46] $A C T$
[47] AGAIN:' ,
[48] 'DO YOU WISH TO Change ANY DATA? ANSWER YES OR NO.'
[49] $\rightarrow(Y E S, N O, A G A I N)\left[{ }^{\prime} Y N^{\prime}: 1 \uparrow, \mathbb{D}\right]$

```
[50] YES:' '
[51] 'ENTER ROW NUMBER, COLUMN NUMBER, AND NEW VALUE.'
[52] p DATA COKRECTIONS ENTERED HERE
[53] A+\square
[54] & CHECK THAT THREE ITEMS HAVE BEEN ENTERED FOR DATA CORRECTION
[55] A (ROW NO., COL.NO..NEW VALUE)
[56] ->(GOOD1,BAD1)[1+(\rhoA)\not=3]
[57] EAD1:"INPUT MUST BE 3 ITEMS.'
[58] ->YES
[59] GOOD 1:->((A[1]>1+\rhoACT)\vee(A[2]> }\mp@subsup{}{}{-}1+\rhoACT))/YE
[60] & DATA CORRECTIONS MADE HERE
[61] ACT[A[1];A[2]] A A[3]
[62] ,
[63] 'REVISED DATA:'
[64] , '
[65] ACT
[66] & BRANCH BACK TO SEE IF THERE AFE MORE CORRECTIONS TO BE ENTERED
[67] +AGAIN
[68] ค NO (MOFE) CORRECTIONS
[69] NO:NA+1+\rhoACT
[70] ' '
[71] 'ENTER LATEST ALLOWABLE DATE FOR COMPLETION OF PROJECT.'
[72] LATEST }
[73] , '
[74] A NEXT TEN LINES SUMMARIZE THE INPUT DATA
[75] NA;' ACTIVITIES HAVE BEEN ENTERED.'
[76] B1 &ACT[;1],ACT[;2]
[77] B1*B1[4B1]
[78] B2 1+((B1,0)-(0,B1))
[79j B2&(0工B2)/B1
[80] NE ¢ B2
[81] 'INVOLVING ';NE;' DIFFERENT EVENTS, AS FOLLOWS:'
[82] ',
[83j B2
[84] ค CHECK FOR MULTIPLE FINISH EVENTS
[85] D1\leftarrow(- 1+B2)\inACT[;1]
[86] ->((^/D1)=1)/OK3
[87] 'MULTIPLE FINISH EVENTS IN THE NETWORK, USE DUMMY ACTIVITY.'
[88] ค IF MULTIPLE FINISH EVENTS, EXIT PROGRAM
[89] }->
[90] OK3:D1&(1+B2)\inACT[:2]
[91] ^ CHECK FOR MULTIPLE START EVENTS
[92j }->((N/D1)=1)/OK
[93] 'MULTIPLE STARTING EVENTS IN THE NETWORK, USE DUMMY ACTIVITY."
[94] & IF MULTIPLE START EVENTS, EXIT PROGRAM
[95] ->0
[96] OK4:' '
[97] 'THE STARTING EVENT FOR THE NETWORK IS ';1^B2;' AND THE FINISH EVENT IS '
    ; - 1+B2
[98] A SET UP ARRAYS FOR NETWORK ANALYSIS. E FOR EVENTS AND C FOR ACTIVITIES.
[99] E+(NE,5)\rho0
[100] C+(NA.7)p0
[101j] (Z=3)/OK5
[102]ACALCULATE EXPECTED TIMES AND SD'S EOR PERT NETWORKS
```

```
[103] C[;1]+(ACT[;3]+(4\timesACT[;4])+ACT[;5])\div6
[104] C[;6]+(ACT[;5]-ACT[;3])\div6
[105] ->GO2
[106]OK5:C[;1]+ACT[;3]
[107]a PUT EVENT NUMBERS IN MATRIX E
[108]GO2:E[;1] & B2
[109] E[1;2]+0
[110] E[1;5j+1
[111]^ N IS ACTIVITY INDEX
[112]GOO2:N+1
[113]aREFERENCE NUMBER IN E FOR BEGINNING EVENT OF ACTIVITY
[114]GO3:F1+B2,ACT[N;1]
[115] }->(~(E[F1;5]=1)^(C[N;7]=0))/GO
[116] C[N;2]+E[F1;2]
[117] C[N;3]+C[N;2]+C[N;1]
[118] C[N;7j+1
[119]G04:->(N=NA)/G05
[120] N+N+1
[121] }->\mathrm{ GO3
[122]^ M IS EVENT INDEX
[123]GO5:M+1
[124]G06:->(E[M;5]=1)/GO7
[125]a F2 IS LIST OF ACTIVITIES WHOSE ENDING EVENT IS EVENT BEING ANALYZED
[126] F2世,(ACT[;2]=E[M;1])/1NA
[127.ja IF FLAGS FOR ALL SUCH activities are set, update Event.
[128] FLAGS&,C[F2;7]
[129] }->(~(^/FLAGS))/G0
[130]a EXPECTED DATE FOR EVENT IS LATEST COMPLETION DATE OF ALL ACTIVITIES
[131]a LEADING TO THE EVENT
[132] E[M;2]+[/C[F2;3]
[133] E[M;5]+1
[134]G07:->(M=NE)/G08
[135] M+M+1
[136] }->G0
[137]^ IF ALL EVENT FLAGS ARE SET, ALL EXPECTED DATES ARE RESOLVED AND
[138]a FOFWARD PART OF ANALYSIS IS COMPLETE
[139]G08:+(~(^/E[;5]))/G002
[140]a FORWARD ANALYSIS COMPLETED. REVERSE NEXT
[141]a ZERO OUT FLAGS FOR RE-USE
[142] E[;5]+0
[143] C[;7]*0
[144] E[NE;3]+LATTEST
[145] E[NE;5]+1
[146]a N IS ACTIVITY INDEX
[147]G020:N+1
[148] F F1 IS REF. NO. IN E FOR ENDING EVENT aF ACTIVITY
[149]GO21:F1+B2,ACT[N;2]
[150]->(~(E[F1;5]=1)^(C[N;7]=0))/GO22
[151] C[N;5]+E[F1;3]
[152] C[N;4]+C[N;5]-C[N;1]
[153] C[N;7]+1
[154]GO22:->(N=NA)/GO23
[155] N+N+1
[156] ->GO21
[157 ja M IS EVENT INDEX
[158]GO23:M+1
```

```
[159]GO24:->(E[M;5]=1)/G025
[160]^ F2 IS A LIST OF ACTIVITIES WHOSE BEGINNING EVENT IS EVENT BEING ANALYZED
[161] F2+,(ACT[;1]=E[M;1])/1NA
[162] If flags for all such activities are SET, update EVENT
[163] FLAGS+,C[F2;7]
[164] ->(~(^/FLAGS))/GO25
[165]@ LATEST DATE FOR EVENT IS EARLIEST START DATE OF ALL ACTIVITIES COMING F
    ROM THE EVENT
[166] E[M;3]+L/C[F2;4]
[167] E[M;5]+1
[168]G025:+(M=NE)/GO26
[169] M+M+1
[170] ->GO24
[171]@ If all event flags are set, all latest dates are resolved and network a
    NALYSIS IS NEARLY COMPLETE
[172]GO26:->(~(^/E[;5]))/GO20
[173]@ COMPUTE SLACK
[174] E[;4]+E[;3]-E[;2]
[175]a DETEFMINE CRITICAL PATH
[176] CRIT+(E[;4]=(L/E[;4]))/E[;1]
[177]a CALL NET2 FOR OUTPUT REPORT
[178] NET2
    \nabla
    | NET2
[1] & THIS FUNCTION PRODUCES OUTPUT OF CPM OR PERT NETWORK ANALYSIS. IT
[2] A ACCEPTS VALUES FROM FUNCTION NET1 WHICH CALLS THIS FUNCTION AS ITS
[3] A LAST STATEMENT. THIS FUNCTION SHOULD NOT BE USED ALONE. NETWORK
[4] & ANALYSIS SHOULD BE INITIATED BY EXECUTING NETINFO OR NET1. THE FORMER
[5] & PROVIDES A DESCRIPTION OF THE WORKSPACE PRIOR TO GIVING THE USER THE
[6] A OPTION OF PERFORMING NETWORK ANALYSIS. THIS FUNCTION REFERENCES
[7] & \triangleFMT WHICH MAY NOT BE AVAILABLE ON SOME SYSTEMS.
[8] ค
```



```
[10] & THE CRITICAL PATH EVENTS AND IN ARRAYS E AND C. ARRAY E CONTAINS
[11] & EVENT INFORMATION.ONE ROW IS ASSIGNED TO EACH EVENT.
[12] & COLUMNS IN ARRAY E ARE DEFINED AS FOLLOWS:
[13] A (1) EVENT NUMBER (2) EXPECTED DATE (3) LATEST DATE
[14] (4) SLACK (5) STATUS FLAG
[15] a ARray C CONTAINS ACtIVITY INFORMATION. oNE ROW IS ASSIGNED to EACH
[16] ACTIVITY. COLUMNS IN ARRAY C ARE DEFINED AS FOLLOWS:
[17j ค (1) EXPECTED TIME (2) EXPECTED START DATE (3) EXPECTED
[18] COMPLETION DATE (4) LATEST START DATE (5) LATEST COMPLETION DATE
[19] (6) STANDARD DEVIATION (PERT ONLY) (7) STATUS FLAG
[20] A
    [21] VECTORS 1= ON CRITICAL PATH O=NOT ON CRITICAL PATH
[22] & CPAC IS ACTIVITY VECTOR CPEV IS EVENT VECTOR
[23] CPAC+(ACT[;1]\epsilonCRIT)^(ACT[;2]\epsilonCRIT)
[24] CPEV+E[:1]ECRIT
[25] ,
[26] 'CRITICAL PATH:'
[27] ',
[28j CRIT+(1,\rhoCRIT) \rhoCRIT
[29] 'P\+\squareI3' \triangleFMT(CRIT)
[30] , ,
```

```
[31] 'DEXPECTED COMPLETION DATE FOR PROJECT: ■,F7.2'\triangleFMT(E[NE;2])
[32] ',
[33] '\SLACK: M,F7.2' \triangleFMT(E[NE;4])
[34] ' '
[35] A CPM NETWORKS BFANCH TO LABEL GO3O
[36] }->(Z=3)/G03
[37] A PROBABILITY ANALYSIS FOR PERT NETWORKS ONLY
[38] QUES1:'DO YOU WANT TO INPUT COMPLETION DATE(S) FOR COMPUTATION OF Z VALUES
        '
[39] 'FOR THE NORMAL PROBABILITY DISTRIBUTION? ANSWER YES OR NO.'
[40] ->(GO31,GO30,QUES1)['YN'i1^,D]
[41] G031:';
[42] A COMPUTE STANDARD DEVIATION FOR THE NETWORK
[43] STDEV+(+/(C[;6]*2)*CPAC)*0.5
[44] ->(STDEV=0)/GO30
[45] 'INPUT COMPLETION DATE(S):'
[46] A+,口
[48] '\NETWORK STANDARD DEVIATION:\,F7.2' \triangleFMT(STDEV)
[49] , ,
[50] p compute 2 values
[51] K+(A-E[NE;2])\divSTDEV
[52] K+(1, \rhoK) \rhoK
[53] 'Z VALUES:'
[54] ,
[55] 'X5,F7.3' \triangleFMT K
[56] , ,
[57] ->GUES1
[58] G030:',
[59] QUES2:'FOR COMPLETE EVENT AND ACTIVITY ANALYSIS, TYPE MORE.'
[60] 'TO EXIT PROGRAM TYPE STOP.'
[61] +(GO32,0,QUES2)['MS'ו1^,D]
[62] GO32:' '
[63],
[64] ' EVENT ANALYSIS'
[65] , '
[66] EXPECTED EVENT LATEST ON CRTTICAL:
```




```
        AN ACTIVITY
[69] H-ACT[;1]
[70] J I ACT[;2]
[71] & ARRAY E WITH EVENT FLAG COLUMN REMOVED
[72] DATA1+(NE,4)+E
[73] G+NEP'.
[74] ARRAY G IS * FOR 'ON CRITICAL PATH' AND bLANK FOR 'NOT ON CRITICAL
[75] & PATH' USED IN EVENT ANALYSTS
[76] N+1
[77] G034:->(CPEV[N]=0)/G035
[78] G[N]*'*'
[79] GO35:->(N=NE)/G036
[80] N+N+1
[81] ->G034
[82] GO36:' '
[83] 'X4,I3,X12,F6.2,X9,F6.2,X6,F6.2,X11,A1' \triangleFMT(DATM1;G)
[84]G+NAp',
```

```
[85] A ARRAY G IS * FOR 'ON CRITICAL PATH' AND BLANK FOR 'NOT ON CRITICAL
[86] ค PATH' USED IN ACTIVITY ANALYSIS.
[87] N+1
[88] GO38:+(CPAC[N]=0)/C039
[89] G[N]+'*'
[90] G039:+(N=NA)/G040
[91] N+N+1
[92] }->\mathrm{ G038
[93] GO40:' '
[94] ,
[95] , '
[96j A CPM NETWORKS BRANCH TO GO50
[97] +(Z=3)/G050
[98] a PRODUCE PERT ACTIVITY REPORT
[99] , PERT ACTIVITY ANALYSIS.
[100]' '
[101]a AFfAY C WITH activity FLAG COLUMN REMOVED.
[102j DATA1+(NA,6)^C
[103] EXPECTED EXPECTED EXPECTED LATEST L
        ATEST STANDARD ONCRITICAL' COMPLETION START
```



```
[105]?-
```



```
        ; J;DATA1;G)
[107] ->0
[108]G050:' '
[109]^ PRODUCE CPM ACTIVITY REPORT
[110] DATA 1+(NA,5)+C
[111];,
[113] EXPECTED EXPECTED EXPECTED EATEST L
```



```
[115]
[116] 'I3, | \, I3,X7,F6.2,X9,F6.2,X9,F6.2,X8,F6.2,X7,F6.2,X12,A1' \triangleFMT(H;J;DATA1
    ;G)
    \nabla
```


# INTERACTIVE OPTIMIZATION OF A PRODUCTION SYSTEM 

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## DESCRIPTION

The APL model presented here uses Monte Carlo methods to simulate the behavior of a simplified production system. The system involves two independent random variables, one dependent random variable, and two decision variables. Given particular cost information, the problem is to find decision-variable values which minimize the average daily cost of the production process. This implies the need to experimentally investigate the nature of a cost surface, searching across the surface in an attempt to tind its low point. In general, such a search can be conducted according to one or more formalized searching strategies, or it can be based solely on informal strategies which the investigator devises intuitively. No searching strategy is built directly into the model given here; it consequently falls to the user to supply either a formal or an informal strategy for searching the cost surface efficiently and successfully. The model supports the search by letting the user interactively estimate the cost consequences of various alternative values (s)he chooses for the decision variables.

Assignments involving use of this model, or models similar to it, can be appropriate for a variety of audiences and in a variety of settings. Some of the possibilities are suggested below.

- The model can be used (as one in a series of computer models) in a "computer applications
in business" course to illustrate one way the computer can be employed to support decision making in the firm.
- As a more specific alternative to the above, the model can be brought into play in a course in production and operations management to suggest one mode of computer use in a production context.
- The model can be used in an introductory course in a discrete-event simulation as an example of the type of modeling in which the students themselves will engage.
- It can be used in a second-level course in computerimplemented algorithms to motivate the student of methods for seeking optima.
- The model may be of interest in courses dealing with probability and statistics. The production system on which the model is based has the flavor of a practical problem involving a combination of random variables whose complete analytic manipulation is difficult or impossible; in this sense, the underlying model demonstrates an alternative method for determining the properties of dependent random variables. In addition, for any given choice of decision-variable values, the model can be used to estimate the sampling distribution of a statistic of interest (e.g., average daily cost). Finally, the model can be used to explore the behavior of the distribution of the average daily cost estimator as a function of sample size (that is, as a function of the duration of each simulation).

Use of the model does not require previous computer experience. The user should understand the fundamental concepts of "relative frequency," but these concepts can be motivated intuitively for the purpose at hand; as a result, no course in probability and/or statistics is prerequisite to use of the model. Within these guidelines, and subject to whatever other requirements may be implied in the above list of suggested applications, the model could be used by students at any level in the curriculum.

It might be noted here that the model is designed to protect itself against "bad data" which the user might accidentally or intentionally feed to it. That is, the model examines all information inputted to it by the user, and determines whether the information is feasible in the context of the problem. If infeasible information is detected, the model asks the user to re-enter the information in question. For example, the model will not accept negative values for relative frequencies, it requires that relative frequencies sum to one hundred percent, and so on. A later section in this paper displays a sample session in which a hypothetical user deliberately tries to get the model into trouble, and shows how the model responds to such a user.

Provided below, under section headings entitled Instructions for Use and Sample Use, is a "user's writeup" which includes the following:

- A description of the production system
- An indication of the problem to be solved
- A description of a formalized searching strategy
- An illustration of model use

In spirit, the user's writeup is designed to be a self-contained problem statement from which copies can be made for distribution to students. Of course, instructors who decide to use the
problem might want to modify the user's writeup to suit their own purposes. For example, the writeup presented here describes the univariate searching strategy as one which might be employed to explore the cost surface in methodical fashion. Those who assign the problem might prefer to let their students develop their own heuristics spontaneously as a user-conducted search proceeds; or, it might be thought preferable to have the students follow some formalized searching strategy other than that of univariate search.

This problem was originally composed by the author to meet several differing needs for such a problem-model combination in the business curriculum at The University of Michigan. The system described here has been modeled in FORTRAN ${ }^{7}$ and in GPSS. ${ }^{2}$ Variations on the problem described here have been presented in SIMULETTER, the quarterly publication of ACM's Special Interest Group for Simulation. ${ }^{3}$

Instructions for Use
Statement of the Problem
In a certain factory, a goal of management is to operate 50 machines of a particular kind 8 hours a day, 5 days a week. Management owns 50 machines of the kind in question, and employs 50 machine operators (one per machine), so that this operating objective can be met, at least in theory. In practice, however, a problem arises in that each of the machines is subject to random failure. Whenever a machine fails, it must of course be taken out of operation. It is then routed to an in-house repair shop,

[^3]where it is eventually repaired. Meanwhile, unless backup machines are available to supplement the 50 owned machines, management's operating objective is not being met.

Management estimates that the profit opportunity which is foregone whenever fewer than 50 machines are in operation at all times during the 40 -hour work week is $\$ 22.50$ per hour per machine. For example, if only 47 machines are being operated during a given 2-hour period, then the associated profit opportunity which is foregone is $\$ 135$ ( $\$ 22.50$ times 3 times 2). For various reasons, any under-capacity operation which might come about cannot be made up by working overtime. Management does have the option, however, to supplement the 50 machines it owns by leasing (renting) machines of like kind on a long-term basis at a cost of $\$ 30$ per day per machine. (The leasing charges are independent of the extent to which the leased machines are actually used.) Management also can decide how many repairmen to employ for the purpose of repairing failed machines. For example, it might be decided to hire 2 repairmen, and to lease 9 machines. The Figure 1 diagram then shows what the overall state of affairs might be in the system at some arbitrary time. Each square in the diagram represents a machine. Squares without an $X$ in them denote machines which are either being operated, or are in backup status, ready for use when needed. Squares with an $X$ in them signify machines which either are being repaired, or are queued up waiting to go into repair. Of the 59 machines in this hypothesized situation, then, 2 are in repair; 2 are queued for repair; 5 are in backup status; and the other 59 are being operated.

Assignment
Your task is to determine for management that combination of repairmen-hired and machines-leased which will minimize the average daily cost of the production process. To help you in


Figure 1
task, a computer model has been built to simulate the operation of the factory. You are to work with the model to conduct a search for that hire-lease combination which minimizes the average daily cost of operating the factory. Pertinent lifetime and repairtime data for the machines in question are given below, and various modeling assumptions are stated. A strategy is also described for methodically searching for the minimum-cost hirelease combination. Finally, the history of a typical session involving use of the available computer model is shown.

After scanning the sections on data and modeling assumptions, you should do the following:

- Study the section on searching strategy
- Review the specifics of the sample session
- Go to a computer terminal and use the model to perform the requested optimization.
- Write up and hand in a brief report to management, summarizing the results of your investigation and providing your final recommendations.

Data
Based on past records, the lifetime of a machine which has just been repaired is distributed as follows:

| Lifetime, |  |  |  |  |  |  |  |  |  |  |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Hours: | 110 | 120 | 730 | 140 | 150 | 160 | 170 | 180 | 190 | 200 |
| Relative Frequency, $\%: ~$ | 3 | 6 | 8 | 12 | 21 | 17 | 11 | 9 | 8 | 5 |

Records also indicate that the time required to repair a failed machine (not counting any time spent waiting to go into repair) follows the distribution given below.

| Repairtime, Hours: |  | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| :--- | :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Relative Frequency, \%: | 7 | 10 | 16 | 20 | 15 | 11 | 10 | 8 | 3 |  |

## Modeling Assumptions

The computer model which simulates operation of the factory is based on the following assumptions.

- The time required to replace a failed machine with a backup machine is negligibly small.
- Owned machines and leased machines are virtually identical to one another. They are characterized by the same lifetime and repairtime distributions. Like owned machines, when leased machines fail they are repaired in-house.
- The lifetime and repairtime distributions are independent of a machine's operating history.
- Machines are taken out of operation only when they fail.
- Repairmen always work on an individual basis, one repairman per machine being repaired. (Idle repairmen cannot team up with busy repairmen to speed up the process of completing a machine's repair.)
- Each simulation performed with the model starts with the factory at typical "steady state" conditions. For example, at startup time those machines being operated already have used up some randomlychosen fraction of their current lifetime. (The random fraction is determined separately, machine by machine.) This means that transient phenomena do not have to be taken into account in interpreting statistics printed out by the model at the end of each simulation.

Strategy for Use of the Model
The model is to be used to estimate the hire-lease combination which minimizes the average daily cost of running the factory. Some thought should be given then, to the way the cost is expected to behave as various hire-lease combinations are considered. For a fixed number of repairmen, average daily cost will vary with "machines rented" as shown in Figure 2. With too few rented machines, costs are high because of the foregone profit opportunities resulting from under-capacity operation. With too many rented machines, costs are also high because the leasing fee is being paid to provide more supplemental machines than are necessary. Somewhere between these two extremes, the average


Figure 2
Figure 3
cost can be expected to pass through a minimum, as is suggested in Figure 2.

Similarly, for a given number of rented machines, the influence of "repairmen hired" will follow the pattern in Figure 3. With too few repairmen, high average costs are experienced because the cost component associated with under-capacity operation is large. With too many repairmen, costs are high because the wage component is larger than it need be. It is reasonable to expect that average daily cost goes through a minimum somewhere between these two extremes, as per Figure 3.

A three-dimensional perspective of the situation is suggested in Figure 4. Note that the mesh points in the grid laid down in the Figure 4 hired-rented plane represent feasible (that is, non-negative and integer-valued) choices of values for the decision-variable pair. Located above each of these mesh points, in the third dimension, is the expected value of the daily cost corresponding to that particular hire-rent alternative. (These cost points are not shown in Figure 4.) The collection of all such cost points forms a cost surface in the third


Figure 4
dimension. (The term "surface," although suggestive, is a bit misleading here. The points do not actually form a surface; instead, they simply form a collection of discrete values, with no continuum joining them.) Figures 2 and 3 are then simply contours through this cost surface.

It can be argued that the cost surface in this problem is like that of an irregularly shaped bowl. More specifically, it can be argued that the cost is a unimodal function of the two decision variables involved. A function is unimodal if the independent variables are altered in an (arbitrarily) given direction, and if the resulting values of the function are found initially to decrease down to some minimum, and then to rise again. In such functions, as the name suggests, there is only a single low point. Note the consistency between the concept of unimodality, and the shape of the Figure 2 and Figure 3 contours through the
cost surface. ${ }^{4}$
Given that the cost surface is unimodal, the search for the optimal hire-rent combination, then, is essentially a search for the only "lowest point" on the cost surface. This unimodality can be exploited by employing a univariate searching strategy to seek the conditions under which the cost function assumes its minimum value. Briefly, the univariate strategy involves moving through the search domain along successive contours until all more promising directions of movement have been exhausted. In the context of the problem at hand, the specifics of a univariate search are outlined below.
(1) Perform a simulation with the model to estimate the average daily cost associated with some first choice of a hire-rent combination. (In this problem, preliminary hand computations can be carried out to estimate a reasonable hire-rent combination with which to begin.)
(2) Holding the "number hired" constant, vary the "number rented" and perform corresponding simulations until the low point in the corresponding cost contour has been found. This corresponds to finding the low point in Figure 2.
(3) Holding the "number rented" constant at its lowpoint value from (2), vary the "number hired" and perform corresponding simulations until the low point in that cost contour has been found.

4 For more information about the concept of unimodality, see Beveridge and Schechter, Optimization: Theory and Practice, McGraw-Hill, New York, 1970, and Wilde and BeightTer, Foundations of Optimization, Prentice-Ha11, Englewood Cliffs, N. J. , 1967.

This is equivalent to finding the low point in Figure 3.
(4) Is the final hire-rent pair in (3) the same as that in (2)? If not, return to (2). Otherwise, go to (5).
(5) Call the best hire-rent combination found so far the tentative optimum. As a final check, simulate for the as-yet-uninvestigated hire-rent combinations (if any) surrounding this tentatively optimal combination.
(6) Is the lowest-cost point in (5) that of the tentative optimum? If so, the search is finished. If not, let the lowest-cost point be the new tentative optimum, and return to (5).

In carrying out the steps just described, it is helpful to enter the various cost points in a grid as the search proceeds. Figure 5 provides a grid which can be used for this purpose.

It should now be clear where the univariate searching strategy gets its name. Only one decision variable is permitted to vary at a time, while the other is held constant (or, more generally, while the others are held constant). Of course, the univariate searching strategy involves a well defined, step-by-step procedure, meaning it can be programmed and need not necessarily be carried out interactively by a person sitting at a computer terminal. (For a FORTRAN subroutine which implements the generalized univariate searching strategy, see "Use of An External Optimizing Algorithm with a GPSS Model," by Robert M. Lefkowits and Thomas J. Schriber, Proceedings of the Fifth Conference on Applications of Simulation, 1971, pp. 1-6.)


Figure 5

Note that in a simulation context, a potential problem can arise with any searching strategy because each simulation only provides an estimate of the expected daily cost. If the variability of the estimator is high (because, for example, each simulation is of short duration), it is possible to draw a false conclusion about where the low cost point is located. (Strictly speaking, before the computer model is employed for optimization purposes, it should be used to study the behavior of the cost estimator as a function of the duration of simulation. Statistical methods should then be used either to determine point estimates of the expected cost values, or to construct interval estimates of the expected cost values at whatever is judged to be an acceptable confidence level. For simplicity here, it is simply recommended that each simulation be performed for 200 working days, and that the resulting average daily cost be taken as a point estimate of the expected cost value.)

Sample Use

Use of the computer model is illustrated in the sample sessions displayed in the following section. Lifetime and repairtime data used in these sessions are identical to those given earlier in the statement of the problem. This is also true of the cost data. The recommended simulation span of 200 days has been used for each of the two simulations performed in the sample session.

The first sample session should be largely self-explanatory. The model requests information from the user by issuing questions such as HOW MANY VALUES CAN THE LIFETIME RANDOM VARIABLE ASSUME? and commands such as ENTER THE VARIOUS LIFETIME VALUES. The user responds by typing in numbers on some occasions and by typing in words on other occasions. The dialogue between the model and the
user is easily followed simply by reading through this sample session. With the sample session in hand, even a first-time computer user can sit at a terminal and engage in a similar dialogue with the model almost without effort.

The second sample session is designed to demonstrate how the model analyzes the user inputs for feasibility. As in the first session, this second session should be self-explanatory. As this session suggests, every attempt has been made to design the model to trap infeasible data inputs, notify the user when infeasible data are encountered, and give the user an immediate opportunity to type in acceptable information.

## Comments on the Program Listing

Following the sample sessions is a complete listing of the model. Except for using the public functions IPI, INP, and $\triangle F M T$, the model is self-contained. (Code for the input functions IPI and INP is provided in an appendix to this monograph. $\triangle F \bar{Z} T T$ is a proprietary function of the Scientific Time Sharing Corporation, and is available in their APL/Plus System. The user who does not have access to APL/Plus can substitute his own logic in place of $\triangle E M T$. In this model, that would not be unduly difficult to do.)

The model consists of 15 functions (modules). The first of these functions, MASTERACONTROL, acts as a logical main program. MASTERACONTROL systematically routes control to each of the other functions which make up the overall package. The names of these other functions have been chosen to suggest their role in context (e.g., GETALIFEADATA, GET $\triangle R E P A I R \triangle D A T A, S I M U L A T E, ~ P R O D U C E A R E P O R T$ ). All variables in the model are global in type, which paves the way for ease of communication among the various modules.

The last point to be made involves the amount of CPU time required to simulate with this model. Each 200-day simulation performed in the first sample session required about 12 CPU seconds on UCLA's IBM 360/91 computer. Of course, Monte Carlo simulations are known for the computer time they may require, and this is compounded here by the fact that APL is an interpretive language. Those who might choose to use this model for pedagogical purposes should take this rather large CPU-time requirement into account.

## PROGRAM USAGE

```
    ) LOAO KUN\trianglePACKAGE
SAVED 16.18.21 07/11/75
HON MANY VALUES CAN THE LIFETIME RANDOM VAKIAELE ASSUME?
(ENTER AN UNSIGEEL INTEGER > 0): 1
ENIER TiE VAKIOUS LIEETINE VALUES: 225
ENTEK THE COFKESPONDING RELATIVE FKEQUENCIES
(AS EEEKCENTAGES): 100
HOW MANY VALUES CAN THE KEPAIKTIME RANDON VARIABLE ASSUME?
(ENTER AN UNSIGNED INTEGER > 0): FIDDLESTICKS
PLEASE ENTEK POSITIVE INTEGER(S): -}
PLEASE ENTER POSITIVE INTEGER(S): 0
TRY AGAIN
HOW MANY VALUES CAN THE FEPAIRTIME RANDOM VARIABLE ASSUME?
(ENTEK AN UNSIGNED INTEGEK > 0): +4
ELEASE ENTER POSITIVE INTE,AR(S): 4
enTEk The vakiOUS kEPAIRTIME VALIES: 50
ENTEK 3 MOFE VALUES 6O 70 80 90
IOO MANY VALUES ENTEKED, SHOULD HAVE ENTERED 3 VALUES
ENTEK 3 MORE VALUES 60 70 80
ENTEK THE COKRESPONDING FELATIVE FREQUEWCIES
(AS EEKCENTAGES): 15 20 25 20
YOUK KELATIVE FREQUENCIES SUM TO 80 PEFCENT
TRY AGAIN
EWTEF THE COKKESPONLING RELATIVE FKEGUENCIES
(AS EEFCENTAGES): 20 25 30 25
ENTER THE REPAIRVEN'S WAGES ($/MAN-HOUR): -5.75
NEGATIVE VALUES AEE NOT VALID, TRY AGAIN
ENTER THE REEAIRMEN'S WAGES (S/MAN-HOUR): THEY EAKN TOO MUCH!
NONE NUMEFIC INEUTS ARE INVALID, TRY AGAIN
ENTER ThE FEPAIRMEN'S WAGES ($/MAN-HOUK): 7.50
ENTER THE MACHINE LEASING CHARGE (#/MACHINE-DAY): $25.50
NONE NUMEEIC INEUTS ARE INVALID, TRY AGAIN
ENTEK THE MACBINE LEASING CHARGE ($/MACHINE-DAY): 25.50
ENTEK THE ERODUCTION CAPACITY (I.E., THE NUMBER
OE MACHINES WHICH CAN BE OPERATED SIMULTANEOUSLY): 0
```

```
TRY AGAIN
ENTEF THE PRODUCTION CAPACITY (I.E., THE NUMBEK
OF MACHINES WHICH CAN BE OPERATED SIMULTANEOUSLY): 50
ENTER THE LOST PRODICTION PENALTY ($/MACHINE-HOUR): +10
NONE NUMERIC INPUTS ARE INVALID, TRY AGAIN
ENTER THE LOST PRODUCTION fENALTY ($/MACHINE-HOUR): 10
HOW MANY REPAIRMEN SHOULD THERE BE IN TOTAL?: NONE
PLEASE ENTER POSITIVE INTEGEK(S): 0
TRY AGAIN
how maNy repalkmein should there be in total?: 5
HOW MANY LEASED MACHINES ShOULD THERE EE IN TOTAL?: 0
FOR HOW MANY 8-HOUR DAYS DO YOU WANT TO SImULATE?: 0
TEY AGAIN
FOR HON MANY 8-HOUR DAYS DO YOU WANT TO SIMULATE?: -500
PLEASE ENTER POSITIVE INTEGER(S): 250
```


NO. OF DAYS SIMULATEL: 250
FEFAIRMEN HIRED:
AVERAGE REFAIRMEN IN USE: 4.97
DAILY EAYROLL EXPENSE: $\$ 300.00$
MACHINES LEASED:
0
DAILY LEASING EXPENSE: $\$ 0.00$
AVERAGE DAILY
UNDEE-PRODUCTION LOSSES: \$2.548.85
---------------------------------------
AVERAGE DAILY COST: $\quad \$ 2,874.35$

WHAT DO YGU WANT TO DO NEXT?

```
YOUR CHOICES ARE AS FOLLOWS...
IF YOU YOU WILL BE GIVEN A CHANCE TO
TYPE IN... SET A NEW KALUE EQR...
HIRED MEN-HTRED
LEASED MACHINES-LEASED
ruN-LENGTH DURATION of SImULATION
IF YOU
TYPE IN... WHAT WILL HAPPEN IS...
SImulate ANOTHER SIMULATION WILL EE PEREORMED
DONE YOUR USE OE THE MODEL WILL END
EXPLAIN THIS LIST OF CHOICES WILL BE TYPED OUT
(yOU ONLY NEED tYPE IN the firSt letter in each case)
WHAT IS YOUR CHOICE?
AIRED
HOW MANY REPAIRMEN SHOULD THERE BE IN TOTAL?: 3
WHAT DO YOU WANT TO DO NEXT?
LEASED
HOW MANY LEASED MACHINES ShOULD THERE BE IN TOTAL?: 5
WHAT DO YOU WANT TO DO NEXT?
SIMULATE
_ REPQRT QN SIMULATIQN_RESULTS
NO. OF DAYS SIMULATED: 200
REPAIRMEN HIRED: 3
AVERAGE REPAIRMEN IN USE: 2.43
DAILY PAYROLL EXPENSE: $162.00
MACHINES LEASED:
5
DAILY LEASTNG EXPENSE: $150.00
AVERAGE DAILY
UNDER-PRODUCTION LOSSES: $58.08
```



```
AVEFAGE DAILY COST: $250.08
WHAT DO YOU WANT TO DO NEXT?
```

```
        LOAD RUN\trianglePACKAGE
SAVED 16.18.21 07/11/75
How many values can the lifetime random variable assume?
(ENTER AN UNSIGNED INTEGEF > 0): 10
ENTER THE VARIOUS LIEETIME VALUES: 110}120120130 140 150 160 170 180
ENTER 2 MORE VALUES 190 200
enter the corresponding relative erequencies
(AS PERCENTAGES): }\begin{array}{llllllllllll}{3}&{6}&{8}&{12}&{21}&{17}&{11}&{9}&{8}&{5}
HON maNY values can the repairtime random variable assume?
(ENTER AN UNSIGNED INTEGER > 0): 9
ENTER THE VARIOUS REPAIRTIME VALUES: 4 5 5 6 7 8 9 10 11 12
enter the cofresponding relative frequencies
(AS PERCENTAGES): }
entek the repaikmen's wages ($/MAN-HOUR): 6.75
ENTER THE machine LeASING CHARGE ($/mAChINE-dAY): 30
ENTER THE PRODUCTION CAPACITY (I.E., THE NUMEER
OE MACHINES WHICH CAN BE OPERATED SIMULTANEOUSLY): 50
ENTER THE LOST PRODUCTION PENALTY (/MACHINE-HOUR): 22.50
HOW maNY REPAIRMEN SHOULD THERE BE IN TOTAL?: 5
how many leased machines should there be In total?: 3
EOR HOW MANY &-HOUR DAYS DO YOU NANT TO SIMULATE?: 200
RERERT QN SIMULATIQN KESULTS
NO. OF DAYS SIMULATED: 200
FEPAIRMEN HIRED: 5
AVERAGE REPAIRMEN IN USE: 2.39
DAILY PAYROLL EXPENSE: $270.00
MACHINES LEASED:
    3
DAILY LEASING EXPENSE: $90.00
AVERAGE DAILY
UNDER-PRODUCTION LOSSES: $67.12
--------------------------------------
AVERAGE DAILY COST: $367.12
WHAT DO YOU WANT TO DO NEXT?
```

```
LEASED
```

```
HOW mANY LEASED machines ShOULD there be In total?: 6
NHAT DO YOU WANT TO DO NEXT?
SIMULATE
    REPQRI_QN_SIMULATIQN RESULTS
NO. OF DAYS SIMULATED: 200
REPAIRMEN HIRED:
2.38
AVERAGE REPAIRMEN IN USE:
DAILY PAYROLL EXPENSE:
MACHINES LEASED: 6
162.00
DAILY LEASING EXPENSE: $180.00
AVERAGE DAILY
UNDER-PRODUCTION LOSSES: $4.82
--------------------------------------
AVEFAGE DAILY COST: $196.82
WHAT DO YOU WANT TO DO NEXT?
DONE
```


## PROGRAM DESCRIPTION

```
    \nabla PRODUCE\triangleREPOFT
[1] CR,', EEPQRT QN_SIMULATIQN_RESULTS_,'CR
[2] 'DNO.OF DAYS SIMULATED:O,I10' \triangleFMT (DAYS)
[3] 'पREPAIRMEN HIRED:\,I16' \triangleFMT(HIRED)
[4] 'TAVERAGE REPAIRMEN IN USE:凹,F10.2' \triangleFMT(MEN\triangleUSE\divCLOCK)
[5] PAY+8\timesHIRED NWAGE\triangleEATE
[6] 'DDAILY PAYROLL EXPENSE:T,CPT&TE13.2' \triangleFMT(PAY)
[7] 'WMCHINES LEASED:M,I16' \triangleFMT(LEASED)
[8] '[DAILY LEASING EXPENSE'#,CPM&ME13.2* \triangleFMT(LEASED\timesLEASE\triangleRATE)
[9] LP\triangleLOSS +((PKOD\triangleCAPASITY ×CLOCK) -MACH\triangleUSE) ×LOSS\triangleRATE\divDAYS
[10] 'AVERAGE DAILY'
[11] 'WUNDER-PRODUCTION LOSSES:[,CP#QMF11.2' \triangleEMT(LP\triangleLOSS)
[12] (35\rho'-')
[13] '\AVERAGE DAILY COST:ए,CPए&#F16.2' \triangleFMT(+/PAY,LEASE\triangleRATE,LP\triangleLOSS)
[14] (35\rho,'')
\nabla
    \nabla EXPLAIN\triangleCHOICES
[1] CR,'YOUR CHOICES ARE AS FOLLOWS...',CR
[2] IE YOU YOU WILL BE GIVEN A CHANCE TO'
[3] 'TYEE IN... SET A NEW KALUEE EQE ..',CR
[4] THIRED MEN-HIRED'
[5] 'LEASED MACHINES-LEASED'
[6] 'RUN-LENGTH DUKATION OF SIMULATION',CR,CR,'IF'YOU'
[7] 'TYPE IN... WHATT WILL HAPEPEN IS..',C\underline{R}
[8] 'SIMULATE ANOTHER SIMULATION WILL BE PERFORMED'
[9] 'DONE YOUR USE OE THE MODEL WILL END'
[10] 'EXPLAIN THIS LIST OF CHOICES WILL BE TYPED OUT',CE
[11] '(YOU ONLY NEED TYPE IN THE EIRST LETTER IN EACH CASE)',
[12] CE,'WHAT IS YOUR CHOICE?',CE
\nabla
```

```
    \nablaGET\triangleWAGE\triangleDATA
[1] aNOTE THE USE OE 'IINP'' IN THIS FUNCTION.
[2] WAGE\triangleRATE+1 INP EROMPT7
    \nabla
    \nablaGET\triangleLEASING\triangleDATA
[1] ANOTE THE USE OF 'INP'' IN TAIS EUNCTION.
[2] LEASE\triangleRATE+1 INP EROMPT8
    \nabla
    \nablaGET\trianglePEOD\triangleCAPACITY
[1] qNOTE THE USE OF ''IPI'' IN THIS EUNCTION.
[2] REPEAT:->REPEAT\times1\rho\+(1>PROD\triangleCAFACITY+1\uparrowIPI PROMPT10)/'TRY AGAIN'
    \nabla
    \nablaGET\triangleLOST\trianglePROD\trianglePENALTY
[1] ANOTE THE USE OE "INP" IN THIS EUNCTION.
[2] LOSS\triangleRATE+1 INP PROMPT9
    \nabla
    \nabla GET\triangleMEN\triangleHIRED
[1] ANOTE THE USE OF 'IPI'" IN THIS FUNCTION
[2] REPEAT:->REPEAT\timesı\rho[] (1>EIRED<1^IPI PROMPT11)/'TRY AGAIN'
    \nabla
    \nablaGET\triangleMACHINES\triangleLEASED
[1] RNOTE TEE USE OF 'IPI'' IN THIS FUNCTION
[2] REPEAT:->REPEAT\times1\rho\square+(0>LEASED*1\uparrowIPI PROMPT12)/'TKY AGAIN'
    \nabla
    \nabla GET\triangleSIM\triangleSPAN
[1] qNOTE THE USE OF 'IPI'" IN THIS FUNCTION
[2] KEPEAT: +REPEAT\times1\rho[1&(1>DAYS+1ヶIPI PROMPT13)/'TRY AGAIN',
    \nabla
```

```
    \nabla K+CH NM MT;G
[1] }\quadk+(M\mp@subsup{]}{}{\prime}=CH)/1\rhoM
[2] G+[/K+K-1,1+-}1+
[3] MT*(MT\not=CH)/MT
[4] }K+((\rhoK),G)\rho(,F\circ,\geq1G)\(MT\not=CH)/M
    \nabla
    \nablaK<NIP P;O;S;I;D;E;T
[1] A NUMERTC INEUT;AUTHOR: KOY SYKES, STSC.
[2] }->4,04-?
[3] E:P*'INCORKECT NUMBEF...PLEASE REENTER',(1+(0=\rhoE) \rho':'),E
[4] E\leftarrow(1+T\leftarrowO+P1'A') +P\leftarrow,P
[5] P&T+P
[6] }->(0\quad1=\rhoT+AKI P)/ 6 9
[7] T+O+'0123456789.- -E'`T
[8] }->(13\inT+(S+((F\leftarrow1)\uparrowT)\epsilon 11 12)+T)\phi 15 11
```



```
[10] 
[11] P<(1+D<O+T:13) \downarrowT
[12] }->(v/10\leqP+(I+11=1\uparrowP)\downarrowP)\rhoE
[13] }->(0\in(\rhoE),\rhoT\leftarrowD\uparrowT)\rhoE\underline{E
[14] P*10*(-1*I)\times10\perpP
[15] ->((\vee/T\geq11)\vee10€D&(1+I\leftarrow0+T110)+T)\rhoE
[16] }->(0=\rhoT+(I\uparrowT),D)\rhoE
[17] T+P\times(\mp@subsup{}{}{-1}10.1 <.*S,\rhoD)\times10\perpT
[18] }->19+T\pm\lfloor\mp@subsup{T}{}{\prime
[19] T}\leftarrow\
[20] K+I
    \nabla
    \nabla DRAW <CDE SAMFCN RVVALS
[1] ATHIS FUNCTION FETURNS A VALUE ORAWN EROM THE POPULATION 'RVVALS'' EOR
[2] aWHICH THE CORKESPONDING CUMULATIVE DISTRIBUTION FUNCTION IS 'CDE''
[3] DKAW+(,RVVALS)[(((-1+?100000)\div100000)\leq,CDF):1]
    \nabla
    \nabla SEFAKATE S; B
[1] NUM*(B\leftarrow\DeltaVI互)/\DeltaFI \underline{S}
[2]
    ALPH+(~B)+\triangleMI \underline{S}
    \nabla
```

```
    \nabla DEFINE\triangleMAIORAPROMPTS
[1] athese fromptS ARE USED bY THE INPUT FUNCTIONS CALLED IN
[2] aLINES 7-15 AND 27-29 IN THE MASTER CONTROL FUNCTION.
[3] aDEFINE CR TO BE A CARRIAGE RETURN CHARACTER
        CR+'
    !
[5] PROMPT1+CE,'HOW MANY VALUES CAN THE LIFETIME RANDOM VAFIABLE ASSUME? '
[6] PROMPT 1+PROMPT 1,CR,'(ENTER AN UNSIGNED INTEGEK> 0):,
[7] PROMPT 2+'ENTER THE VARIOUS LIFETIME VALUES: '
[8] PROMPT3-GR,'ENTER THE CORRESPONDING RELATIVE EREQUENCIES'
[9] PROMPT 3+PROMPT 3,CR,'(AS PEECENTAGES): '
[10] PROMFT4+GR,'HOW MANY VALDES CAN THE REPAIRTIME fANDOM VAFIABLE ASSUME?'
[11] PROMPT4+PROMPT4,CR,'(ENTER AN UNSIGNED INTEGER> >): '
[12] PROMPT5*'ENTER THE VARIOUS REPAIRTIME VALUES: '
[13] PROMPT6+CR,'ENTER THE CORRESPONDING RELATIVE FREQUENCIES'
[14] PROMPT6+PROMPT6,CR,'(AS PERCENTAGES): '
[15] PROMPT7+CR,'ENTER THE REPAIRMEN''S WAGES (A/MAN-HOUR): '
[16] PROMPT8+CR,'ENTER THE MACHINE LEASING CHARGE ($/MACHINE-DAY): '
[17] PROMPT9+'ENTER THE LOST PRODUCTION PENALTY ($/MACHINE-HOUK): '
[18] PROMPT 10+CR,'ENTER THE PRODUCTION CAPACITY (I.E., THE NUMEEER,
[19] PROMPT10&PROMPT10,CE,'OF MACHINES WHICH CAN BE OPERATED SIMULTANEOUSLY):
[20] PROMPT11-CR,'HOW MANY FEPAIRMEN SHOULD THERE BE IN TOTAL?:'
[21] PROMPT12*'HOW MANY LEASED MACHINES SHOULD THERE EE IN TOTAL?: '
[22] PROMPT13+'FOR HOW MANY 8-HOUR DAYS DO YOU WANT TO SIMULATE?:'
    \nabla
    | getalife\dATA
[1] athis function makes direct use of the INPUT funCtIONS "IPI'"
[2] AAND ''INP''. (SEE THE MONOGRAPH APPENDICES FOK DETAILS)
[3] REPEAT:->REPEAT\times10[1+(1>LTIMES <1^IPI PROMPT1)/'TRY AGAIN:
[4] LTVALS&LTIMES INP PROMPT2
[5] AGAIN:LTDIST ++\0.01\timesLTDIST LTIMES INP EROMPT3
[6] }->((\mp@subsup{(}{}{-}1\uparrowLTDIST)>0.99)^(\mp@subsup{}{}{-}1\uparrowLTDIST<1.01))/SET2ONE
[7] YOUR RELATIVE FREQUENCIES SUM TO ';100*`1^LTDIST;' PERCENT'
[8] 'TRY AGAIN'仓 ใAGAIN
[9] SET2ONE:LTDIST[LTIMES]+1 0 ->0
    \nabla
    \nabla GETAREPAIR\triangleDATA
[1] aTHIS EUNCTION MAKES DIRECT USE OF THE INPUT EUNCTIONS 'IPI'"
[2] AAND 'INP''. (SEE THE MONOGRAPH APPENDICES EOK DETAILS)
[3] REPEAT:->REPEAT\times10П+(1>FTIMES+14IPI PROMPT4)/'TRY AGAIN,
[4] RTVALS&ETIMES INP PROMPT5
[5] AGAIN:RTDIST++\0.01\timesRTDIST+RTIMES INP PROMPT6
[6] }->(((\mp@subsup{}{}{-}1\uparrowRTDIST)>0.99)^(~1^RTDIST<1.01))/SET 2ONE
[7] 'YOUR RELATIVE FREQUENCIES SUM TO ';100×`1^RTDIST;' PERCENT'
[8] 'TRY AGAIN'\diamond ->AGAIN
[9] SET2ONE:RTDIST[RTIMES]+1 & ->0
\nabla
```

```
    | MASTER\triangleCONTROL
[1] aTHE mASTER CONTROL FUNCTION ROUTES CONTROL DIRECTLY TO
[2] a13 OF THE OTHER 14 FUNCTIONS WHICH CONSTGITUTE THE MODEL.
[3] a(THE 14TH FUNCTION, ''SAMFCN'', IS CALLED FROM THE
[4] afunCTION 'SIMULATE''.) THE VARIOUS FUNCTION NAMES
[5] aARE DESIGNED TO REVEAL THE FUNCTION fOLES.
[6] DEFINE\triangleMAJOR\trianglePROMPTS
[7] GET\triangleLIFE\triangleDATA
[8] GET\triangleREPAIR\triangleDATA
[9] GET\triangleWAGE\triangleDATA
[10] GET\triangleLEASING\triangleDATA
[11] GET\trianglePROD\triangleCAPACITY
[12] GET\triangleLOST\trianglePFOD\trianglePENALTY
[13] GET\triangleMEN\triangleHIRED
[14] GET\triangleMACHINES\triangleLEASED
[15] GET\triangleSIM\triangleSPAN
[16] ASET CODE TO CONTROL PRINTING OF EXPLANATIONS
[17] R(SEE LINES 22-25)
[18] CODE+0
[19] SIM:SIMULATE
[20] PRODUCE\triangleEEPORT
[21] MORE:CR,'WHAT DO YOU WANT TO DO NEXT?',CE
[22] }->(CODE=1)/SKI
[23] EXPLAIN\triangleCHOICES
[24] CODE+1
[25] SKIP:->SKIP\times1p[+(1\not=(CHAR+1^巴)\epsilon('HLRSDE'))/'TRY AGAIN'
[26] ->(HIRE,LEASE,SPAN,SIM,DONE,EXPLAIN)['HLFSDE',CHAR]
[27] HIRE:GET\triangleMEN\triangleHIRED 人 ->MORE
[28] LEASE:GET\triangleMACHINES\triangleLEASED\diamond ->MORE
[29] SPAN:GET\triangleSIM\triangleSPAN \diamond ->MORE
[30] EXPLAIN:EXPLAIN\triangleCHOICES O ->MORE
[31] DONE:->
    \nabla
```

```
    \nabla SIMULATE
[1]
[2] AINITIALIZE PEKTINLNT VARIABLES
[3] CLOCK+FIXQ MACH\triangleUSE+MEN\triangleUSE&O \ FCTIMES+BUTIMES&10
4] INUSE+FROD\triangleCAPACITY
[5] TOY:BDTIMES+BLTIMES,(LTDIST SAMFCN LTVALS)\times(``1+?1000)\div1000
[6] }->(PKOD\triangleCAPACITY>PBDTIMES)/TO
[7] MEN\triangleIDLE\leftarrowHIRED 人 READY\leftarrowLEASED\widehat{STOPTIME\leftarrowDAYS×8}
[8] AFIND IMMINENT EVENT TIME; UPDATE USE STATISTICS AND CLOCK
[9] NEXT\triangleE'VENT:ETIME'&L/BDTIMES,RCTIMES.STUPTIME
[10] MEN\triangleUSE+MEN\triangleUSE+(HIKED-MEN\triangleIDLE) x(JUMP+ETIMEE-CLOCK)
[11] MACH\triangleUSE+MACH\triangleUSEE+INUSEXJUMP \ CLOCK+ETIME
[12] USAGE&USAGE+INUSE×(ETIME-CLOCK)\diamondCLOCK\leftarrowETIME
[13] aBRANCH TO IMMINENT EVENT, OF BRANCH OUT NHEN DONE
[14] }->((ETIME\inKCTIMES), ETIME\inBUTIMES)/EIXED,EAILED O ->
[15] aUPDATING IN KESPONSE TO A MACHINE BREAKDOWN EOLLOWS
[16] EAILED:EDTIMES +(`1\downarrow(HOLD\uparrowBDTIMES)),(HOLD\leftarrowBDTINESIETIME) &EDTIMES
[17] ABRANCH IF FAILED MACHINE MUST QUEUE UP FOR REPAIR
[18] ->Q2FIX\timesIMEN\triangleIDLE=0 ○ MEN\triangleIDLE&MENDIDLE-1
[19] RCTIMES&RCTIMES,CLOCK+RTDIST SAMFCN KTVALS
[20] aBRANCH IF NO OTHEK MACHINES ARE READY FOK USE
[21] TEST\KEADYQ:->(KEADY=0)/NONE\triangleREADY 今 KEADY - READY-1
[22] ->NEXT\triangleEVENT,BDTIMES+BDTIMES,CLUCK+LTDIST SAMFCN LTVALS
[23] Q2FIX:->TEST\triangleREADYQ,EIXQ&FIXQ+1
[24] NONE\triangleKEADY:->NEXT\triangleEVENT,INUSE+INUSE-1
[25] aUPDATING IN RESPONSE TO FEPAIR COMPLETION FOLLOWS
[26] FIXEV:KCTIMES*('1\downarrow(HOLD\uparrowECTIMES)),(HOLD~KCTIMESIETIME)\downarrowKCTIMES
[27] &EKANCH IE THE KEPAIKED MACHINE IS NEEDED NOW
[28] +NEEDED\timesIINUSE*PKOD\triangleCAPACITY
[29] ABRANCH TO PUT KEPAIRMAN BACK TO WORK (IF POSSIBLE)
[30] ->QTEST,READY+KEALY+1
[31] NEEDED:INUSE+INUSE+1 今 BDTIMES&BDTIMES,CLOCK+LTDIST SAMFCN LTVALS
[32] &BKANCH IF ANOTHEK FAILED MACHINE IS WAITING FOK THIS REPAIKMAN
[33] QTEST:->NEXT\triangleKEPAIF\times1FIXQ\not=0
[34] ->NEXT\triangleEVENT,NEN\triangleIDLE&NEN\triangleIDLE+1
[35] NEXT\triangleFEFAIK:EIXQ+EIXQ-1
[36]
->NEXT\triangleEVENT,FCTIMES FCTIMES,CLOCK+KTLIST SAMFCN KTVALS
\nabla
```

3.14<br>INTERACTIVE INVENTORY SIMULATOR<br>Ralph H. Sprague, Jr.<br>Professor<br>College of Business Administation<br>University of Hawaii Honolulu, Hawaii

## DESCRIPTION

## Introduction

This system of APL programs allows students to obtain an optimum decision for economic order quantity ( $Q$ ) and reorder point (R) in a stochastic inventory system by iterative search. The iterative search procedure allows the student to experiment with alternative methods of convergence on the optimum solution. One of the functions can also be used to reinforce the concept of appropriate choice of simulation run length based on the sampling distribution of resultant cost. The major functions in the system are:

SET - To set initial values
SETRL - To experiment with simulation run length
SIM - To perform one simulation run
SEARCH - To search for optimum, Q, R
ENTDDIST - To enter probability distributions
ENTLDIST
HPLOT

- To display sampling distributions

SHIST
For a detailed description of each major function and its purpose, see the listing of $\operatorname{DESCRIBE}$.

This exercise is useful in a variety of courses, including those in operations research, production/operations management,
computer simulation, and those dealing with computer-based decision models. The flexibility of its use makes it appropriate for graduate or undergraduate courses.

It can also be used by students with a variety of backgrounds and capabilities in APL. The student who knows little or no APL will call the first function and respond to the questions and instructions given by the programs. A student with some APL knowledge may enter the required data input using the assignment operator, use calculator mode to do some preliminary calculations on EOQ, and execute each major function when needed. The fully knowledgeable APL user may write his own functions utilizing SIM to implement a search algorithm, or perform a sensitivity analysis.

Instructions for Use

Several types of data must be entered before running the system. See the listing of SETHOW for specific variable names and descriptions.

1. Cost Coefficients - (3 cost coefficients are required): order cost, carrying cost, and stockout cost. Note that the latter two are unit daily cost. Only positive numbers are acceptable.
2. Probability Distributions - (2 empirical probability distributions are required): one for daily demand and one for order lead time. These must be entered by using the function SET or the functions ENTDDIST and ENTLDIST (which are called by SET).
3. Initial conditions: beginning inventory and initial values for $Q$ and R. All three may be entered through $S E T$ or by the assignment operator directly. Only positive integers will be accepted.
4. Run length: a positive integer which can be entered using SET or by using the assignment operator. Only a positive integer is acceptable. The function SETRL allows the student to replicate simulation runs of a given length and display the sample of resultant average daily costs. This reveals the variability of response from a simulation with a short run length and allows the choice of appropriate length run. Note that the program will not accept more than 20 replications, or a run length of more than 250 days. Even these limits may be excessively expensive in CPU time on some APL installations.

After the required data are entered, the user begins the search for an optimum $Q$ and $R$ decision by executing the function SEARCH. This function accepts the value for $Q$ and R, calls SIM and returns the average daily cost of that run. The student must first identify the appropriate search region and decide whether to conduct a coarse search over a large area or a fine search over a smaller area. He may use a primitive search algorithm which iteratively scans a relevant range for $Q$ while $R$ is fixed, then increments $R$ and scans again over $Q$, etc. Alternatively, he may use a more sophisticated search algorithm such as the simplex technique described in Meier, et al. 1 The student may be encouraged

[^4]to use a Q, R grid to track the progress of his search.
If the student writes his own function to conduct the search, he may wish to use the simulation function SIM directly. It requires all the variables described above and calculates the average daily cost of a run. Total cost of each type is also available in global variables if needed (see below). For a further description of the logic of the simulation modeule, see a similar FORTRAN model in Schriber. ${ }^{2}$

Summary of Functions and Variables

The two following tables summarize the functions and the global variables in the INVASIM workspace.

FUNCTIONS

| FUNCTION NAME | PURPOSE | CALLED BY | CALLS |
| :--- | :--- | :--- | :--- |
| DESCRIBE | Gives basic description <br> of INV $\triangle S I M$ | SETHOW |  |
| DISTHOW | Gives instructions for <br> entering probability <br> distributions | SETHOW |  |
| ENTDDIST | Enters probability <br> distribution for <br> demand | SET | DISTHOW |

2. Schriber, Thomas J., Fortran Case Studies for Business Applications, John WiTey \& Sons, Inc., 1969, pp. 10-1 ff.

| FUNCTION NAME | PURPOSE | CALLED BY | CALLS |
| :---: | :---: | :---: | :---: |
| EfTLDIST | Enters probability distribution for lead time | SET | DISTHOW |
| $F R$ | Constructs frequency vector | HPLOT |  |
| HPLOT | Constructs scale for histogram of sampling distribution | SETRL | SHIST, VS |
| SEARCH | Permits iterative simulations with different Q, R |  | SIM |
| SET | Accepts input data |  | SETHOW, <br> ENTDDIST, <br> ENTLDIST, <br> SETRL |
| SETHOW | Gives input instructions for the use of $S E T$ | $\begin{aligned} & \text { DESCRIBE, } \\ & \text { SET } \end{aligned}$ | DISTHOW |
| SETRL | Replicates SIM with varying run length | SET | SIM, HPLOT |
| SHIST | Prints histogram of sampling distribution | HPLOT |  |
| SIM | Simulates the inventory system | SETRL, <br> SEARCH |  |
| VS,AND | Utilities used for plotting | HPLOT |  |
| $\begin{aligned} & A K I, A Y N, I N P, \\ & \triangle F I, \triangle F M T, \triangle V I \end{aligned}$ | Input/Output utilities |  |  |


| NAME | DESCRIPTION | INITIALIZED IN | USED IN |
| :---: | :---: | :---: | :---: |
| $A D C$ | Average Daily Cost | SIM | SEARCH, <br> SETRL |
| BINV | Beginning INVentory | SET | SIM |
| CAT | Number of CATegories in histogram | HPLOT | SHIST |
| $C C$ | Carrying Cost | SET | SIM |
| CO | Cost per Order | SET | SIM |
| $C S$ | Cost of Stockout | SET | STM |
| DDIST | Demand DISTribution as a 100 è lement vector | ENTDDIST | SIM |
| FLAG | A FLAG to fix scale of histogram during one session | SETRL, HPLOT | HPLOT |
| INC | INCrement of histogram scale | HPLOT |  |
| LDIST | Lead time DISTribution as a 100 element vector | ENTLDIST | SIM |
| MIN | MINimum range of the histogram scale | HPLOT |  |
| $Q$ | Order Quantity | SET | SIM |
| $R$ | Reorder point | SET | SIM |
| $R L$ | Run Length in days | SET, SETRL | SIM |
| $S$ | Vector of frequencies, S, for histogram | HPLOT | SHIST |
| SAMPLE | Vector of SAMPLE costs from replication of | SETRL | HPLOT |
| SCALE | SCALE for histogram | HPLOT | SHIST |
| TCC | Total Carrying Cost for 1 run | SIM |  |
| TCO | Total Cost of Order for 1 run | $S .1 M$ |  |
| TCS | Total Cost for Stockout for Trun | SIM |  |

## PROGRAM USAGE

SET
entry of parameters for inventory simulation DO YOU NEED INSTRUCTIONS?
YES OR NO N
ENTEF CARFYING COST PER INIT PFR PERIOD
? . 2
ENTER COST FEF ORDER PLACED
? 2.
ENTER STOCKOUT COST PEF UNIT PER EERIOD
? .75
enter beginning inventofy in units
? 15
ENTER PROBABILITY DISTRIEUTION FOR DEMAND
dO you need InSTructions on entering the pfobability DISTAIBUTION
? N
ENTEF D PD
? 08
ENTER D PD
? $1 \quad 13$
ENTER D PD
? 216
ENTEF D PD ? 320
ENTEF D PD
? 417
ENTEFD PD
? 511
ENTER D PD
? 69
ENTER D PD
? 76
ENTER D PD
? 00
DO YOU VISH TO DISPLAY THE DISTRIBUTION?
YES OR NO Y
$--\underline{D}_{-} \underbrace{8}_{--\underline{P}_{-}}$
$1 \mid 13$

| 2 | 16 |
| :--- | :--- |

3 | 20

| 4 | 17 |
| :--- | :--- |

5 | 11

| 5 | 9 |
| :--- | :--- |
| 7 | 6 |

SHALL WE GO ON?
YES OR NO Y
ENTEE PROBARILITY DISTRIBUTION FOF LEAD TIME
dO YOU NEFD INSTfUCTIONS ON ENTERING THE PFOBABILITY
DISTEIBJTION
? N
ENTEF LT P(LT)
? 30
ENTEF LT E (LT)
? 450

```
ENTER LT P(LT)
? 5 20
ENTER LT P(LT)
? 0 0
DO YOU WISH TO DISPLAY THE DISTRIBUTION?
YES OR NO Y
-LT
    4 1 50
    | | 20
SHALL WE GO ON?
YES OR NO Y
ENTER INITIAL VALUE FOR Q
? }1
ENTER INITIAL VALUE FOR R
? 13
DO YOU WANT TO EXPERIMENT IN ORDER TO DETERMINE THE
APPROFRIATE RUN LENGTH?
YES OR NO Y
ENTER TEST VALUE FOR RUN LENGTH IN PERIODS
? 20
HOW maNY RUNS OF that length do you WISH to try?
? }1
REPLICATION 1 AVG DAILY COST = 3.67
REPLICATION 2 AVG DAILY COST = 2.65
REPLICATION 3 AVG DAILY COST = 2.75
REPLICATION 4 AVG DAILY COST = 1.8375
REPLICATION 5 AVG DAILY COST = 2.0275
REPLICATION 6 AVG DAILY COST = 2.09
REPLICATION 7 AVG DAILY COST = 2.3
REPLICATION 8 AVG DAILY COST = 2.305
REPLICATION 9 AVG DAILY COST = 2.7725
REPLICATION 10 AVG DAILY COST = 2.6825
REPLICATION 11 AVG DAILY COST = 2.09
REPLICATION 12 AVG DAILY COST = 2.2075
REPLICATION 13 AVG DAILY COST = 2.7925
REPLICATION 14 AVG DAILY COST = 2.6275
REPLICATION 15 AVG DAILY COST = 2.73
SAMPLE MEAN = 2.502166667
SAMPLE STD = 0.4380295525
WOULD YOU LIKE TO SEE A PLOT OF THIS SAMPLING DISTRIBUTION? Y
```

```
    O.5:
OO YOJ VISH TO TRY ANOTHER FUN LENGTH? Y
ENTER TEST VALUE FOR RUN LENGTH IN PEFIODS
? 50
HON MANY RUNS OF THAT LENGTH DO YOU WISH TO TRY?
? 15
REELICATION 1 AVG DAILY COST = 2.459
REPLICATION 2 AVG DAILY COST = 2.428
REPLICATION 3 AVG DAILY COST = 2.141
REPLICATION 4 AVG DAILY COST = 2.644
REPLICATION 5 AVG DAILY COST = 2.386
REFLICATION 6 AVG DAILY COST = 2.354
REPLICATION 7 AVG DAILY COST = 2.047
FEPLICATION 8 AVG DAILY COST = 2.3
REPLICATION 9 AVG DAILY COST = 2.28?
REPLICATION 10 AVG DAILY COST = 2.302
REFLICATION 11 AVG DAILY COST = 2.303
REFLICATION 12 AVG DAILY COST = 2.379
REPLICATION 13 AVG DAILY COST = 2.429
REPLICATION 14 AVG DAILY COST = 2.781
REPLICATION 15 AVG DAILY COST = 2.157
SAMPLE MEAN = 2.365466667
SAMPLE STD = 0.1786959677
WOULD YOI LIKE TO SEE A PLOT OF THIS SAMPLING DISTRIBUTION? Y
```

```
    10.01
    \:OM
DO yOU WISH TO TRY ANOTHER RUN LENGTH? N
ENTER LENGTH OF EACH RUN IN PERIODS
? }4
PARAMETER ENTRY COMPLETE. WOULD YOU LIKE TO REVIEW THE VALDES?
? Y
CO}=
CC=0.2
CS = 0.75
BINV = 15
Q=15
R=13
RL=40
DO YOU WANT TO PROCEED WITH THE SIMULATION?
IF SO, ENTER SEARCH, OTHERWISE RESTART PARAMETER SETTING process
BY ENTERING SET
```


## PROGRAM DESCRIPTION

[1] [2]
[3] ,
[4] , THIS SET OF APL FUNCTIONS ALLOWS THE USER TO SEARCH FOR OPTIMUM.
[5] 'VALUES OF ORDER QUANTTTY (Q) AND REORDER POINT (R) IN A STOCHASTIC'
[6] 'Inventory system. after entering cost coefficients, probability'
[7] 'DISTRIBUTIONS, AND SIMULATION RUN PARAMETERS, THE USEF CONDUCTS AN'
[8] 'INTERACTIVE SEARCH FOR THE OPTIMUM $Q R$ PAIR. the PRIMARY FUNCtions ARE'
[9] 'DESCRIBED BELOW.'
[10] '
[11] 'SET.
[12] $\quad$ •
[13] ' This program allows the user to enter the data for the simulation'
[14] 'RUN. SPECIFICALLY IT:'
[15] '
[16] 1 1. ACCEPTS VALUES FOR UNIT CARRYING COST, UNIT STOCKOUT COST.' [17] , ORDER COST, AND BEGINNING INVENTORY.'
[18] , 2. CALLS TWO EUNCTIONS (ENTDDIST AND ENTLDIST) TO ENTER AND SHAPE'
[19] , THE PROBABILITY DISTRIBUTIONS FOR DEMAND AND LEAD TIME.'
$[20]$ '
3. ALLOWS THE USER TO CALL A SEPARATE FUNCTION (SETRL--SEE BELOW)' TO HELP DETERMINE THE APPROPRIATE LENGTH OF EACH SIMULATION RUN.'
[22] ' '
[23] 'SETRL'
[24] ,
[25] , THIS PROGRAM ALLOWS THE USER TO EXPERIMENT WITH SEVERAL VALUES FOR'
[26] 'THE RUN LENGTH OF THE SIMULATION. SPECIFICALLY, IT PERFORMS SEVERAL'
[27] 'runs of a given length and displays the resultant average daily cost'
[28] ' FOR EACH RUN. ~HE USER MAY DISPLAY THE COST FOR EACH SET OF',
[29] 'REPLICATIONS AS A EREQUENCY HISTOGRAM.'
[30] $\quad$ "
[31] 'SEARCH'
[32] '
[33] , THIS PROGRAM ALLOWS THE USER TO ALTER THE VALUES OF Q AND R AND, [34] 'PERFORM REPEATED SIMULLATION RUNS. THE VALUE FOR AVERAGE DAILY COST IS'
[35] 'DISPLAYED AFTER EACH ITERATION.'
[36] '.
[37] 'SIM'
[38]
[39] ' THIS PROGRAM IS CALLED BY SETRL AND SEARCH TO PRODUCE THE AVERAGE,
[40] 'DAILY COST FOR A SINGLE SIMULAT $\overline{I O N R U N}, \widehat{A L L T H E ~ C O S T ~ C O E F F I C I E N T S, ' ~}$
[41] 'PROBABILITY DISTRIbutions,and RUN PARAMETERS must be defined in advance.'
[42] "
[43] 'ENTDDIST AND ENTLDIST'
[44] "
[45] .

```
    - these programs accept values of an empirical probabilitye
```

[46] 'DISTRIBUTION FOR DEMAND AND LEAD TIME. SEE ADDITIONAL INSTRUCIONS BELOW' $\nabla$

```
    \nabla SETRL;REPL;COUNT;SM;STD
[1] aREPLCATES THE INVENTORY SIMULATION TO DEVELOP
[2J aA SAMPLING DISTRIBUTION OF AVERAGE COST. CALLS
[3] ^HPLOT ON USER OPTION TO DISPLAY HISTOGRAM OF
[4] RSAMPLE MEANS. REQUIRES THE PUBLIC FUNCTIONS AYN
[5] AAND INF.
        FLAG<0
    start:'enter test value for run length in periods'
        RL+1 INP '?'
    [9] +(RL>250)/ERR1
    [11] REPL+1 INP '?'
    [12] }->(REPL>20)/ERR
    [13] COUNT+0
    [14] SAMPLE+10
    [15] LOOP:SIM
    [16] COUNT+COUNT+1
    [17J 'REPLICATION ';COUNT;' AVG DAILY COST = ;ADC
    [18] SAMPLE+SAMPLE,ADC
    [19] }->(REPL>COUNT)/LOO
    [20] SM+(+/SAMPLE)\div\rhoSAMPLE
    [21] 'SAMPLE MEAN = ;SM
    [22] STD +((\div(\rhoSAMPLE-1))*(+/(SM-SAMPLE)*2))*0.5
    [23] SAMPLE STD = ; STD
    [24] YNT&AYN 'WOULD YOU LIKE TO SEE A PLOT OF THIS SAMPLING DISTRIBUTION?'
    [25] }->(YNT=0)/P
    [26] HPLOT
    [27] P2:YNT+AYN 'DO YOU WISH TO TRY ANOTHER RUN LENGTH?'
    [28j }->(YNT=1)/STAR
    [29] }->
    [30] ERR1:'that''S TOO LONG A RUN. CHOOSE A NUMBER<250'
    [31] ->START
    [32] ERR2:'THAT''S TOO MANY REPLICATIONS. 20 OR LESS SHOULD BE SUFFICIENT'
    [33] }->P
    \nabla
    \nabla SIM;INV;ORDQ;DAYS;LT
    [1] athIS FUNCTION IS CALLED BY SEARCH AND SETRL TO GENEFATE
    [2] aAN AVERAGE DAILY COST FOR A SINGLE SIMULATION fUN OF
    [3] ATHE INVENTORY SYSTEM.
    [4] DAYS+TCO+TCC +TCS+0
    [5] INV + BINV
    [6] A INITIALIZE ORDER QUEUE
    [7] ORDQ+(\Gamma/LDIST)\rho0
    [8] CYCLE:+(RL<DAYS+DAYS+1)/END
    [9] AADD INCOMING ORDER TO INVENTORY
    [10] INV+INV+(1\uparrowOKDG)
    [11] & SHIFT ORDER QUEUE
    [12] ORDQ+(1+ORDQ),0
    [13] a SUBTRACT DAILY DEMAND FROM INVENTOFY
    [14] INV+INV-DDIST[?100]
    [15] a PLACE ORDER IE INVENTOFY + COMING OKDERS < R
    [16] }->(R<+/INV,ORDQ)/O
    [17] a PLACE ORDER, UPDATE ORDER OUEUE AND TOTAL ORDEF COST
    [18] LT +LDIST[?100]
    [19] ORDQ[LT] +ORDQ[LT]+Q
    [20] TCO+TCO+CO
    [.21] a UPDATE CARRYING COST OF STOCKOUT COST
    [22] ON:->((INV=0),(INV>O))/CYCLE,GT
    [23] ->CYCLE,TCS-TCS+CSX-INV
[24] GT: +CYCLE,TCC+TCC+CC\timesINV
[25] a CALCULATE AVERAGE DAILY COST
[26] END:ADC++/(TCS,TCO,TCC)\divRL
    \nabla
```

```
    \nabla HPLOT; FANGE
「17 aACCEPTS SAMPLE OF COST MEANS FFOM SETRL, SETS A SCALE,
[2] aCONSTFICTS A FREQUENCY DISTRIBUTION, AND CALLS SHIST
[3] aTO PRINm a HISTOGFAM. ELAG IS SET TO
[4] aUSE THE SAME SCALE FOF ALL RUNS OF A
[s] aSINGLE SESSION. EEQUIFES THE IISE OF THE
[6] aPUELIC FUNCTION VS.
[7] }->(FLAG=1)/PI
[8] ELAG+1
[9] RANGE+(「/SAMPLE)-L/SAMPLE
[10] MIN+(L/SAMPLE)-0.25*RANGE
[11] CAT+(\rhoSAMPLE)\div3
[12] }->(CAT<6)/EORC
[13] }->(CAT\geq15)/FORCE
[14] SETINC:INC+FANGE:CAT
[15] SCALE+(INC*)
[16] PL:S+(MIN,INC,CAT) ER SAMFLE
[17] S*S,((pSCALE)-\rhoS)\rho0
[18] 20 40 SHIST S VS SCALE
[19] }->
[20] FOFCE:CAT+6
[21] ->SETINC
[22] FOFCE2:CAT+15
[23] ->SETINC
    \nabla
    \nabla SEAFCH;T
[1] aACCEPTS A valuE FOF Q AND F, CALLS SIM
[2] aTOO EETURN THF AVEFAGE DAILY COST. ISSED TO ITEFATIVELY
[.3] ASFARCH FOF THE OFTIMUM VALUES OF Q AND K.
[4] afEQUIFES THE PUBLIC FUNCTIONS AYN AND INP
[5] T+10
[6] 'HAVE YOU ENTEFED ALL THE NECESSAEY DATA?'
[7] YNT*AYN '?'
[8] }->(YNT=1)/GO
[9] 'PLEASE ENmFR DATA. TYPE DESCRIBE FOR INSTRUCTIONS'
[10] ->0
[11] GO1:'INITIAL VALUES FOK Q AND R ARE;'
[12] ' Q= ';Q;', R= ';R
[13] 'SHALL WE FROCEED?'
[14] YNT+AYN '?'
[15] ->(YNT=1)/LOOP
[16] END:'DONE'
[17] ->0
[18] LOOP:SIM
[19] 'AVERAGE DAILY COST = ';ADC
[20] ' '
[21] 'ENTER Q E'
[22] T+2 INF '?'
[23] }->(\wedge/T=0)/EN
[24] 0+14T
[25] F*-1+T
[25] ->LOOP
\27] ->
    \nabla
```

$\nabla$ SET

```
[1] aIT PERUIFES THE FOLLOWING USEF-DEFINED FUNCTIONS:
[2] aENTDDIST, ENTLDIST, SETHOH, SFTRL. ALSO FEQUIFED AFE THE
[3] apUELIC fUNCTIONS AYN AND IPI.
[4] aTHIS EUNCTION ACCRETS USER INFUT TOO SET VALUES EOF THE SIMULATION
[5] aRUN.
[6] 'entey of pafametefs fof inventoky simulation'
[7] 'DO YOU NEED INSTRUCTIONS?
[8] YNT+AYN YES OF NO'
[9] }->(YNT=0)/PFOCEED
[10] SETHOW
[11] PROCEED1:'enter Carbying cost per uNIt eef fefiod'
[12] CC+1 IND '?'
[13] 'ENTEK COST FEF OFDER PLIACFD'
[14] CO+1 INE '?'
[15] 'ENTEE STOCKOUT COST PEF UMIT PER FERIOD'
[16] CS+1 INP '?'
[17] 'ENTER EEGINNING INVENTOEY IN UNITS'
[18] BINV+1 INE '?'
[19] 'ENTEF PROBABILITY DISTrifUTION FOF DEMAND'
[20] ENTDDIST
[21] 'ENTER FROBABILITY DISTRIFIJTON FOF LEAD TIME'
[22] ENTLDIST
[23] PROCEED2:'ENTER INITIAL VALUE FOFQ '
[24] 0+1 INP '?'
[25] 'ENTER INITIAL VAI|IE EOF F '
[26] R+1 INF '?'
[27] 'DO YOU WANT TO EXPERIMENT IN OFDER TO DETEFMINE THE '
[28] 'AFPFOPRIATE RUN LENGTH?'
[29] YNT+AYN YYES OR NO'
[30] ->(YNT=0)/PROCEED3
[31] SETFL
[32] PROCEED3:'ENTER LENGTH OF EACH RUN IN PEFIODS'
[33] FL+1 INP '?'
[34] 'PARAMETER ENTRY COMPLETE. WOULD YOU LIKE TO FEVIEW THE VALUES?'
[35] YNT&AYN '? '
[36] }->(YNT=0)/PFOCEED
[37] 'CO = ';CO
[38] 'CC = ';}C
[39] 'CS = ';CS
[40] 'BINV = ';EINV
[41] 1Q = ':0
[42] 'F= ';
[43] 'RL= ';RL
[.44] FROCEED4:'DO YOU WANT TO EROCEED WITH THE SIMDLATION?'
[45] 'IF SO, ENTER SEARCH, OTHERWISE RESTART PARAMETER SETTING PROCESS'
[46] 'BY ENTERING SET'
    \nabla
```

| [1] | SETHOW |
| :---: | :---: |
| [2] | INPUT INSTRUCTIONS' |
| [3] | ', |
| [4] | 'the following data must be entered for the inventory simulation.' |
| [5] | '' |
| [6] | 'DATA NAME DESCRIPTION' $^{\prime}$ |
| [7] |  |
| [ 8 ] | '' ${ }^{\prime}$ ( ${ }^{\text {a }}$ |
| [9] | CO ORDER COST: THE COST OF PLACING AN ORDER' |
| [10] |  |
| [11] | $C C$ CARRYING COST: THE COST OF CARRYING ONE UNIT OF' |
| [12] | INVENTORY FOR ONE DAY' |
| [13] | '' ${ }^{\prime}$ ( ${ }^{\text {a }}$ |
| [14] | Cs Stockout cost: the cost of back ordering one unit' |
| [15] | FOR ONE DAY' |
| [16] | "' ${ }^{\prime \prime}$ |
| [17] | BINV BEGINNING INVENTORY: THE NUMBER OF UNTTS IN' |
| [18] | INVENTORY At the beginning of each simulation run' |
| [19] | ', ${ }^{\prime}$ |
| [20] | Q QUANTITY ORDERED: THE NUMBER OF UNITS TO BE' |
| [21] | ORDERED EACH TIME AN ORDER IS PLACED' |
| [22] | ', ${ }^{\prime}$ |
| [23] | $R$ REORDER FOINT: THE STOCK LEVEL AT WHICH ORDER |
| [24] | PLACEMENT IS TRIGGERED' |
| [25] | '' ${ }^{\text {' }}$ |
| [26] | RL RUN LENGTH: THE NUMBER OF PERIODS IN EACH' |
| [27] | SIMULATION RUN' |
| [28] | '' |
| [29] | - DDISt THE PROBABILITY DIStribution for demand' |
| [30] | '' |
| [31] | , LDIST THE PROBABILItY DIStribution for lead time' |
| [32] | '' |
| [33] | all the data can be entered by typing 'sset' and answering the |
| [34] | ' QUESTIONS. ENTER only NUMERIC data. to interupt a run, hit the |
| [35] | 'ATTENTION KEY,TYPE THE RIGHT ARROW $\left(\rightarrow\right.$ OR ENTER O BACKSPACE U, ${ }^{\prime}$ |
| [36] | 'BACKSPACE T, AND START AGAIN.' |
| [37] | '' |
| [38] | As an alternative to using set, all the data items (except the' |
| [39] | ' PRobability distributions) Can be Entered or Changed by using the apl' |
| [40] | ' ASSIGNMENT OPERATOR (FOR INSTANCE CO+2.25). TO ENTER THE PROBABILITY', |
| [41] | ' Distributions (WITHOUT USING the ' 'set'" funcilon) type entddist and |
| [42] | - ENTLDIST FOR DEMAND AND LEAD TIME DISTRIBUTIONS RESPECTIVELY AND |
| [43] | 'FOLLOW the instructions given below. after the data and distributions' |
| [44] | 'HAVE BEEN ENTERED, TYPE SETRL TO DETERMINE the appropriate run length. |
| [45] | 'FINALLY, TYPE SEARCH TO INTERACTIVELY SEARCH FOR THE OPTIMUM Q AND R.' |
|  |  |

```
\nabla DISTHOW
[1]
[2]
[3]
[4]
[5]
[6]
[7]
[8]
[9]
[10]
[11] ,
[12] ''
[13] 'IN RESPONSE TO THE PROMPT ''ENTEF D PD'', TYPE ONE DEMAND FIGURE AND '
[14] 'ITS PROBABILITY IN WHOLE PEFCENTAGE FORM (WITHOUT DECIMAL, TWO DIGITS'
[15] 'MAXIMUM) WITH A SPACE IN BETWEEN. FOR EXAMPLE:'
[16] ''
[17] ' ENTER D PD'
[18] , 0 25.
[19] ' ENTER D PD'
[20] , 1 50'
[21] ' ENTER D PD'
22] ' 2 25'
[23] ' ENTER D PD'
[24] , 0 0'
[25] ',
[26] 'AFTER THE LAST ENTRY HAS BEEN MADE, ENTER O o TO EXIT.'
    \nabla
    \nabla ENTDDIST;IN;T
[1] aREQUIRES THE PUBLIC FUNCTIONS AYN, \triangleFMT,
[2] PAND INP.
[3] faCCEPTS PROBABILITY DISTRIBUTION FOR DEMAND AND
[4] ACONSTRUCTS A 100 ELEMENT VECTOR FOR RANDOMLY
[5] agENERATING DEMAND IN SIMULATION.
[6] 'DO YOU NEED INSTRUCTIONS ON ENTERING THE PROBABILITY'
[7] 'DISTRIBUTION'
[8] YNT*AYN '?'
[9] ->((YNT=1),YNT=0)/OUT,START
[10] OUT:DISTHOW
[11] START:DDIST*10
[12] IN+10
[13] LOOP:'ENTER D PD'
[14] T+2 INP '?'
[15] +(^/T=0)/TEST
[16] IN+IN,T
[17] DDIST+DDIST,(` - 1+T) \rho1+T
[18] +LOOP
[19] TEST: +((\rhoDDIST)\not=100)/ERR
[20] 'DO YOU WISH TO DISPLAY THE DISTRIBUTION? '
[21] YNT+AYN 'YES OR NO'
[22] }->(YNT=0)/
[23] IN+(((\rhoIN):2),2)\rhoIN
[24] , D | PD ;
[25] 'T I,ए \ प,I5' \triangleFMT IN
[26] 'SHALL WE GO ON?'
[27] YNT+AYN 'YES OR NO.
[28] }->(YNT=1)/
[29] OK, START OVER.
[30] +START
[31] ERK:'PKOBABILITY PERCENTAGES DO NOT ADD TO 100, START OVEF'
[32] ->START
    \nabla
```

```
    \nabla ENTLDIST;IN;T
[1] aREQUIRES THE PUBLIC FUNCTIONS AYN, \triangleFMT,
[2] คAND INP.
[3] aACCEPTS Probability distribution for LOAD tIme aND
[4] aCONSTRUCTS A 100 ELEMENT VECTOR FOR RANDOMLY
[5] aGENERATING LOAD TIME IN THE SIMULATION.
[6] 'DO YOU NEED INSTRUCTIONS ON ENTERING THE PROBABILITY'
[7] 'DISTRIBUTION'
[8] YNT&AYN '?'
[9] }->((YNT=1),YNT=0)/OUT,STAR
[10] OUT:DISTHOW
[11] START:LDIST+10
[12] IN+10
[13] LOOP:'ENTEK LT P(LT)'
[14] T+2 INP '?'
[15] }->(\wedge/T=0)/TES
[16] IN+IN,T
[17] LDIST+LDIST,(` - +T T) \rho1\uparrowT
[18] ->LOOP
[19] TEST: +((\rhoLDIST)\not=100)/ERR
[20] 'DO YOU WISH TO DISPLAY THE DISTRIBUTION? '
[21] YNT+AYN YES OR NO'
[22] }->(YNT=0)/
[23] IN*(((\rhoIN)\div2),2)\rhoIN
[24] ' LT \PLT ;
[25] , I4,D \ D,I5 \triangleFMT IN
[26] 'SHALL WE GO ON?'
[27] YNT+AYN 'YES OR NO'
[28] }->(YNT=1)/
[29] 'OK, START OVER'
[30] +START
[31] ERR:'PROBABILITY PERCENTAGES DO NOT ADD TO 100, START OVER'
[32] ->START
\nabla
```

FINANCIAL RATIO CALCULATIONS<br>Wilma D. Stricklin<br>Professor of Management<br>College of Business Administration Northern Arizona University Flagstaff, Arizona

DESCRIPTION

This program performs a number of ratio calculations which are typically used to gauge the financial effectiveness of an organization. These ratios are:

| Net Income Total Assets | Return on investment as a function of assets |
| :---: | :---: |
| Net Income | Return on investment as a function |
| Total Common Equity | of equity |
| Net Income | Earnings per share |
| Number of Shares | Earnings per share |
| Net Income <br> Total Sales | Profits as a function of sales |
| Long Term Debt | Long term debt as a function of |
| Total Assets | assets |
| $\frac{\text { Total Sales }}{\text { Toal Assets }}$ | - Sales as a function of assets |

The program is initiated by typing EFFRATIO and then following the instructions given. Any number of years' worth of data can be entered; but, beyond five, the data inputting can be tedious and error prone.

In the sample shown in the following section, the data were taken from the Boise-Cascade Case found in Robert L. Katz, Cases and Concepts in Corporate Strategy, Englewood Cliffs, N. J.: Prentice-Hall, 1970.

## PROGRAM USAGE

```
    EFEFATIO
OBSEFVE THE EOLLOWING INSTRUCTIONS IN ENTFRING DATA:
    A. ROUND YOUF DATA TO THE NEAREST THOUSAND DOLLARS,
    B. ENTEF O(ZEFO) IN EACH INSTANCE WHERE DATA IS |NKNOWN OF UNAVAIIABLE,
    C. USE THE - SIGN (OVFE THF 2-KEY) TO MARK NEGATIVE NUMBEFS,
    D. DO NOT USE COMMAS TO SEPARATE NUMBERS.
```

```
ENTER YEARS FOF WHICH YOU HAVE DATA: 1962 1963 1954 1965 1966
```

ENTER YEARS FOF WHICH YOU HAVE DATA: 1962 1963 1954 1965 1966
ENTER TOTAI ASSETS FOF EACH YEAR:
ENTER TOTAI ASSETS FOF EACH YEAR:
\Pi:
\Pi:
124382 130456 293475 370522 454250
124382 130456 293475 370522 454250
ENTEF NET INCOME AFTER TAXES EOF EACH YEAR:
ENTEF NET INCOME AFTER TAXES EOF EACH YEAR:
\square:
\square:
5055 7390 14947 17898 17014
5055 7390 14947 17898 17014
ENTER TOTAL LONG TERM DEET FOR EACH YEAR
ENTER TOTAL LONG TERM DEET FOR EACH YEAR
\Gamma:
\Gamma:
71548 63815 117127 156921 193909
71548 63815 117127 156921 193909
ENTER TOTAL COMMON EOUITY FOF EACH YEAR:
ENTER TOTAL COMMON EOUITY FOF EACH YEAR:
П:
П:
52834 64653
52834 64653
LENGTH ERFOR...FEENTER 5 VALUES.
LENGTH ERFOR...FEENTER 5 VALUES.
\:
\:
52834 64663 166496 172251 192751
52834 64663 166496 172251 192751
ENTER TOTAL SHARES OF GOMMON STOCK FOF EACH YEAR:
ENTER TOTAL SHARES OF GOMMON STOCK FOF EACH YEAR:
\square:
\square:
374140014487 4375 9005
374140014487 4375 9005
ENTEF TOTAL SALES FOR EACH YEAR:
ENTEF TOTAL SALES FOR EACH YEAR:
_:
_:
176015 219361 363581 422911442466
176015 219361 363581 422911442466
ENTEF HEADING FOR YOUR REPORT: BOISE CASCADE COFP.
ENTEF HEADING FOR YOUR REPORT: BOISE CASCADE COFP.
EFFECTIVENESS RATIOS--BOISE CASCADE COFP.
EFFECTIVENESS RATIOS--BOISE CASCADE COFP.
YEAR ROI-A ROI-EQ EPS PFOE/SLS DT/ASSET SLS/ASSET
YEAR ROI-A ROI-EQ EPS PFOE/SLS DT/ASSET SLS/ASSET
1962 0.0406 0.0957 1.3512 0.0287 0.5752 1.4151
1962 0.0406 0.0957 1.3512 0.0287 0.5752 1.4151
1063 0.0566 0.1143 1.8470 0.0337 0.4892 1.6815
1063 0.0566 0.1143 1.8470 0.0337 0.4892 1.6815
1964 0.0509 0.0898
1964 0.0509 0.0898
1965 0.0483 0.1038
1965 0.0483 0.1038
1966 0.0375 0.0883 1.0.8894 1.0.0.0345 0.0.4269 1.0841
1966 0.0375 0.0883 1.0.8894 1.0.0.0345 0.0.4269 1.0841
DO YOU WISH TO CONTINUE? NO

```
DO YOU WISH TO CONTINUE? NO
```


## PROGRAM DESCRIPTION

```
    \nabla EFFRATIO;N;M;YRS;TA;NP;LTD;CE;CMS;SA;CO
[1] aTHE FOLLOWING PURLIC FUNCTIONS ARE REQUIRED IN ORDER
[2] aTO USE THIS PROGRAM: AKI, CENTER, COLNAMES, \triangleFMT, INP,
[3] AAND IPI.
[4] a THE FOLLOWING LINES GIVE THE USER INSTRUCTIONS ON INPUT RESTRICTIONS.
[5] a//////////////////
[^] 'OBSERVE THE FOLLOWING INSTRUCTIONS IN ENTERTNG DATA:'
[7] : A. ROUND YOUR DATA TO THE NEAREST THOUSAND DOLLARS,'
    B. FNTER O(ZERO) IN EACH INSTANCE WHERE DATA IS UNKNOWN OR UNAV,
    AILABLE,'
[9] ' C. USETHE ' SIGN (OVER THE 2-KEY) TO MARK NEGATIVE NUMBERS,'
[10] ' D. DO NOT USE COMMAS TO SEPARATE NUMBERS.'
[11] ' '
[12] , ,
[13] TOP:N&OYRS+IPI 'ENTER YEARS FOR WHICH YOU HAVE DATA:'
[14] ATHIS SECTION ACCEPT INPUT, TESTS EACH SET EOR ACCURACY OF NUMBER OF INPUT',
        S, AND CYCLES FOR CORRECT DATA.
        'ENTER TOTAL ASSETS FOR EACH YEAR:'
[16] TA&INP N
[17] 'ENTER NET INCOME AFTER TAXES FOR EACH YEAR:'
[18] NI&INP N
[19] 'ENTEF TOTAL LONG TERM DEBT FOP EACH YEAR'
[20] LTD<INP N
[21] 'ENTER TOTAL COMMON EQUITY EOR EACH YEAF:'
[2?] CE+INP N
[23] 'ENTER TOTAL SHAEES OE COMMON STOCK FOR EACH YEAR:'
[24] CMS+INP N
[25] 'ENTER TOTAL SALES FOR EACH YEAR:'
[26] SA+INP N
[27] aTHIS CREATES A MATRIX OF RATIOS RESULTING FROM A DIVISION OF VECTORS.
[28] CO\leftarrow(6,N)\rho(NI,NI,NI,NI,LTD,SA)\div(TA,CE,CMS,SA,TA,TA)
[29] aTHIS ESTABLISHES REPORT FORMAT.
[30] TITLE&AKI 'ENTER HEADING EOR YOUR REPORT:'
[31] FORMAT&'I5,6F10.4'
[32] FORMAT CENTER 'EFFECTIVENESS RATIOS-.-',TITLE
[33] FORMAT COLNAMES 'XYEARXROI-AXROI-EQXEPSXPROE/SLSXDT/ASSETXSLS/ASSETX'
[34] FORMAT \triangleFMT(YRS;QCO)
[35] ~THIS PERMITS THE USER TO REPEAT THE PROGRAM FOF ANOTHER SET OF DATA, FOR
        A COMPETITOR, FOR THE INDUSTRY, ETC.
[3К] }->(AYN 'DO YOU'WISH TO CONTINUE?')/TO
\nabla
```

COMPUTATION OF A PRICE INDEX
BY THE METHOD OF THE WEIGHTED GEOMETRIC MEAN

Bernard A. Thielges<br>Assistant Professor<br>Management Department<br>College of Business Administration<br>Marquette University<br>Milwaukee, Wisconsin

## DESCRIPTION

## Statement of the Problem

The computation of a price index can be done by various averaging techniques. The arithmetic mean, however, is the average most often used because of its simplicity and ease in calculation. Various weighting methods can also be used with the arithmetic mean, but the one most often used is the method which uses the base year values as the weights.

The method of the arithmetic mean together with base year values as weights provides a good index. There are deficiencies, however. It is known that there is an upward bias to the arithmetic mean. On the other hand, the use of base year values as weights provides a downward bias by giving too much weight to those items having the smallest change in price. At times, one bias may tend to offset the other; but in other instances, this will not be the case.

In order to compute a price index which is consistently more accurate, the geometric mean, which is an unbiased mean, might be used. And, to provide for a more appropriate weighting system, it is suggested that the average of the values computed for all years, from the base year to the current year, be used. The computation of the price index by this method is considerably longer and more sophisticated. However, the initial computation and subsequent
updating are readily facilitated through the use of the computer.

## Program Description

The program PINDEX computes a price index for selected items. The index is computed for the final year of data submitted, using the first year as the base year. The formula used in the computation is

$$
\text { Price Index }=\frac{\sum w\left(\log \frac{p_{1}}{p_{0}}\right)}{\Sigma w}
$$

where, w (Average value of all $\begin{gathered}\text { years for each item } \\ \text { in the index) }\end{gathered}$

$$
\begin{aligned}
& p_{\mathbf{i}}=\text { price for the } i \text { th year of data } \\
& q_{\mathbf{i}}=\text { quantity for the } i \text { th year of data } \\
& p_{1}=\text { price for the last year of data submitted } \\
& p_{0}=\text { price for the first (base) year of data submitted } \\
& N=\text { number of years for which data is submitted. }
\end{aligned}
$$

To begin the computation, the data must be entered in the following fashion. First, the years for which data are to be submitted are entered, i.e., 19711972 1973, and 1974. These data on years are needed for labeling the table in the print-out. The number of items to be included in the index is entered as a numberal followed by the individual item names when asked for by the program. Item names should not exceed 16 characters in length, should be only one word (compound words can be hyphenated or run together), and should be separated by blanks (do not use commas).

Quantity data is then entered by year for all items, followed by price data by year for all items. These entries constitute the quantity and price matrices. Data are entered for all items by year and appear as shown in the sample. The program puts the data in proper matrix form for calculations.

Internal computation of the index starts with the calculation of the ratio between the final year price data and the first year price data. The first year of data is therefore the base year. The logarithm to the base 10 of this ratio is then determined.

The weight to be used is calculated by first multiplying the price matrix by the quantity matrix and obtaining a value matrix. This matrix lists the value of each individual item in the index by years. The average value for each specific item is calculated by summing each year'svalue and then dividing by the number of years. The resultant average is used as the weight.

Next, the logarithm of the price ratio for each item is multipied by its weight. This weighted value is summed for all items and divided by the sum of the weights, i.e., the sum of the average values for all of the years for all of the items. The final computation of the price index is made by finding the antilog of the weighted data.

The print-out of data includes a repeat of the price and quantity matrix as well as the final price index as a percent. The user should be aware that if data for many years are submitted or if the data are fairly large, then the available space might not be sufficient to print out the price and quantity matrices. In this case, an asterisk will appear wherever there is insufficient space in the print-out.

```
    PINDEX
ENTER THE YEARS FOR WHICH THE INDEX IS TO BE COMPUTED, EG, 1973 1974 1975
\square:
    1973 1974 1975
enter the Number of items to be INCLUded IN the priCe indeX, eG, 6
\square:
    6
enter the names of the items to be included in the price index, eg,
LUMBER CEMENT NAILS ASPHALTSHINGLES. NOTE THAT ANY ITEM CONTAINING
TWO OR MORE WORDS IS TO BE JOINED TOGETHER TO MAKE ONE WORD. NO ITEM
SHOULD EXCEED SIXTEEN CHARACTERS IN LENGTH.
CORN WHEAT OATS BARLEY RYE RICE
ENTER dATA FOR THE PRODUCTION MATRIX, EG, QUANTITIES OF EACH ITEM SOLD, FOR
    1973
\square:
    4084 1316 927 392 33 76
ENTER dATA FOR THE froduction matrix, EG, Quantities of each item sold, FOR
\square:
    4760 1522 789 373 24 89
ENTER DATA FOR the production matrix, eg, quantities of each item sold, for
    1975
[:
    4375 1570 930
INCORRECT NUMBER OF ITENS. TRY AGAIN
I:
    4375 1570 930 418 23 105
enter data for the price matrix,eg, prices of each Item, for 1973
\square:
    1.16 1.35 . }62 1.03 . 97 4.93
ENTER DATA FOR THE PRICE MATRIX,EG, PRICES OF EACH ITEM, FOR 1974
\square:
    1.04 1.39 ..66 1.00 1.07 4.97
enter data for the price matrix,eg, prICEs of each ITEM, FOR 1975
\square:
    1.05 1.22 . 59 . 88 . 99 5
```

PRODUCTION DATA

ITEM

CORN
WHEAT
OATS
BARLEY
RYE
RICE

PRICE DATA
ITEM
CORN
WHEAT
OATS

VALUE DATA
ITEM
COKN
WHEAT
OATS
B.ARLEY

RYE
RIC E
$4,084.00$
$1,316.00$
927.00
392.00
33.00
76.00

BARLEY
RYE
KICE

197
1.1

1. 35
0.62
1.03
0.97
4.93

1973
1974
4,760.00 1,522.00 789.00 373.00 24.00 89.00
1974
1.04
1.39 0.66 1.00 1.07 4.97

1974
4,950.40
2,115.58
520.74
373.00
25.68
442.33

1975
4,375.00
1,570.00 930.00 418.00 23.00 105.00

1975
1.05

1. 22
0.59
0.88
0.99
5.00

1975
4.593 .75

1,915.40 548.70 367.84 22.77 525.00

## PROGRAM DESCRIPTION

```
    \(\nabla\) PINDEX:R
[1] APREPARED BY:
[2] aBERNARD A. THIELGES
[3] adSSISTANT PROEESSOR OF MANAGEMENT
[4] ACOLLEGE OF BUSINESS ADMINISTRATION
[5] MMARQUETTE UNIVERSITY
[6] AMILWAUKEE, WISCONSIN 53233
[7] a this program computes a price index by the method of the weighted
[8] aGEOMETRIC MEAN.
[9] AINPUT: PRICE AND QUANTITY DATA FOR 'N' YEARS. TOTE THAT BOTH ITEMS
[10] aARE ENTERED AS ROW VECTORS. ITEM NAMES ARE TRANSPOSED AS NECESSARY INTO
    \(A\)
[11] a COLUMN MATRIX FOR DATA PRINTOUT.
[12] athe price ratios for all items included in data are computed with the
[13] aLASt year of data referenced to the first year of data as base year.
[14] athe price rations are weighted by the average of all of the years value
[15] aOF THE ITEM FROM THE FIRST YEAF THROUGH THE LAST YEAR OF THE DATA
[16] ASUBMITTED. THE GEOMETRIC MEAN OF THE WEIGHTED PRICE FATIOS IS THEN
[17] acomputed. this weighted price ratio is then divided by the sum of the
[18] aWEIGHTS (TOTAL OF THE AVEfAGE VALUES) TO PRODUCE THE PRICE INDEX.
[19] athis progfam requires the use of afmt, LISt, and min
[20] \(C T R \leftarrow 1\)
[21] 'ENTER THE YEARS FOR WHICH THE INDEX IS TO BE COMPUTED, EG, 1973197419
        75 •
[22] \(N+\rho N N+\square\)
[23] 'enter the number of items to be included in the price index, eg, 6'
[24] \(M+\square\)
[25] PRICE+QUAN+(M,N) 00
[26] 'enter the names of the ttems to be included in the price index, eg, ,
[27] 'LUMBER CEMENT NAILS ASPHALTSHINGLES. NOTE THAT ANY ITEM CONTAINING'
[28] 'TWO OR MORE WORDS IS TO BE JOINED TOGETHER TO MAKE ONE WORD. NO ITEM'
[29] 'SHOULD EXCEED SIXTEEN CHAFACTERS IN LENGTH.'
[30] LIST+MIM ' ', achanges a row of words into a column matrix of the words.
[31] LIST+LIST,((1+oLIST),(16-1+рLIST))p' ' ataKES LITERAL MatRIX CONTAINING I
        TEM NAMES
[32] afd pads with blanks to produce a literal matrix of the following form: \(L\)
        \(\operatorname{IST}[N ; 16]\).
[33] L1:'ENTER data FOR THE PRODUCTTON MATRIX, EG, quantities of each item sold
        , FOR '; \(N N[C T R]\)
[34] L11: \(\rightarrow(M=\rho V V+, \square) / A G A I N\)
[35] \(\square+A^{+}\)'INCORRECT NUMBER OF ITEMS. TRY AGAIN',
[36] \(\rightarrow\) L11
[37] AGAIN: QUAN[:CTR]+(( \(\rho V V), 1) \rho V V\)
[38] CTR \(-C T R+1\)
[39] \(\rightarrow L 1 \times 1(C T R) \leq N\)
[40] \(C T R+1\)
[41] L2:'ENTER data for the price matrix, eg. Prices of each item, for ; ;NN[Ctr
        ]
[42] L111:*(M=pVV*, ])/AGAIN 1
[43] \(A\)
[44] \(\rightarrow\) L111
[45] AGAIN1:PRICE[;CTR]+(( \(\rho V V), 1) \rho V V\)
[46] \(C T R+C T R+1\)
[47] \(\rightarrow L 2 \times 1(C T R) \leq N\)
[48] VALUE + QUA \(N \times P R I C E\)
[49] LOGFAT+(M,1)p10@(,PRICE[;N]) \(\operatorname{PRICE}[; 1]\)
[50] AVEVAL+(+/VALUE) \(\div N\)
```

[51] WTRATIO++/(AVEVAL×.LOGRAT)
[52] LOGPINDEX+WTRATIO $\div+$ /AVEVAL
[53] $R+(10 *$ LOGPINDEX $) \times 100$
[54] 'PRODUCTION DATA'
[55] '4A1,X12,10I12' $\triangle F M T\left(\left(14 \rho \rho^{\prime} I T E M^{\prime}\right) ;(1, \rho N N) \rho N N\right)$
[56] ''
[57] '16A1,10CF12.2' $\triangle$ FMT (LIST;QUAN $)$
[58] ''
[59] '
[60] 'PRICE DATA'
[61] '4A1,X12,10I12' $\triangle \operatorname{AFMT}\left(\left(14 \rho^{\prime} \operatorname{ITEM}{ }^{\prime}\right) ;(1, \rho N N) \rho N N\right)$
[62] ''
[63] '16A1,10CF12.2' $\triangle E M T(L I S T ; P R I C E)$
[64] '
[65] '
[66] 'VALUE DATA.

[68] '•
[69] '16A1,10CF'12.2' $\triangle F M T(L I S T ; V A L U E)$
[70] ''
[71] '•
[72] '
[73] 'PRICE INDEX (PERCENT) IS: ; R $\nabla$
4.0

IJCLA APL LIBRARY FUNCTIONS

```
--> 1 PLOTFORMAT PLOT<<-
```

SYNTAX: A PLOT B

```
the function plot will gFafH one or more functions
simultaNEOUSLY, aUTOMATIC.ally SC.aling the values to fit
APPROXIMATELY WITHIN SCALE DIMENSIONS SPECIFIED BY THE USEK.
IT WILL WORK ONLY IN 1-ORIGIN INDEXING.
THE FORM IN WHICH PLOT IS USED IS:
    SCALESIZE PLOT FUNCTION
LEFT ARGUMENT: ONE OR TWO NUMEERS.
SCALESIZE[1]: HEIGHT OF PLOT ON PAPEF IN LINES
SCALESIZE[2]: WIDTH OF PLOT ON PAFER IN CHARACTEAS
NOTE: IE NO SCALESIZE[2] IS GIVEN, SCALESIZE[I] IS RE-USED.
    THERE IS NO BUILT-IN LIMIT TO THE DIMENSIONS, AND A
    HORIZOITAL AXIS LARGER THAN THE WOFKSPACE WIDTH WILL
    CAUSE SOME FOINTS TO BE PFINTED ON THE NEXT LOWER
    LINE.
RIGHT AEGUMENT: A FECTANGULAR ARRAY WITH RANK}\leqslant3
    scalar: will be treated as a vectar of length one.
    vector: will be plotted as ordinate agatnst its own
    INDICES AS ABSCISSA.
    matrix: the leftmost column will be taken as the
    ABSCISSA AND ALL OTHER COLUMNS WILL BE PLOTTED AS
    ORDINATES. A DIFFERENT PLOTTING SYMBOL UP TO THE
    NUMBER OE SYMBOLS AVAILABLE WILL BE USED FOR EACH
    COLUMN. IN CASE TWO ORDINATES HAVE A COMMON FOINT,
    the symbol for the column fufthest to the right will
    BE USED.
    3-Dimensional array: the first plane will be plotted
    as a matrix, and all othef planes will be disregarded.
GUXILIARY FUNCTIONS: THE FUNCTIONS AND AND VS CAN BE
    used to generate thf fight argument in the profek form
    FOR PLOT. FOF EXAMPLE:
    20 PLOT Z AND Y VS X
```



```
    \nabla A PLOT B;C;D;F;G;H;I;J;L;T;Y;HZ;NB;VT;PT;ST;ISV;U
[1]
    PC+'O\star\circ\nabla\triangle\square'
[2]
    H.S+0
    ST
    SM* 5 10
    T((0=x/(2\rho.4),pB), 3 2 { < \rho\rhoB)/O,PFKEFF,PLOTL2,PLOTL3
    * PLOTL 3 < \rho\rho\rhoB+Q(2,D)\rho(1D+\rho,B),B
    PLOTL2:B+B[1;;]
    PLOTL3:Y+1+1(\rhoB)[2]-1
[9] C+((Г/\Gamma/B[;Y])-L/L/E[;Y]),(\Gamma/B[;1])-L/E[;1]
[10] }F+{(2p.A):C+(C=0)\timesB[1; 2 1] ] B[1; 2 1]=
[11] F*(ST[+/(L0.0001+F\times10*-G)0.\geqST])\times10*G*L100F
[12] G+(SM\divF)\timesL((L/L/B[;Y|),L/E[;T]})\timesF\divSM+16LSM[ 1 4
[13] }B[;\mp@code{1]}+[0.5+F[2]\timesB[;1]-G[2
[14] }B[;Y]+L0.5+F[1]\timesE[;YY]-G[1
[15] H+SM\times\Gamma((Г/\Gamma/E[;Y]),\Gamma/E[;1])\divSM
[16] NB-G[1]+(SM[1]:F[1])\times0,1H[1]\divSM[1]
[17] HZ-G[2]+(\widetilde{SM[2]\divF[2])\times0,1H[2]\divSM[2]}
[18] 00.ST+6p~ISV+1\geqU*9
[19] FLOTL4:VI*V/0>NB+NB\times10*U-ST[6-ISV]+I*1+\Gamma/L10*|(NB70)/NB
[20] }PT+L1+10|PT-1|PT+1\mp@subsup{E}{}{-}5+(|NB)0.\div10** 1+\phi,U
[21] L+U+1-(\phi((C+\rhoNB)\rho1)^. =PT) 10
[22] (( U>T+VT+\Gamma/I,(L+L\not=I),(I\leq0)\times2+L-I),ST[2-ISV]+ST[2-ISV]\veeL\geqU-VT+L>I)/
    3 2 +I26
[23] }\mp@subsup{\mp@code{(}}{}{-1}1+I25)\times\rho\rho\rhoST[4-ISV]+I&
```



```
[25] FT+(-VT+O\Gamma1-T)\ointPT
```



```
[27] }->(2+I25)\times1~V
[28] PT[(U-+/(C,U) \rhoJ ) +U\times-}-1+1C]+11\timesNB<
[29] PT\leftarrow(~(\imathU+J)\epsilon(I+J),i-1+J\leftarrowU-T)\(1 0 + C,U) \rhoPT,U\rhoO
[30] PT[iC;TI+J]+12
[31] PT*' 0123456789-.'[1+PT[;!U-1]]
[32] }->\mathrm{ PLOTL13*1~ISV
[33] L+1,H[2]\rho O NC+H[1]
[34] PLOTL8:L+(L\timesHS\timesC\not=O)\lceil1,H[2]p 0
[35] L[1+(D\not=0)/E[;1]]+(D\not=0)/D+(C=B[;Y]) \. xY
[36] }->(C\not=0)/PLOTL11
[37] L+L[0=(SM[2]:2)|0,1H[2]
[38] PLOTL11:SM[((\rhoPT)[1],1+C:SM[1])[1+0=SM[1]|C1;],(' |, (\rhoY)PPC)[1+L]
[39] }->(0\leqC+C-1)\rhoPLOTL
[40] }->(U=U\leftarrowSM[2]-~ISV*~\rho\rhoNB&,HZ)\rhoPLOTL
[41] PLOTL13:(SM[2]-9)ф(,(0 0 , (U-1)\rho1)\PT),',
[42] ->(ST[11 3-2 4],1)/ 1 3 5 7 10 +I26
[43] ('ORIGIN AND SCALE FACTOR FOR ORDINATE: ';G[1],:F[1])
[44] }->(2+I26)\times10=ST[3
[45] ('SCALE FACTOR FOR ORDINATE: ';10*ST[5]-1)
[46] }->(2+I25)\times:0=ST[2
[47] (ORIGIN AND SCALE FACTOR FOR ABSCISSA: ';G[2],:F[2])
[48] ->0 * O O=ST[4]
[49] ('SCALE FACTOR FOR ABSCISSA: ';10*ST[6]-1)
[50] ->0
[51] PRKERR:'THE RIGHT ARGUMENT OF PLOT MUST HAVE FANK s 3.'
    \nabla
```

```
--> 1 PLOTFORMAT VS<--
```

```
SYNTAX: 2&A VS B
    THE <VS> FUNCTION IS ESSENTIALLY A COLUMN-CATENATOR, SIMILAR TO
AND, EXCEPT THAT THE FIGHT-HAND ARGUMENT MUST BE OF FANK \leq 1. IT IS
DESIGNED FRIMARILY TO PROVIDE CONVENIENT FOFMATION OF INPUT TO PLOT
FUNCTION. WHETHER USED BY ITSELF OR WITH AND, VS WILL CAUSE ITS
RIGHT ARGUMENT TO APPEAR AS the LEFTMOST COLumN oF the resulting
ARRAY. (THE fESULTANT WILL BE AN ARRAY OF RANK THREE, CONSISTING OF
A SINGLE PLANE).
```

```
    \nabla M+A VS B;C;D
[1] +(((\rho\rhoB+,B)<\rho\rhoB), 2 1 0 <\rho\rhoAA)/ 8 8 4 3
[2] }A*((\rhoB),1)\rho
[3] A+((x/0.4),1) P. A
[4] }->(\wedge/(\rhoB)\not=1,1\rho\rhoA)/
[5] M-(0,(1\rho\phi\rhoA)\rho1)\A
[6] M[;11]+B
[7] }->0\times\rho\rhoM+(1,\rhoM) \rho
[8] +0 =OD+'AN ARGUMENT OF VS IS OF IMPROPER RANK.'
[9] 'arguments of vs afe not conformable.'
\nabla
```

--> 1 PLOTFORMAT AND <--
SYNTAX: $2 \leftarrow A$ AND $B$
THE <AND> FUNCTION IS ESSENTIALLY A COLUMN-CATENATOR, WITH SOME
EXifa effects when the arguments afe not matrices. the function is
DESIGNED TO BE USED EITHEK INDEPENDENTLY, OR IN CONJUNCTION WITH
VS. it provides a convenient way of forming input to dFt and eft.
$\nabla A N D[\square] \nabla$
$\nabla L \leftarrow A \quad A N D \quad B ; C ; D$
[1]
[2] $\quad B \leftarrow, B$
[3] $\rightarrow(((3=\rho \rho B) \wedge 1 \neq 1 \rho \rho B), 2=\rho \rho A) / 177$
[4] $A+, 4$
$[5] \rightarrow(\wedge /((\rho, A) \neq 1, D), 1 \neq D+1 \rho-2 \phi \rho B) / 16$
[6] $\quad A+(((D \times \rho . A) \downharpoonright D\lceil\rho . A), 1) \rho A$
[7] $\rightarrow(1 \neq \rho \rho B) / 9$
[8] $B+(((\rho B) \Gamma(1=\rho B) \times 1 \rho \rho A), 1) \rho B$
[9] $\rightarrow\left((\wedge / D \neq 1,1 \rho \rho A), 1 \neq D \leftarrow 1 \rho^{-} 2 \phi \rho B\right) / 1611$
[10] $B+(((3=\rho \rho B) \rho 1),(1 \rho \rho A), 1 \rho \phi \rho B) \rho B$
[11] $+(3=\rho \rho B) / 14$
[12] $L \leftarrow(((C+1 \rho \phi \rho . A) \rho 0),(1 \rho \phi \rho B) \rho 1) \backslash B$
$[13] \rightarrow 0 \times \rho \rho L[; 1 C]+A$
[14] $L \leftarrow\left(1,((C+1 \rho \phi \rho A) \rho 0),\left({ }^{-} 1+1 \rho \phi \rho B\right) \rho 1\right) \backslash B$
$[15] \quad+0 \times \rho \rho L[; 1+1 C]+A$
[16] $\rightarrow 0=0[+A R G U M E N T S$ OF AND ARE NOT CONFORMABLE.'
[17] 'AN ARGUMENT OF AND IS OF IMPROPER F.ANK.'
$\nabla$

```
--> 1 FORMAT \triangleFMT <--
```

```
SYNTAX: FS \triangleFMT (V1;V2;V3;VN)
AUTHOR: STSC
REFERENCE: \triangleFMT - fEPORT FORMATtING IN APL PLUS , STSC
    \triangleFMT GIVES THE APL PLUS USER A SIMFLE, ECONOMICAL, AND
ADAPTABLE MEANS OF PFODUCING fEPORTS INVOLVING tabular formatting
OF NUMEFIC AND CHARACTER DATA. TABULAR OUTPUT PRODUCED USING \triangleFMT
takes about one-thentieth the cpu time fequired using other
METHODS.
\triangleFMT EMPLOYS ITS LEFT ARGUMENT to CONTROL PRINTING of ITS RIGHT IN
ONE OR MORE COLUMNS.
```


## RIGHT ARGUMENT

$V 1, V 2, V 3, \ldots, \operatorname{AND} V N$ ARE APL VARIABLES OR EXERESSIONS. THEY MAY BE ANY COMBINATION OF CHARACTER OR NUMERIC SCALAKS, VECTORS OF MATRICES. A MATRIX IS PRINTED IN ONE OR MORE COLUMNS; A VECTOR OR SCALAR IS TREATED AS THOUGH IT WERE A SINGLE COLUMN MATRIX.

## LEFT ARGUMENT

Fs is a character VECTOR made up of one or more format ehrases SEPARATED BY COMMAS. EACH PHRASE CONTROLS THE PRINTING OF ONE OR more columns. the allowable format phrases are:

| $\underline{M A W}$ |  | CHARACTER EDITING |
| :---: | :---: | :---: |
| $\bar{M} I \bar{W} \quad O R$ | MQIW | INTEGER EDITINS |
| $\bar{M} F \underline{W} \cdot \underline{D} \quad O R$ | $\underline{M Q} F \underline{W} \cdot \underline{D}$ | FIXED-POINT NUMERTC EDITING |
| $\bar{M} E \bar{W} \cdot \underline{S}$ |  | floating-poInt numeric editing |
| $\bar{M} X \bar{W}$ |  | INSERTION OF BLANKS |
| $\bar{M} \bar{T} E X T \square$ |  | insertion of text |

HERE $\quad \underline{M}, \underline{W}, ~ A N D ~ S E P R E S N T$ INTEGER CONSTANTS. $\underline{Q}$ REPRESENTS OPTIONA $\bar{L}$ QUAL $\bar{I} F I E R S$ And DECORATIONS.

M, WHICH IS OPTIONAL, INDICATES HOW MAY TIMES A PHRASE IS TO APPLY. $\bar{I} F \operatorname{M}$ IS NOT PRESENT, IT IS TAKEN TO BE 1. THUS, $3 A 1$ IS EQUIVALENT TO A1, A1,.A1 AND $2 I 4$ IS EQUIVALENT TO I4,I4.

W is the field is the field width, indicating the number of print FOSITIONS OCCUPIED BY THE EDITED VALUE (FOR A, I, F, AND E) OF BY INSETED BLANKS (FOR X).

FOR FIXED-POINT EDITING, D is the NUMBER OF DIGITS to appear to the RIGHT OF the decimal POINT. D MUST BE LESS than W. FOR FLoating-point editing, s is the numeer of significant digits to be PRINTED. S MUST BE LESS THAN W-4.

THE A PHRASE IS USED ONLY TO EDITY CHARACTER VALUES WHILE I, E, AND E PHRASES ARE USED ONLY TO EDIT NUMERIC VALUES.

CHARACTERS ENCLOSED BETWEEN SYMBOLS ARE INSERTED DIRECTLY INTO TOE EDITED LINE. THE INSERTED TEXT IS PRINTED EXACTLY AS IT APPEARS (INCLUDING SPACES) BETWEEN THE © SYMBOLS.

QUALIFIER CODES

```
B Leaves the result field blank if the edited value is
    ZERO
C INSERTS COMMAS BETWEEN EACH GfoUP OF THREE DIGITS IN
    the integer part of the edited value.
L LEfT-ADJUSTS the value in the result field.
2 FILLS UNUSED LEADING FOSITIONS IN THE FESULT FIELD
    WITH ZEROS (AND INSERTED COMMAS, IF THE C QUALIFIEK
    IS USED) INSTEAD OF BLANKS.
```

DECOFATION CODES
MLTEXTM PLACES THE TEXT ON THE LEET OF AN EDITED NAGATIVE value. the default value for the m decorations is the NEGATIVE SIGN, " ${ }^{-}$.
NCTEXTU PLACES the teXt on the fight of an edited negative value. the default value is null.
PDTEXTU PLACES THE TEXT ON THE LEFT OF AN EDITED POSTIVE OR zefo value. the default value is null.
QDtexty places the text on the right of an edited positive or zEfo value. the default value is null.
ritextu fills the result field with the text, prior to editing the value into the eield. the text will appear in all positions of the result field not filled by the edited VALUE. THE TEXT IS USED AS MANY TIMES (REPLICATED) AS Needed to fill the field. the default value is blank.

```
--> 1 FOKMAT COLNAMES<--
```

```
SYNTAX: FESULT * FS COLNAMES TEXTVECTOR
```

REGUIRES: FWTD
FEFEFENCE: $\triangle F M T-F E P O K T$ FORMATTING IN APL PLUS, STSC
THE FUNCIION COLNAMES PRODUCES COLUMN HEADINGS FOR A $\triangle F M T$ REGULT.
FS IS THE VECTOR OF FORMAT PHRASES NORMALLY USED BY $\triangle F M T$ AND
TEXTVECTOR CONTAINS THE COLUMN HEADINGS. THE FIRST CHARACTER OF
TEXTVECTOR IS TAKEN AS THE SEPAFATOR CHARACTEF, AND THE CHARACTERS
BETWEEN SUCCESSIVE SEPARATORS WILL APPEAR OVER $\triangle F M T$ FIELDS. A $\triangle E M T$
FIELD CAN BE SKIPPED BY USING TWO CONTIGUOUS SEPARATORS. THE
CHAFACTEKS AFE FIGHT~JUSTIETED EOR F, I, AND E FIELDS, AND AFE
LEFT-JUSTIEIED FOR A FIELDS. X AND 凹TEXTए FIELDS ARE SKIEPED. IF
THE NUMBER OF CHARACTERS TO BE PRINTED EXCEEDS THE FIELD WIDTH,
THAT PART OE THE LINE WILL BE EILLED WITH STAFS, EXCEPT THAT
OVEFSIZE TEXT ASSOCIATED WITH A FIELDS WILL BE FLACED IN FOLLOWING
X AND UTEXTE POSITIONS.
VCOLNAMES[D] $\nabla$
$\nabla K \leftarrow A$ COLNAMES $B ; C ; D ; E ; S$
[1] $C+F+0 \rho A+((E+\sim ? 1) \rho 0)$, RWTD $A$
[2] $\rightarrow(1 \geq \rho A) \rho 12$
$[3] \rightarrow(A[3] \geq 4) \rho 7$
$[4] \quad C+C, A[1] \rho-A[2]$
[5] $.4+4 \not+A$
[6] +2
[7] $\quad C+C,(0.5 \times 4 \geq A[3])+x / A\left[\begin{array}{ll}1 & 2\end{array}\right]$
$[8] \rightarrow(1 \geq p .4+4+A) p 12$
[9] $\rightarrow(A[3]<45) / 27$
$[10] \quad C+\left({ }^{-} 1+C\right),\left({ }^{-} 1+C\right)+x / A\left[\begin{array}{ll}1 & 2\end{array}\right]$
$[11]+8$
[12] $A \leftarrow+/ \mid L C$
[13] $S+0, E+\left(B={ }^{-} 1+B\right) / \imath \rho B+1 \phi, B$
$[14] \rightarrow(10.5=(\rho S), 1 \mid 14 C) / 2219$
$[15] \quad R+R,(\mid 1+C)+\left(((\rho D)>\mid 1+C) /(\mid 1+C) \rho^{\prime} \star^{\prime}\right),(1+C)+\operatorname{L}^{-} 1+S[1-E]+S[2-E]+B$
$[16] \quad S \leftarrow 1+S$
$[17] \quad C+1+C$
[18] $\rightarrow 14$
$[19] \quad R+R,(L 1+C) \uparrow^{\prime}$.
[20] $C+1 \downarrow C$
[21] $\rightarrow 14$
[22] $R \leftarrow(1, A) \rho A \uparrow R$
$\nabla$

```
--> 1 FORMAT CENTER<-
SYNTAX: RESULT & FS CENTER TEXTVECTOR
REQUIRES: FWTD
FEFERENCE: \(\triangle F M T\) - REPORT FORMATTING IN APL PLUS, STSC
THE FUNCTION CENTER PRODUCES A CENTERED TITLE LINE FOR USE WITH A \(\triangle F M T\) DISPLAY. FS IS THE VECTOR OF FORMAT PHRASES NORMALLY USED BY \(\triangle F M T\), AND THE TEXTVECTOR IS A CHARACTER VECTOR HOLDING THE TITLE. THE KESULT IS A CHARACTER MATRIX WITH ONE ROW AND AS MANY COLUMNS AS A \(\triangle E M T\) RESULT WOULD HAVE IF USED WITH FS AS THE LEET ARGUMENT. THE CHARACTERS GIVEN IN TEXTVECTOR ARE CENTERED IN THIS MATRIX. IF TEXTVECTOR IS TOO LONG, IT IS TRUNCATED AT THE RIGHT
```

```
    F F\leftarrowA CENTER B
[1] A++/\times/ 0 -2 +RWTD A
[2] }\mp@subsup{|}{\nabla}{}\mp@subsup{F}{}{+}(1,A)\rhoA\uparrow((\Gamma0.5\times0\lceilA-\rhoB)\uparrow', '),B\leftarrow,
```

--> 1 FOKMAT RWTD<--
SYNTAX: $F E S U L T \leftarrow R W T D F S$
REEERENCE: $\triangle F M T-R E P O R T$ FORMATTING IN APL PLUS, STSC
THE RESULT OF RWTD IS A NUMERIC MATRIX WITH AS MANY ROWS AS THERE
ARE FORMAT PHRASES IN FS (A VALID $\triangle F M T$ FORMAT PHRASE
(LEFT-AFGUMENT)), AND FOUR COLUMNS. THE COLUMNS HAVE THE FOLLOWING
INTERPRETATION:
1 REEETITIONS
2 WIDTH OE FIELD
3 TYPE OF FIELD, AS FOLLOWS
$1 E$ EIXED-POINT
2 I INTEGER
3 E FLOATING-POINT
4 A CHARACTER DAT.S
5 X SKIP
6 】TEXTV LITERAL TEXT
4 DECIMAL FOSITIONS EOR EIXED-POINT,
SIGNIFICANCE FOR FLOATING-POINT, AND
ZEKO OTHERWISE.
EKFOR CHECKING IS NOT PERFORMED AND IT IS ASSUMED THAT FS IS A
PROPER $\triangle F M T$ ARGUMENT.

## SYNTAX: $R \nleftarrow A K I \quad P$

AUTHOR: ROY SYKES. STSC, L.A. OEFICE
WHEN EXECUTED, <AKI> PRINTS OUT THE PRONPT P AND AWATTS A USE RESPONSE ON THE SAME LINE. CONSECUTIVE SPACES ARE COMPRESSED OUT OF THE KESPONSE, WHICH IS THEN RETURNED AS THE EXPLICIT RESULT OF THE FUNCTION.

```
    \nabla R+AKI AKI;A
[1] [ +AKI
[2] 20I:0
[3] +(4 7 =0.4*, (#)/ 9 8
[4] F*' '=A+' ', A
[5] F+1+(R*1+R,1)/A
[6] 5I120LOF-140+2\times(\rho.4)+-14\rhoAKI
[7] }->
[8] }->4\mp@subsup{x}{}{\prime}SUSPEND'v.z
[9] -('STOP'v.7A) \rho4
[10] 
    \nabla
--> 1 INFNS AYN<--
```

SYNTAX: $R \leftarrow A Y N \quad P$
REQUIRES:AKI
AUTHOR: FOY SYKES, STSC, L.A. OFEICE
THE EUNCTION <AYN> PRINTS THE PROMPT, SPECIFIED BY THE MAIN
PROGRAM IN THE VARIABLE P, AND ATTEMPTS TO RECEIVE A YES OR NO
REPONSE FROM THE USER. THE ONLY RESPONSES ACCEPTED ARE: YES, NO, Y,
OR N. ANY OTHER RESPONSE WILL CAUSE THE <AYN> FUNCTION TO PRODUCE
AN ERROR MESSAGE AND REQUEST THE USER TO TRY AGAIN. WHEV A VALID
RESPONSE IS GIVEN BY THE USER, THE <AYN> FUNCTION RFTURNS TO THE
MAIN PROGFAM A 1 IF THE RESPONSE WAS YES AND A O IF THE RESPONSE
WAS NO.

```
    \nabla R\leftarrowAYN AYN;A;N;T
[1] & ACCEPT YES/NO INPUT. REGUIRES <AKI>, AND<ES>. AUTHOR: K. SYKES, STSC.
[2] A* 4 3 \rhoTYESN्NO Y N .
[3] T*AYN
[4] +(0 3 \geq0N-AKI T,', ',4\rhoBS)/ 3 6
[5] *4,\rhoT*'PLEASE ANSWEIR YES OR NO:*
[6] }+(v/T+A^.=3+N)+
[7] 
\nabla
```

```
SYNTAX: F+INP L
AUTHOR: KOY SYKES, STSC, L.A. OFFICE
    the fuNCTION <INP> ALLOWS thE USER TO SPECIFY THE ACCEPTABLE
NUMBER OF INPUTS. THE RIGHT ARGUMENT IS ONE OR MORE NUMBERS WHICH
REPRESENT THE ACCEPTABLE SIZE OF THE INPUT VECTOR. FOR INSTANCE, IF
yOU WOULD ACCECT EITHER 1 OR 5 NUMERIC INPUTS, WHERE IN THE CASE
WHERE 1 WAS GIVEN IT WOULD BE USED FOR ALL FIVE NUMBERS, THE
FOLLOWING FORM WOULD BE USED:
```

    \(h^{+}+I N P \quad 15\)
    THE <NIP> FUNCTION WOULD ACCEPT A SERIES OF NUMBERS AND CHECK
    to see if there was either 1 of 5 values given. if there was, the
result would be returned to the calling program. if there was a
LARGER OR SMALLER GROUP OF NUMBERS GIVEN, AN APPROPRIATE ERROR
message would be given.

```
        \nabla 2-INP X;V;EXIT
    [1] GENPUTXVALUES.HAS 'EXIT` ( }->\mathrm{ \ OPTION. FEQUIRES: < AFMT>. AUTHOR: C. CLAU
    [2] EXIT* 0 0 00
[3] }->(1\geq\rho\rho2-[])\rho
[4] }
[5] }->6\times(\wedge/X\not=\rho,2)^^人\rho,
[6] 攵+', =\overline{Y}+\mp@subsup{+}{0}{\prime}
[7] 1\overline{\}(\underline{Z}~\overline{1}+\underline{2},1)/\underline{V}
[8] *3
\nabla
```

--> 1 INENS IPI<--
SYNTAX: $\quad R \in I P I P$
FEQUIRES: AKI MIM
AUTHOR: CHRIS CLAUSEN, PHYSIOLOGY DEPARTMENT, UCLA
THE EUNCTION <IPI> ALLOWS THE MAIN PROGRAM TO PROMPT THE USEK
fof a series of positive integers. the matn progfam prints the
FIGHT ARGUMENT, WHICH IS AN ALPHA NUMERIC LITERAL VECTOR (PROMPT)
explaintng to the use what numbers he should enter. the function
THEN WILL ACCEPT THE RESPONSE FROM THE USER, TYPED ON THE SAME LINE
as the prompt, and return the result to the main program. if
ANYTHING OTHER THEN POSITIVE INTEGERS ARE ENTERED AN APPROPRIATE
EfROR MESSAGE WILL BE GIVEN. THIS PROGFAM WILL ACCEPT EITHER 1
VALUE, WHICH IS CONVEFTED INTO A SCALAF; OR A SEfIES OE VALUES,
WHICH AFE CONVERTED INTO A VECTOR.

```
SYNTAX: R+LINE S
AUTHOF: CHRIS CLAUSEN, PHYSIOLOGY DEPAETMENT, UCLA
    THE FUNCTIDN <LINP> IS DESIGNED TO ACCEFT INPUT THAT WOULD
NOfMally NOT fit on ONE LINE. the main frogram specifies the number
OE INFUTS DESIRED, S, AND THE <LINP> CONTINUES TO ASK FOF MORE DATA
uNtil it has received the fequired numbek. lf the usef types in
mORE NUMBERS than are NEEDED, the fuNCtION WILL ASK the usef to
fEENTER dUST THE LAST LINE OF HIS INEUTS.
```

```
\(\nabla\) 2 LINP X;EXIT;END; \(N ; M\)
[1] a LAKGE INPUT OF X VALUES. HAS 'EXIT' OFTION. REGUIRES: <NOSPACE>, < \(\triangle F M T>\)
                .;AUTHOF: CHRIS CLAUSEN, UCLA-PHYSIOLOGY
        EXIT-000 00
\(\left[\begin{array}{ll}{[2]} & E X I T+000 \\ {[3]} & E N D+0\end{array}\right.\)
\(\left[\begin{array}{ll}{[2]} & N+1 \Gamma / X\end{array}\right.\)
[5] \(2+10\)
[6] \(\rightarrow(2 \quad 3=\rho \rho N+\square) / 1215\)
\([7] \rightarrow(M<\rho N+Z, \underline{N}) \rho 11\)
[8] \(Z+\bar{N}\)
\([9] \quad(\bar{M}=\rho \underline{N}) \rho 0\)
\([10] \rightarrow 6\)
\([11]+6, \mathrm{D}\left[{ }^{\prime}\right.\) LENGTH ERROR...REENTER LAST LINE.'
\([12] \rightarrow((0=\rho, X) \vee X \vee .=\rho Z) / 0\)
```



```
\([14 j \rightarrow 5\)
\([15]\)
```

```
SYNTAX: R+NIP P
REQUIRES:AKI LF
AUTHOR: ROY SYKES, STSC, L.A.OFFICE
    THE FUNCTION <NIP> ACCEPTS A PROMFTED NUMERIC ANSWER AND
feturns the result to the calling program. the right argument.p ,
IS A ALFHANUMERIC LITERAL DIFINING TO THE USER WHAT INFORMATION IS
DESIRED. THIS FUNCTION WILL ACCEPT JUST ONE NUMBER, BUT THAT NUMBER
CAN BE ANY VALID FEPRESENTATION ACKNOWLEDGEABLE IN APL.
    \nabla R NIP P;O;S;I;D;E;T
[1] a NUMEFIC INPUT;AUTHOR: ROY SYKES, STSC.
[2] +4,0*-?1
[3] E:P*'INCOFRECT NUMBER...PLEASE REENTEF',(1^(0=\rhoE)p':'),E
[4] E+(1+T+O+\mp@subsup{F}{1}{\prime\prime}\mp@subsup{A}{}{\prime})\downarrowP*,P
[5] P*I'\uparrowP
[6] }->0\mathrm{ 0 1 = OT + AKI P)/ 6 9
[7] T+O+.0123456789.--E'IT
[8] +(13\epsilonT+(S+((P+1)+T)\epsilon 11 12)+T)\phi 15 11
[9] +(11 10 0 \leqT+O+'0123456789口'1T)/E, 10 20
[10] +0, \rhoR*D
[11] 
[12] +(v/10\leqP+(I+11 =1+P)+P)\rhoE
[13] + (9\epsilon(\rhoP),\rhoT+D\uparrowT)\rhoE
[14] P+10*(-1*I) < 101P
[15] +((v/T\geq11)\vee10\inD+(1+I+0+T:10)+T)\rhoE
[16] +(0=\rhoT*(I\uparrowT),D) \rhoE
[17] T&P\times(`1 0.1 x.*S,\rhoD) 人101T
[18] +19+Tz\T
[19] T+LT
[20] F+T
\nabla
```

```
--> 1 INENS BS <--
```

the bs character can be used to backspace the print element. it CAN BE STORE LIKE ANY OTHER APL CHARACTER IN A CHARACTER ARRAY. AN EXAMPLE OF ITS USE IS:
$R^{+}$'THIS IS A TEST', ( 14 pBS ),14p'_'
R NOW LOOKS LIKE THIS:
THIS IS A TEST
--> 1 INFNS CR<--

THE CR CHARACTER CAN BE USED TO CAUSE A CARRIAGE RETURN WITHIN A PROGRAM. IT CAN BE STORED LIKE ANY OTHER APL CHARACTEK. FOR EXAMPLE IT CAN BE IMEEDDED WITH IN A CHARACTER ARRAY. FOR EXAMFLE:

R+'THIS', CR,'IS', CR,'A', CK, 'TEST'
$R$ IS NOW THIS:
THIS
IS
A
TEST
--> 1 INFNS LF <--

THE LINE FEED CHARACTER CAN BE USE TO CAUSE THE TERMINAL TO SKIp Lines without returning the cafriage. for instance, if the PRINT BALL WAS POSITIONED AT POSITION 50 ON THE PAGE, 4 LF', SOULD CAUSE THE TERMINAL TO ADVANCE 4 LINES, BUT THE TYPE BALL WOULD STILL BE IN POSITION 50.

ENTER DOCUMENT NUMBER(S) TO PRINT:
5.0

OUTLINE OF THE COURSE
5.1

Class Schedule and Reading Assignments

# INTERACTIVE COMPUTING FOR MANAGEMENT EDUCATORS 

Graduate School of Management<br>University of California, Los Angeles

## CLASS SCHEDULE

Topic

| Day | Time | Group A | Group B |
| :---: | :---: | :---: | :---: |
| Monday, 30 June | 9:00-10:00 a.m. | Course Introduction and Overview: Adminis trative Details of the Program (2232A GSM) |  |
|  | 10:00-11:00 a.m. | Tour of the UCLA Campus |  |
|  | 11:00-11:30 a.m. | Tour of UCLA Campus Computing Network (CCN) | Visit Ackerman and Kerckhoff Halls |
|  | 11:30-12:00 a.m. | Visit Ackerman and Kerckhoff Halls | Tour of UCLA Campus Computing Network (CCN) |
|  | 12:00-1:00 p.m. | Lunch, UCLA Faculty Center |  |
|  | 1:00-2:30 p.m. | Assignment Hl, Lecture ( 2232 A GSMi) |  |
|  | 2:30-4:00 p.m. | Assign. \#2, Lecture (2232A GSM) | Assign. \#l, Lab. (2035C GSM) |
|  | 4:00-5:30 p.m. | Assign. \#l, <br> Lab. (2035C GSM) | Assign. \#3, <br> Lecture (2232A GSM) |
| Tuesday, <br> 1 July | 8:30-10:00 a.m. | Assign. \#3, <br> Lecture (2232A GSM) | Assign. \#3, <br> Lab. (2035C GSM) |
|  | 10:00-10:15 a.m. | Break | Break |
|  | 10:15-11:45 a.m. | Assign. \#3, <br> Lab. (2035C GSM) | Assign. \#4, <br> Lecture (2232A GSM) |
|  | 11:45-12:50 p.m. | Lunch, UCLA Faculty Center |  |
|  | 12:50-2:20 p.m. | Assign. \#4, <br> Lecture (2232A GSM) | Assign. \#4. <br> Lab. (2035C GSM) |
|  | 2:20-2:25 p.m. | Break | Break |



|  | 3:55-4:00 p.m. | Break | Break |
| :---: | :---: | :---: | :---: |
|  | 4:00-5:30 p.m. | Assign. \#10, <br> Lecture (2232A GSM) | Assign. \#10, <br> Lab. (2035C GSM) |
| Friday, 4 July | 8:30-10:00 a.m. | Assign. \#10, <br> Lab. (2035C GSM) | Assign. \#ll, <br> Lecture (2232A GSM) |
|  | 10:00-10:15 | Break | Break |
|  | 10:15-11:45 a.m. | Assign. \#ll, <br> Lecture (2232A GSM) | Assign. \#ll, <br> Lab. (2035C GSM) |
|  | 11:45-12:50 p.m. | Lunch, Buffet in 2355 |  |
|  | 12:50-2:20 p.m. | Assign. \#ll, <br> Lab. (2035C GSM) | Assign. \#12, <br> Lecture (2232A GSM) |
|  | 2:20-2:25 p.m. | Break | Break |
|  | 2:25-3:55 p.m. | Assign. \#12, <br> Lecture (2232A GSM) | Assign. \#12, <br> Lab. (2035C GSM) |
|  | 3:55-4:00 p.m. | Break | Break |
|  | 4:00-5:30 p.m. | Assign. \#12, <br> Lab. (2035C GSM) | Assign. \#l3, <br> Lecture (2232A GSM) |
| Monday, 7 July | 8:30-10:00 a.m. | Assign. \#13, <br> Lecture (2232A GSM) | Assign. \#13, <br> Lab. (2035C GSM) |
|  | 10:00-10:15 a.m. | Break | Break |
|  | 10:15-11:45 a.m. | Assign. \#13, Lab. (2035C GSM) | Assign. \#14, <br> Lecture (2232A GSM) |
|  | 11:45-12:50 p.m. | Lunch, UCLA Faculty Center |  |
|  | 12:50-2:20 p.m. | Assign. \#14, <br> Lecture (2232A GSM) | Assign. \#14, <br> Lab. (2035C GSM) |
|  | 2:20-2:25 p.m. | Break | Break |
|  | 2:25-3:55 p.m. | Assign. \#14, <br> Lab. (2035C GSM) | Assign. \#l5, <br> Lecture (2232A GSM) |
|  | 3:55-4:00 p.m. | 3 reak | Break |


|  | 4:00-5:30 p.m. | Assign. \#15, <br> Assign. \#15, <br> Lecture (2232A GSM) <br> Lab. (2035C GSM) |
| :---: | :---: | :---: |
| Tuesday <br> 8 July | 8:30-10:00a.m. | Assign. \#15 <br> Assign. \#16, <br> Lab. (2035C GSM) <br> Lecture (2232A GSM) |
|  | 10:00-10:15 a.m. | Break Break |
|  | 10:15-11:45 a.m. | Assign. \#17, Lecture (2232A GSM) |
|  | 11:45-12:50 p.m. | Lunch, UCIA Faculty Center |
|  | 12:50-2:20 p.m. | Assign. \#18, Lecture (2232A GSM) |
|  | 2:20-2:25 p.m. | Break Break |
|  | 2:25-3:55 p.m. | Assign. \#16, Programming Project <br> Lecture (2232A GSM) Lab. (2035C GSM) |
|  | 3:55-4:00 p.m. | Break Break |
|  | 4:00-5:30 p.m. | Programming Project, Lab. (2035C GSM) |
| Wednesday, <br> 9 July | 8:30-10:45 a.m. | Programming Project, Lab. (2035C GSM) |
|  | 10:45-il:00 a.m. | Break |
|  | 11:00-12:00 a.m. | Commerical Applications of APL, Scientific Time <br> Sharing Corp., Lecture, (2232A GSM) |
|  | 12:00-1:00 p.m. | Lunch, UCLA Faculty Center |
|  | 1:00-5:30 p.m. | Programming Project, Lab (2035C GSM) |
| Thursday, <br> 10 July | 8:30-10:45 a.m. | Programming Project, Lab (2035C GSM) |
|  | 10:45-11:00 a.m. | Break |
|  | 11:00-12:00 a.m. | Commerical Applications of APL, Proprietary Computer Systems, Inc., Lecture (2232A GSM) |
|  | 12:00-1:00 p.m. | Lunch, UCLA Faculty Center |
|  | 1:00-5:30 p.m. | Programming Project, Lab. (2035C GSM) |
| Friday, <br> 11 July | 8:30-10:00 a.m. | A Review of APL Usage, Lecture (2232A GSm) |
|  | 10:00-10:15 a.m. | Break |
|  | 10:15-11:00 a.m. | Pedagogical Approaches to Teaching APL, Lecture (2232A GSM) |


| 11:00-12:00 a.m. | Programming Project, Lab. (2035C GSM) |
| :--- | :--- |
| 12:00-1:00 p.m. | Lunch, UCLA Faculty Center |
| 1:00-5:30 p.m. | Programming Project, Lab. (2035C GSM) |

$6 / 30 / 75$

INTERACTIVE COMPUTING FOR MANAGEMENT EDUCATORS

## Graduate School of Management

 University of California, Los Angeles
## Reading Assignments

Note: "Buckley et al." refers to Buckley, Nagaraj, Sharp, and Schenck, Management Problem-Solving in APL, Melville, 1974.
"G. \& R." refers to Gilman \& Rose, APL: An Interactive Approach (2nd Edition), John Wiley \& Sons, 1974.

Assign. \# Required Reading
1.

Buckley et al., Chapter 1. G.\&R., Chapters $1 \& 2$.
2.

Bohl, Information Processing, SRA, 1971, pp. 1-37, 49-93, 106-171, 189-220, 231-235 and 247-282.
3.
G. \& R., Chapters 3, 4, \& 5 .
4. G.\& R., Chapters 6 \& 7 .
5.
G. \& R., Chapters $8 \& 9$.
6. G. \& R., Chapters $10 \& 12$.
7. G. \& R., Chapters ll\& 13 .
8. G.\&R., pp. 131-137, 159-164, Chapters $22 \& 23$
9. G.\&R., Chapter 14 \& 15 .
10.
G.\& R., Chapters 16, 17, \& 28.
11. G. \& R., Chapters $18 \& 19$.
12.
13.
G.\& R., Chapters $20 \& 24$.
G.\&R., Chapters 25, 26, \& 27.
14.
15.
16.
17.
18.

UCLA APL Library Discription (Handout); PLOT Description (Handout); Buckley et al., Chapter 7.

STSC, APL Plus $\triangle$ FMT Report Formatting Instructions Manual; G. \& R., Chapter 21 (lightly)

No reading assianment (a discussion of programming techniques for use with APL). G.\&R., Chapters 29, 30, \& 31; STSC, APL Plus File Subsystem Instruction Manual. G.\&R., Chapters 32 \& 33.
-
5.2

Class Handouts

## 5.2 .1

## A Guide to Writing APL Programs

A GUIDE TO WRITTNG APL PROGRAMS

1. Define the Problem.

Read the problem statement carefully and decide what it is that is really being asked for.
2. Identify the Steps Needed.

Break down the problem into the logical steps needed to solve the problea (not the specific APL instructions).
3. Define the Logic of Each Step.

Here the exact operations needed to accomplish the desired results are defined; $\overline{\mathrm{e} . \mathrm{g} .,}$ "Input data from a user"--a step as defined in No. 2 above--would require (1) "Display instructions to the users of your program," (2) "Accept a literal input from the user, and (3) "Store the input in a variable," would be the No. 3 equivalent of No. 2.
4. Write the Code and Define the Function.

Taking the detailed logic of Step No. 3, write the actual APL code needed to accomplish each step or task. If you are unsure about a particular operator, or how a line of code will actually execute, you may wish to test it out first before going into function definition mode.
5. When You Have Defined the Function, Test It with Sample Data. In testing your function, use "typical" data first, and then use more unusual data (e.g., vectors rather than scalars, negative numbers, zeros, etc.).
6. When the Function "Hangs," Examine the Indicators. The error messages (e.g., LEUGTH ERROR, RANK ERROR, SYNTAX ERROR, etc.) and the location of the carat (the " $\Delta$ ") can be very helpful in determining what is wrong.
7. Examine the Line of Code at Which Execution Stopped.

It is possible that the problem was caused by a mistake in a preceding line of code (but not of the sort that would produce an error message), but you should first check cut the line where execution stopped. In analyzing a line, the following procedure is a helpful guide:

- START AT THE RIGUTS AND WORK TO THE LEFT (the same way APL executesl)
- Ask the following questions to yourself of each term encountered:

1) Is it an argument or an operator?
2) If an argument, is it a matrix, vector, or scalar?
3) If an operator, is it monadic or dyadic? (To tell, look to see if there is a left argunent.)
4. If it is dyadic, is the left argument a matrix, vector, or scalar and is it compatible with the right argument?

- Once the above have been determined, execute (in desk calculator mode) the portion of the line of code just analyzed.
- Using the result of the preceding execution, proceed agoin to the
left until the entire line of code has been checked out and produces the desired result. (N.B., the first error you find and correct may not be the only error in the line.)
- Two of the most common errors are to overlook the strict right to left execution (which can frequently be corrected by the use of parentheses) and the failure to recognize that vector operations are involved (e.g., thus creating LENGTH, RANK, or INDEX errors). This latter problem may require a variety of solutions (e.g., reduction, ravelling, etc.) as determined by each situation.

8. Clear the Suspend Execution.

Although it is possible to continue the execution of the suspended program (by branching to the point in the program where the execution was suspended)
it is probably easier to terminate execution and start again. You can clear out the suspended execution simply by typing a right arrow ("->"). (To check to see if all suspensions have been cleared, type ")SI". If there are none, nothing will print; if some still exist, one line will print for each suspension stored. As above, one right arrow is needed to clear each suspension.)
9. Correct the Error.

By use of function editing, go into function definition mode and change the incorrect line of code into its corrected version.
10. Retest the Function.

Quite frequently, another error will be detected, so Steps No. 6, 7, and 8 should be repeated.
11. When No Errors are Detected, "Desk Check" Your Results.

Even though no errors have been detected by the system, it does not necessarily mean that the results are what are desired. Therefore, manually calculate the answer for a few test data conditions to insure that the function is working as plenned.
12. (Optional) When Correct, See If the Function Can Be Shortened.

Because APL executes in an interpretive mode, the more lines of code there are, the longer execution will take. Therefore-if you have time and/or the function is likely to be used frequently--investigate ways whereby one or more lines of code can be combined into a single line.
P.S. Don't forget to save a copy of your now-correct function in your stored workspace.

### 5.2.2

Signing-On to the UCLA APL System

# INTERACTTVR COHPUTTN FOR MANAGEMENT <br> moucators 

## NAME

## APL NUMBER

PASSNORD

NEW PASSWORD

## SIGEING-ON

1. TURN THE TERMINAL ON BY FLTPPING THE ON-OFF SUTTCH ON THE LFFT OF THE KEYBOARD.
2. PICK UP THE PHONE AND DTAT ONE OF THESE NUMRERS: 50911, 50921, 50931, 50941 OR 50721. WHEN YO! HEAR A IIGU DITCHFD TONE, PLACE THE HEADSET ON THE TABLE AND PRESS DONN TIE SIMVRR BUTTON TH THE CRADLE OF THE PHONE. TIE ON-LINE LIGTT OA THF LEFT GTDE OF TAF KEYBOARD GHOHLD COMF ON.
3. TYPE '*' (UPPER CASE P) FOLLOEED RY ' $\because$ ' (IPPER CASF A) GOLLOWED BY ')' AND PRESS 'RRTURN'; EXAMRLF * TIE COMPUTER YILL RESPOND HITH THE MESSACE 'YNCORPECT SICN- ON' AND PRINT A SHORT ITIE OE OUFRSTOUCK CHARACTERS TO OBSURE THE NEXT TYPED ENTRY.
4. TYPE YOUR APL NUMPEP AND YOUR PASSNORD: EXAMPLE ) $1234: M C L E A N$ (DO NOT FORGET THE PIGHT PARFHTHESIG BEFORE YOUR APL NUMBER AND THE COION BEFORE YOUR PAGSVORD).

## ERRQR_CQRRECTIOR

1. STRTKF TIR BACKSPACE KEY TO MOVE TIE CARPIACR OVER TO WHERE THE FRROR BTGJNS.
2. HIT TAE JNDEX VEY ON TUF UPPRT PTDE STDE OF THE KRYROARD. AN INVERTED CARET (V) WITI APPEAR UIVDFR TIE CHARACTEP AT TIAT
 FROM THE MFMORV OF THE SYGTEM.
3. TYPF THE CORRECTTON AND THF RPMATHDE? OF TIE LINE.

SIGUING-OETB

1. TYPE JOFE OR )CONTINUF AND PRESS 'RETURN'.
2. TURN OFF THE TERMINAL.
3. PLACE THE PHONE IIEADSET BACK TN THE CRADLE.

SICUING-ON

1. TURN TUF TERMTNAT ON RY FLTPPINF THR ON-OFF SWITCH ON THE RIGHT OF 'JHE KEYROARD.
2. CHECK TAE CNALI SWTTH LOCATED TN THE FROIT LEFT CORIER, UWDER THE KEYBOARD, AND SFITCH TT TO THF RICITT.
3. PICK UP THF PHONE AND DTML ONE OF THECE NHMBERS, 50911. 50921. 50931, 50941, 50721. $H 1 F N$ YOU HFAR A HTGA TTICHED TONE, INSERT TIE PHONE HEADSFW TNTO THE COUPLER, MAKING SURE THE CORD END IS ON THE CORRECT SINE. THE LTCHTS 'C' AND 'S' MUST BE ON IF THE CONNECTION IS MADF.
4. TYPF 'A' FOLLOYPD BY '9' FOLLOTED BV ')' AND PRESS 'RETURN'; EXAMPLE: A9) (CMRPIAGE PFTURN). THE COMPUTER RESDONDG FITH THR MFSSAGF, 'THCOPRRCT STGN-ON' AWD DRTNTS A SHORT LINE OF OVERSXRUCK CHARACTFRG TO ORGURE TYE NEXT TYPED ENTRY.
5. TVPE YOUP APL NUMPPR AND VOUR PAGGWORD; EXANALF: ) 1234: MCLFAN (DO WOT FORGET THE QTGHT PAREWTIESIS BEFORS YOUR APL NUMBER AND TME COLON BEFORE YOUR PASCHORD).

EERQRGQRRTCIQN

1. STRIKE TUE RACKGPACE KEY TO YOVE OVER TO WHERE THE ERROR BEGIMS.
2. HIT THE ATTENTION KEY (ATTN) IN THE UPPER RTGHT HAND CORNER. AN INVERTRD CARET (V) UTIL, APPEAR INDDR THE CHAPACTER AT THAT POINT. EVFRTHING AROVQ AND TO THE RTGHT OF THE CARET IS WIPED OUT FROM THE MEMORY OF TIE SYSTEM.
3. TYPE THE CORqFGTTON AND TIE RFMAINDER OF TIE LTNE

SICNING-OEE

1. TYPE: ) OFF OR CONTINUE AND PRESG 'RETURN'.
2. TURN OFF THF TEPMTNAL AND THE ACOUSTTC COUPLFR.
3. REMOYE THE TPIRPIOME HEADSET EPOM THE COUPLER AND HANG UP.

## TRM 2741 TERMTNALG

SICNIMO-ON

1. TUR! THE TRPMJNAI, QN BY FLTPPINC THE ON-OFF SWITC! ON THE RIGHT OF TIE KEYROARD.
2. CHECK THE GHTTC! ON THE LEFT GIDE OF THE TERMINAL, IT SHOULD BE SET TO COM NOT LCI.
3. PJCK UP THE PHONE AHD DTAL ONE OF THESE NUMBEDS, 50911, 50921, 50931, 50941, 50721. WHEN YOU HEAR A HIGH PITCHED TONE, INGERT THE PHOHE HEADSRT IHTO THE COUPIER, MAKTWA SURE THE CORD END IS ON THE CORRECT CIDE. THE LTCHTS 'C' AND 'S' MUST BE OA IF THE conmection is made.
4. TYPE 'A' FOLIOMRD BY ']' $\operatorname{GOLLOWED~BY~')'~AND~PRESS~'RETURN':~}$ EXAMPLE: A]) (CADRTACE RETVPil). THE COMPUTER RESPONDS WTTH THE MESGAGE, 'IWCODRECT GTCH-ON' AND PRTNTS A SHORT LINE GF overgtruck characmens to nbsure the next typed entry.
5. TYPE YOUR AFL NIMRED AND vOID PACSWORD: EXAMPLE: )1234:MCLEAN (DO WOT FORGET TIIE RTCHT PADENTHESIS BEFORE YOUR APL WIMBER AND THE COLON EEFORR VOUR PAGS!ORD).

ERROK_CQRRCCTIQN

1. STRIKE THE BACKSFACE KEY TO MOVE OVER TO WHERE THE ERROR BEGTIG.
2. HIT THE ATTEUTIOU KEY (ATTN) TN THE UDPRR RTGHT HAND CORNER. AN IUVRRTED CARET (v) VILL APPEAR UNDER THE CHARACTER AT THAT poIHT. EVERTILIN ABOVE AND TO THE DTGHT OF THE CARET JS WIPED OU'T GROM THE MFMORV OT TIE SVGTEM.
3. TvPE THE CORPRCTION AND THE REMAINDER OF THE LINE.

## GIGNING-OEF

1. IYPE: )OFF OR )COHTINUE AND PREST 'RETUPN'.
2. TURA OFF THE TERMTVAL AND T:HE ACOUSTTC COUPLER.
3. reanve the telfplone meancfit from the coupler and hang up.

### 5.2.3

An APL Bibliography
APL: The Language and Its Use
R.P. Polivka and S. Pakin

# Raymond P. Polivka and Sandra Pakin, THE LaNGUAGE AND ITS USAGE, (C) 1975, Pp. 545-569. Reproduced by permission of Prentice-Hall, Inc., Englewood Cliffs, New Jersey. 

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This APL Bibliography is organized in sections as follows:
General: Articles that tell about APL or that describe it generally.
Texts: ‘Books for learning APL.
Applications: Books and articles discussing uses of APL and applications in education, business, engineering and science, computers and computing, mathematics and statistics, and miscellaneous.

APL developments: Articles discussing extensions to APL and/or the APL terminal system.

Miscellaneous: Articles of interest to the APL programmer.
Collections: APL journals and conference proceedings.
The bibliography is rich in source materials with the following exceptions. No books or articles written prior to 1968 are included. 1968 was chosen as a cutoff date because APL/360 was not made publicly available by IBM until then. Earlier references tend to use Iverson notation (as formulated in A Programming Language, Wiley, New York, 1962) rather than APL. Neither articles nor manuals discussing specific implementations of APL on various machines or by various companies or universities nor how APL is used at various installations are included since such information tends to be transient. No foreign language articles are included. Finally no articles whose distribution is restricted are included.

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## 5.2 .4 <br> "Things Go Better with APL" <br> Claire Stegmann <br> Think <br> May/June 1975

## by Claire Stegmann

Tom Ryder, a Salt Lake City businessman, picks up his weekly payroll at a computer service bureau. He stops for a Coke. Then it's back to his office in his Citroën for an appointment with an ibm salesman. He's considering a computer of his own; and he'd like to have it by the time his son, just graduating from M.I.T., joins the firm.

Ryder might be surprised to learn that everything he has just done is involved, in some way, with the computer time-sharing language, APL.

- The customer service bureau he uses, which offers APL service, is operated by Management Systems Corporation, a wholly owned subsidiary of the Church of Jesus Christ of Latter-day Saints. The Mormon Church, as it is more commonly known, also uses APL in many of its own operations.
- Both The Coca-Cola Company and Citroën are increasing users of apl.
- The ibм salesman, to help Ryder tailor a computer to his particular needs. will almost certainly consult a terminal in his branch office for design analysis and to find out what ibm products and services are available, and where. That terminal is tied into the Data Processing Division's hone (Hands-on Network) system, which makes significant use of APL.
- If Ryder decides to order. the System Products Division's worldwide commodity planning system, based on APL, will enable SPD to provide the earliest possible delivery date.

Incidentally, Ryder's son, back at M.I.T., uses API. to do his homework. And he and his father share another Apl-based activity: the National Football League statistics they follow so closely are compiled with the language.

Ryder and his son are fictitious. But the APL applications are real. They illustrate the versatility of $A$ Programming Language, which has come into its own as an important product for the computer user.

For most of its 13 years, Apl's primary habitat has been the classroom, where, as an extension of simple mathematical notation, it has helped high
school and college students learn not only algebra, but also economics and electrical engineering. In Atlanta, students use it to design and compute the cost of making cabinets.
ibm Fellow Dr. Kenneth Iverson, who invented APL as a precise way to describe data processing, explains: "Every field of human knowledge that deals in quantity-mathematics, physics, economics-has a special vocabulary that must be put into a generalpurpose language for computer use. APL defines these terms by their simple mathematical formulas, using a number of symbols, some of them (for example,,,$+- \times, \div$ ) already familiar to every school child. Thus, as a student learns Apl, he or she is also reinforcing knowledge of a particular discipline."

Dr. Iverson believes that ApL's versatility as a teaching aid has barely been touched. Much of his work as a Fellow is devoted to helping educators in many fields study its application to their particular specialties.

But, according to Dr. Truman Hunter, APL manager, because API is relatively simple to learn, versatile, and interactive (the user and the computer "converse" during the processing of a job), it is becoming more and more attractive to business for management decisions that need frequent updating and quick response.
"This has been especially truc," says Adin Falkoff, Dr. Iverson's longtime collaborator. "since the introduction of an APL. program product calied the API. Shared Variable System. This makes it efficient and convenient to work with files and data bases." Both APISV and APL/CMS (Conversational Monitor System), recently introduced by IBM, enable the API. user to do a greater variety of jobs on a much larger scale than before.
"It is the analytic power of API, the language," says Dr. Hunter, "plus the easy access to large stores of information, that I think is going to make it increasingly important to the businessman. Now, more than ever, he can


develop applications and get results while they are still timely."

APL and its conversational cousin basic are by far the most widely used languages specifically designed for terminal use, which allows the user to bypass such time-consuming steps as going to. and queuing up in the computer room. Of the two, basic is older and more widespread. But, according to Curt Bury, DPD senior product administrator, APL's inherent power is extending its effectiveness to areas beyond the scope of basic. An ibm operations planner agrees: "We planners have to sort out a great many complex relationships in a very short time. API is the only game in town for this kind of thing."

IBM's accelerated use of API since it was first introduced in the midSixties. on the IBM 1130 and System/ 360 Model 40 and above, reflects the recognition of the language by data processing people as an effective way of getting applications written faster. "In the past several years," Data Processing Division President John F. Akers told a GUiDe user-group last year, "we have gone from 4,000 to 16,000 apl users within ibm. And the balance has shifted from scientific to commercial users."

Every ıвм division relies on the language in some way. DPD's HONE system. which connects U.S. branch offices to a central data base and makes heavy use of apl programs, made a tremendous contribution to field productivity. In what is possibly the largest single use of API., SPD's commodity planning system integrates production schedules so efficiently that decisions that used to take two months can now be made within a matter of minutes. The General Products Division depends on ApI. to write test cases for its new 3850 mass storage system. Many aspects of the business of 1 ibм in Europe, according to Yves Le Borgne, advisory apl support representative in Europe, are managed from ApI, terminals. I BM World Trade Americas/Far East Corporation has used apl to develop applications for both its oper-
ating plans and its strategic planning.
Office Products Division engineers use APL in the development of Copiers and magnetic keyboard typewriters. opd, incidentally, has another interest in the language. It makes the apl. Selectric typing element.

In a move that brought APL into the mainstream of IBM software production, the apl group was transferred last year from dpros Pbiladelphia Scientific Center into sdD. A design group, consisting of Iverson, Falkoff, Richard Lathwell, and a small staff, remain in Philadelphia. The implementation group, under L. A. Morrow, joined the SDD programming center at San Jose. "We consider apl. one of the primary interactive environments for current and future systems," says R. E. Ruthrauff, SDD manager of language and data facilities advanced system design.

One strong advocate of interactive computing, and of APL in particular, is Professor Ephraim McLean of U.C.L.A.'s Graduate School of Man-
agement. He introduced apl to the business school four years ago. Today, it is a requirement for all entering M.B.A. students.

This summer, with an ibm grant, Professor McLean will offer a course on interactive computing to a limited number of faculty members from other business schools. "I have been surprised at both the number and the variety of requests for applications," he comments. "They come from all over -a Jesuit priest, a woman marketing professor, a faculty member from Howard University, several individuals from both French and Mexican universities, and a surprisingly large number of business school deans and department chairmen."

Next, McLean hopes to do a study on the increased effectiveness of APL users. "I think a study will find that API. is much more productive," he says. "For instance, I am convinced that with APL a programmer can accomplish in 10 instructions and a few hours what

## Here's how it works

One of the virtues of APL is that it is interactive. that is. a person can "converse" with the computer during the processing of a job. Here is a simple example of how such a conversation might go:

Let's say a businessman wants to examine the feasibility of taking out an $\$ 8.000$ loan at $91 / 2$ percent interest. He wants to see what his monthly payment would be each month if he repaid the loan over an eight-year period. Also, for income tax purposes, hed like to know what his annual interest would amount to each year.
Now, let's assume that the APL program to perform this function is identified in the computer as ME. The businessman begins by typing

## M E

The computer responds:


The computer comes back:
ENTER MONTH AND YEAA THAT EIRST PAYMENT IS DUE (E.G. 873 FOR AVG, 1973)

## The businessman types:

## 575

The computer prints out: PAYMENT AMOUNT IS 119.29

| END OF | ANNUAL | PRINCIPAL | END OF | ANNUAL | PRINCIPAL |
| :---: | :---: | :---: | :---: | :---: | :---: |
| YEAR | INT. | REMAINING | YEAR | INT. | REMAINING |
| 1975 | 494.05 | 7539.73 | 1980 | 340.52 | 2984.95 |
| 1976 | 684.30 | 6792.55 | 1981 | 232.24 | 1785.71 |
| 1977 | 610.15 | 5971.22 | 1982 | 113.23 | 467.46 |
| 1978 | 528.63 | 5068.37 | 1983 | 9.28 | .00 |
| 1979 | 439.02 | 4075.91 |  |  |  |

might take 200 instructions and several days in COBOL or FORTRAN."

One of the beauties of APL, says Dr. Iverson, "is that you have to learn so little to get started, like a child, or a grownup for that matter, learning a language. You tell a child two or three things and he builds his vocabulary gradually. With APL, you gradually accumulate a knowledge of the symbols as you do more and more work."

Several clerks and secretaries in town halls near Paris would probably agree. They have never seen a computer but are using terminals, and APL, to do payrolls they formerly did by hand. "Here in Europe," says Yves Le Borgne, "we are confident that api. has a great deal to offer our customers --especially now, with the economic crisis, when there is a need for better management to grasp a situation and react to a changing environment quickly."

In May, Iverson receives the annual Harry H. Goode Menorial Award from the American Federation of Information Processing Societies, for the impact Apl is expected to have on programming language theory and practice in the future. The setting would be the envy of many youngsters: Disneyland, in California. But it probahly wouldn't impress the son and daughter, both under nine, of IBM senior programmer Corey Fair in East Fishkill. Since the Outstanding Contribution Award winner (for his part in development of the SPD commodity planning system) brought a terminal home, his kids don't watch Walt Disney on TV much anymore. Instead, they compete for time on the terminal. when allowed, to practice Apl.

## Think

May/June 1975

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## 5.3

APL Programming Assignment Instructions

# INTERACTIVE COMPUTING FOR MANAGLMENT EDUCATORS 

Graduate School of Managrment University of California, Los Angeles

## APL PROGRAMMING ASSIGNMENT

In applying to this program, each of you described, in varying degrees of detail, the problem or application that you wished to program in APL during the second week of the course. The resulting programs are to be published as a UCIA monograph.

In order for this aspect of the course to be successful, it is vitally important that you prepare for this exercise prior to arrival. Although you of course know nothing about APL, it is reasonable to expect that you should have a good understanding of the application which you intend to program. Toward this end, the following is a list of items that, to the maximum extent possible, should be prepared prior to arrival and brought with you.

1. A concise statement of the problem, application, game, student exercise, or other use you wish to make of the computer in an interactive mode. This should include how you expect the program to be used (as drill-and-practice, gaming or simulation, probien-solving, etc.), by whom (e.g., beginning undergraduates, managers, advanced M.B.A.'s, etc.), and to what end (i.e., what is the object of the program; e.g., to attack problems too complex for hand solution, to reinforce materials already presented by traditional means, etc.). Also included in this should the formula, algorithin, or other logic required to arrive at the solution, result, etc. This is similar to what you put in your appli.cation questionnaire, but unfortunately mosi of them were rather sketchy.
2. A general description of how the program works and what the user can expect from it. This statement, which will naturally be refined after you arrive, will be the kind of documentation you would like to see accompany your program in published form. It should include a specification of the inputs, parameters, and other variables that are nec.essary on the part of the user in order to make the program work. For example, in a simple program to calculate the terminal value of $\$ \mathrm{l} .00$ invested at compound interest, $\underset{\sim}{i}$, for $N$ periods, the user must be told that he needs to supply both i and N.
3. Data which can be used to test the program. These data should be of two types: one should be sample or typical data such as would be used to illustrate the use of your program; the other should be a wide range of data designed to test all possible conditions (e.g., what if a user tries to run the program with zero - or an unreasonably large number? what happens if some input is missing? etc.) In other words, try to think of all the ways the progran might be used - correctly or incorrectly - and then devise data to test these possibilities.

For some of you with little or no experience in computing, you may feel that it is extremely difitcult for you to compile such information prior to the berinning of the course; but it is important that you try, for without having carefully thought through the problem that you wish to undertake, you may find that the two weeks are over before you have hali begun.
6.0
PROGRAM ADMINISTRATION
AND
PROMOTIONAL MATERIALS
6.1

Program Announcement Brochure

## INTERACTIVE COMPUTING

FOR
MANAGEMENT EDUCATORS

June 29 - July 11, 1975


GRADUATE SCHOOL OF MANAGEMENT

UNIVERSITY OF CALIFORNIA LOS ANGELES

## THE PROGRAM

An intensive two-week program, supported by a grant from the IBM Corporation, will be conducted by the Graduate School of Management at UCLA from June 29 to July 11, 1975. Its purpose is to introduce faculty members from business schools and colleges throughout the country to the use of interactive computing in management education.

Unlike other programs which have been offered elsewhere and which have dealt with the use of FORTRAN and computer batch processing, this new program will focus upon the advantages offered by timesharing languages for the teaching as well as for the practice of management. Specifically, it will cover the following four areas:

1. The use of conversational, interactive computing in business.
2. The APL programming language as a new and powerful means for providing this interactive capability.
3. The methods for teaching APL to business students.
4. The ways in which APL can be used for teaching accounting, finance, operations research, and other management subjects.

For many faculty members who have made little or no use of computing in their teaching, the mastery of a computer language represents a substantial hurdle. They feel that in order to use computers they must first learn a batch processing language, with all the accompanying intricacies of the job control language, before they can move on to a time-sharing language like APL.

Such views are unfortunate, for they preclude many teachers from taking advantage of the assistance of the computer because of this perceived high start-up cost. Therefore, it is the intention of this program to help overcome this barrier and to make the transition from non-use to informed use as easy and painless as possible.

Toward this end, the use of APL is particularly appropriate, for it is both simple to learn and yet powerful to use. Rapidly growing in popularity, this conversational, interactive computer language is being used in such dissimilar industries as manufacturing, insurance, and transportation. It is also widely available through commercial time-sharing services.

As a prerequisite to attendance, each participant will be expected to define a potential application in his or her own area of specialization prior to arrival. (This involves specifying a learning objective, structuring the problem or exercise, and gathering the data necessary to test and illustrate the use of the resultant program.) After arrival, this application will be coded into APL. In this way, not only will the participants be able to acquire a deeper understanding of APL relevant to their own discipline, but they will also have produced working programs (or series of programs) which can be put into use immediately upon return.

These programs, identified with the author's name and accompanied by a description of their use, will be published as a monograph after the completion of the program. Copies will be furnished to all participants, to the IBM Corporation, to member schools of the American Assembly of Collegiate Schools of Business (AACSB), and to other interested parties.

Participation is limited to 24 faculty members. The cost of the program, as well as all of the living expenses of the participants while they are at UCLA, will be borne by the sponsoring grant from IBM. Travel costs to and from Los Angeles are not included.

## TOPICS TO BE COVERED

## 1. Introduction to Computing Concepts

A brief overview of computer terminology and technology, covering the general functioning of computer systems, especially those supporting time-sharing services.

## 2. Introduction to APL

A description of the concept and background of APL, including a demonstration of its various features.

## 3. The APL Functions

The complete set of APL primitive functions, showing their use in conjunction with scalars, vectors, and matrices.
4. User-Defined APL Functions

The writing of programs, or, in APL terminology, the defining of one's own functions.

## 5. Systems Commands and Workspace Management

The concepts of public and private libraries, the manipulation of workspaces and their contents, and the functioning of the various systems commands.
6. Report Generation

The preparation of reports, both in a tabular and a graphical mode.
7. File Systems

The concepts of shared variables (SV) and file systems (such as STSC's APL Plus File System).
8. Programming Techniques

A number of APL programming procedures and techniques, exploring the best of current practice.
9. Application of APL to Business

The applications of interactive computing to diverse business problems, drawing upon the experience of the instructional staff, outside speakers, and the program participants.
10. APL as an Aid in Management Education

The use of APL to help teach accounting, finance, operations research, and other disciplines; also, the participants' development of their own applications.
11. Methods for Teaching APL

The teaching strategies used at UCLA over the last four years in introducing APL to well over a thousand M.B.A. students.

## THE FORMAT

The program will begin on Sunday, June 29th, and end on Friday, July 11 th. A reception and welcoming dinner will be held on Sunday evening, with classes beginning the following morning.

All classes will be held at the Graduate School of Management (GSM) from 8:30 A.M. to 5:30 P.M. each day, with the evenings and middle weekend free for studying or recreation.

The participants will be split into two groups of twelve each. One group will attend a lecture while the other works in the computer laboratory. Every two hours the two groups will switch. This allows for small class sizes and maximum individual attention.

Of the three instructors associated with the program, at least two will be lecturing or assisting in the lab at all times. Over the two-week period, each attendee will have 34 hours of lecture and 44 hours of laboratory time, including the programming of his or her own application program.

## WHO SHOULD ATTEND

The program is designed for those business school faculty members who wish to enhance their teaching skills by applying the power of interactive computing to their area of specialization. There is no need to have had any previous experience in computing. Therefore, those who have never used computers, as well as those who had had some programming experience, are invited to apply.

The selection of the 24 participants will be governed, at least in part, by the desire to obtain a broad cross section of disciplines, functional areas, and representation from among AACSB member schools. In the event the program is oversubscribed, all applications for attendance will be retained in case a subsequent offering is possible.

## Requests for applications should be sent by March 15th to:

Dr. Ephraim R. McLean<br>Graduate School of Management University of California<br>Los Angeles, California 90024

## the faculty

EPHRAIM R. McLEAN, Program Coordinator
Professor McLean is presently the Director of the Center for Information Studies, and was formerly the Chairman of the Computers and Information Systems Curriculum Committee, both at GSM. Instrumental in bringing APL onto the UCLA campus, he taught the first regularly-scheduled course in APL at UCLA and has taught it every year since. In conjunction with Professor Siler, he has taught APL to over a thousand graduate students. When the widely-used book APL: An Interactive Approach (which is to be the primary text for the program) was'recently revised in preparation for the second edition, Professor McLean was retained by John Wiley \& Sons as a consultant on the revision.

## KENNETH F. SILER

Professor Siler, the other faculty member associated with the program, is the current Chairman of the Computers and Information Systems Curriculum Committee and has worked closely with APL for the last two years.

## JAMES W. SCHENCK

Mr. Schenck, the third member of the instructional staff, was formerly the Coordinator of Computer Services for GSM and is currently a doctoral student in the School. He is one of the co-authors (with J. W. Buckley, M. R. Nagaraj, and D. L. Sharp) of Management Problem-Solving with APL, (Los Angeles: Melville Publishing Co., 1974), another text in the program.

## ACCOMMODATIONS AND FACILITIES

All of the participants will be housed at the Holiday Inn in Westwood, immediately adjacent to the UCLA campus. A special bus will furnish transportation between the motel and GSM. Meals will be provided at the Holiday Inn and at the UCLA Faculty Center, or participants may choose to dine at one of the many restaurants in Westwood.

The lecture and laboratory sessions at GSM will be conducted "on-line." For lectures, the air-conditioned classroom will be equipped with a computer terminal and with closed circuit television so that everyone in the room can follow the output directly.

The computer laboratory, a carpeted, sounddeadened room equipped with 12 computer terminals, will be reserved for the exclusive use of the participants during the program. In addition, a number of other terminals located within GSM will be available on a first-come, first-served basis. A portable terminal will be placed in the Holiday Inn so that participants may work in the evening without having to return to GSM.

With regards to the terminals themselves, GSM has a wide assortment, including A.J. 841's, IBM 2741's, G.T.\&E. 5741 's, and Tektronix 4013 graphic terminals. The main support computer is the UCLA Campus Computer Network's IBM 360/91 with four million bytes of main storage. Two commercial companies, Proprietary Computer Systems and Scientific Time Sharing Corporation, are available as back-up, if necessary, to insure uninterrupted service.

## 6.2 <br> Invitation Letter to <br> Business School Deans



15 January 1975

## Dear Dean

It is my pleasure to invite your participation in a program that I know will be of interest to you.

With the use of computers expanding on every front, it is difficult for those of us in the academic world to keep up with these developments, let alone employ them in our own educational programs. Significant among these developments is the use of conversational, interactive computing. With this capability being increasingly employed in rovernmont and industry, it is unfortunate when the students we are graduating are not familiar with this powerful aid to manarement. But before our students can use this technology, our faculty must first become comfortable with it. This brings me to the purpose of this letter.

Next summer, a program is being offered at the Graduate School of Manarement here at UCLA on the subiect of Interactive Computing for Manarement Education. The enclosed brochure explains this program in detail.

Made possible by a generous grant by the IBM Corporation, this twoweek prorram provides an opporiunity for 24 faculty members to attend an intensive workshop in the use of APL for management education. All of the expenses connected with attending will be borne by the IBM frant, with the exception of the travel expenses to and from Los Angeles. In this way one or more of your faculty members can substantially uprrade his or her skills by participating in a profram which, if taken commercially, would cost the individual several hundred dollars.

In offering this procram, we belleve that we bring to it a perspective and a measure of experience that is unique in the country. The program will be directed by Dr. Ephraim R. McLean who was instrumental in bringing the interactive computer language ApL to the UCLA campus several years ago and is widely regarded as one of the leaders in the country in its application to management education.

## Page 2

As is described in the brochure, there are only 24 openings in the program, so it is possible that there may not be room for everyone who wishes to attend. May l urge you therefore to bring the enclosed material to the attention of those of your faculty whom you feel would most benefit by attending and have them forward their application to Dr. Mclean. It is not necessary that they have any previous experience with computing or that APL is currently being used on your campus.

I am excited by the promise of this program and hope that you share my enthusiasm. May we hear from you, or from your designated faculty member, in the near future?

Sincerely,

Harold M. Williams
Dean

Enclosure
6.3

Publicity

## ADVANCES IN INTERACTIVE COMPUTING

"Today the computer is as natural an educational tool as paper and pencil for the Tuck students, and their ability to solve operational problems with quantitative computer techniques is highly attractive to prospective employers." Tuck Today

Seventy-five percent of AACSB schools responding to our 1974 survey have time/sharing capability. That compares to 43 percent in the 1970 survey. What are the advantages of $T / S$ over batch prosessing? Each year our March issue is dedicated to that question.

We begin our comparison with an update of Darmouth's T/S approach. During our 1966 survey, 11 schools were visited. Of those 11. Dartmouth's Amos Tack Sehool of Business proved to bic a barometer of T/S potentialities. Weve revisited that campus durine each of our triennial surveys. As in previous visits. Tuck revealed some characteristics which can be cmulated by other schools-even schools with very modest computing budgets.

## Objective in Computer Education

When asked the principal objective in educating Tuck students ahout the computer. Dean John Hennessey responded. "to acquaint students with the power of the computer as an aid to decision making analysis-an aid to thought-for the practicing manager." Dean Hennessey then expanded this concept: "We want to make sure our students are not in any way frightened by the computer.

We hope that at least students will become familiar with the idea of computers as a natural part of the managerial environment. Also, we want students to know how computers will be directly and indirectly useful to them in their work here at Tuck."
Motivating the Faculty to Computer Use
For a decade. Tuck's faculty has been highly computer-oriented. In the carly 1960 's Dean Karl Hill acquired an IBM1 1620 and installed it in the Tuck Schooi hasement. His approach was to make computine resources available - both equipment and advisors. Gradually the faculty began to utilize thowe resources. I asked Dean Hills successor the approach to motivating new faculty to acquire a computer capability". Dean Hennessey replied. "When a new faculty member arrives on our campus he recognizes that everybody else is using the computer as a natural part of their
environment . . . almost as easily as telephones are used. I use it myself-its required of me in order to access the management information systen which President Kemeny has installed as a part of Dartmouth's administration. ... It's a rare faculty member who wouldn't want to be a part of our computer activities."

Asted if a requirement for faculty proficiency was then implicit, rather than cxplicit. Dean Hennessey agrecd. "There are far more persutsive and lasting ways to influence people than telling them what to do. . . The mandate from their colleagues and their students to use the computer is much more powerful. For example. a new faculty member in finance is quickly going to find that other faculty ask the students to use the computer in several ways. So. faculty in any kind of quantitative area would tahe it up inmediately: A new faculty member in a non-quantitative area finds fairly quickly that he would want to be acquainfed enough with computers to understand what students mean when they come to him and say 'I want to do an independent study project and "m going to use a computer the following way in your field'."

## What's New at Dartmouth?

All three AACSB surveys indicated the importance of faculty participation for achieving a viable computer curriculum. Even an extremely capable instructor in the core computer course will not be able to convince students of the value of the computerthat value must be demonstrated through assignments in subsequent courses. Dartmouth has shown the way to create such an environment. Computer proficient faculty in the functional area courses encourage students to use the computer to acquire greater depth of knowledge in each subject area.

Such an environment is not dependent upon, but is facilitated by timesharing. Ease of access is a principal motivator-to both faculty and students. Page 2 will describe some $T / S$ innovations at Tuck School.

## SUMMER FACULTY EDUCATION PROGRAMS

## UCLA

A two-week faculty education program. supported by a grant from the IBM Corporation. will be conducted by the Graduate School of Management at UCLA from June 29 to July 11. 1975. Its purpose is to introduce faculty members from business schools and colleges throughout the country to the use of interactive computing in management education.

Specifically, it will cover the following four areas:

1. The use of conversational, interactive computing in business.
2. The APL programming language as a new and powerful means for providing this interactive capahility.
3. The methots for teaching APL. to husiness students.
4. The ways in which APL, can be used for teaching accounting, finance. operations research, and other management subjects.

## No Cost To Participants

Participation is limited to 24 faculty members. The cost of the program, as well as all of the living expenses of the participants while they are at UCI A, will be borne by the sponsoring grant from IBMA. Tinvel costs to and from Los Angeles are not included.

## Who should Apply

The program is designed for those business school faculty mem-
bers who wish to enhance their teaching skills by applying the power of interactive computing to their area of specialization. There is no ned to have had any previous experience in computing.

Selection of the 24 participants will be governed, at least in part. by the goal to obtain a broad cross section of disciplines, functional areas, and representation from among $\triangle A C S B$ memher schools.

Although the cutoff date is March 15 , if you immediately telephone Dr. Ephraim Mclean. it is possitile to have your application considercd. (213) 825-7982.

## SUNY-BINGHAMTON

Although not formulated at this time. another 3-weck Summer Institute in APL will be offered at SUNY-Binghamton in 1975.

The insitute is largely morivated by numerous requests from APL users and potential APL users from academia and indusiry for various APl. techniques. APL applications. and API, curricular development topics. The three-week syllabus involves: Elementary APL., APL packages, and Advanced APL.

Sessions are suitable for anyone from academia or industry. For complete death, session outlines, fee sheets. and registration Forms contact Geraldine McDonald, Computer Center, SUNYS nghamton. Binghamotor. New York 13901.

## USE OF APL IN MANAGEMENT EDUCATION

Prof. Ephraim AcLean (UCLA) presented a paper of this title at the Sixth International APL Users Conference in May 1974. His school now teaches APL in the introductory data processing course in the School of Management. The following excerpts from his paper support the school's decision.

During the school year 1971-72, UCLA, in collaboration with Scientific lime Sharing Corporation, installed the latter's APL Plus system. This
system. now in use by over ten other university computing centers, con tains a nunber of APL, enhancements. Among them are additional sys tems commands; powerful formatting functions for outputting data: shared file system permitting AI'L, for the first time, to handle significant sized files; and an AI'L-batch file interface a!lowing high speed input output devices to be used instead of the requirement of having to enter all data through the terminal. The i:mportance of this file handling capability will become more apparent when some of the applications are diseussed.

In reviewing use of APL with other busincss educators across the country, the question which most commonly arises is: "But why Jon't you use BASIC?" UCLA first hoped that both would be available. The campus computer center agrced to support only one. The school selected APL. for the following reasons: 1. APL is easy to learn. Although the special symbols and character set are a little strange at first, they are quickly mastered and their power and conciseness are soon appreciated.
2. APL is unique. APL's powerful operations and matrix-handling ability set it apart from other languages. But this supposed "disadvantage" arises only if students do. in fact, go on to some other language. However. most students find little reason to move on to some other language. And again, UCLA's emphasis is on developing problem-solvers and decision-makers-not journeymen programmers.
3. APL is widely available. APL has been implemented, in one way or another. by almost all computer manufacturers. It is true that the number of different machines for which BASIC interpretive compilers presently exist is greater than for APL. Also. tecause of APL's greater power and correspondingly preater memory requirements, it is unlikely that it will ever be implemented on any of the mini-computers. Finally, in terms of the number of service bureaus, again far more are offering BASIC than APL. However. the average user typically does not care whether a language is avalable on five machines or fifty; his main concern is. "ls it available to me?" The answer. in most major cities in the U.S.. is yes; and the availability of APL appears to be growing.
4. APL has large libraries of programs. The number of APL prozrans in the putlic domain is quite large. It is true, of course, that they are nowhere near as numerous as those in BASIC. but the APL libraries are growing rapidly, fueled by such major users as IBM1 itseif and by American Airlines' comprehensive APLbased managenent information system.

Although BASIC might have an edge at this point. APL is gaining so rapidy that soon the number of available programs, as well as the number of companies offering time-sharing services, will result in differences that are more apparent than real.

## Business School Applications

## 1. Finance

Capital budgeting is one area in which a fair amount of work has been done. Such variables as cos! of capital, differing depreciation schedules and tax treatments, variable income streams, and nrovisions ior risk can all be taken into account and tested for their relative sensitivity.

Two examples of specific assignments which have been undertaken involve comptiter acquisition and property tax evaluation. In the first case. the irequently-encountered problem of whether to lease or buy computer hardware was studied. Discount rates, equipment configurations. expected operating. schedules (e.g., one shift or two. and charging and pricing algorithms were all varied to arrive at the most desirable solution. In the second case, a real estate company: capital asset management was partially dependent upon local property tax rates. so the extent of this sensitivity was analyzed.

Another application in the financial area is the use of corporate financial data from such sources as Standard and Poor. Financial ratio analysis across companies or over time has been undertaken. Also. various types of financial forecasting and trends analysis have been studied through the use of regression techniques and time series analvsis. Finally, in the field of investment portfolio ielection, the study of rish by means of beta factor analysis has seen done.

## 2. Statistics.

With the availability of STATPACK2 from the University of Alberta, as well as other statistical tools in the APL public library,
a varicty of problems can be investigated. In a course on measurement theory, analysis of variance and problems of data transformation were studied. For statistics classes. both classical statistics problems (e. g., determining sample sizes and tests of significance) as well as Bayesian statistics (c. g., decision tree analysis) have used the students' APL background to good effect. Correlation, regression, and analysis of variance applications of various types are undertaken; and, in decision theory, much of the calculation drudgery has been eliminated through the use of APL modules without sacrificing the mastery of the concepts.

## 3 Planning and Control.

Of the several courses within the school that focus on planning and control, one is built almost entirely around the use of APL. Student teans have developed planning models, each in a setting of their own choice. In creating these planning systems, stress is placed on the importance of the user-interface and upon sueh issues as data and file management, security features, and realworld feasibility.

## 4. Operations Research.

By using a variety of programs in the public library, students are able to attack nonlinear and integer programming problems which, because of the need to solve a linear programming subprogram for each iteration, are usually so long that only the simplest are assigned. Now, with APL routines to handle the L. P. calculations, students can devote their attention to understanding the underlying nonlinear or integer algorithm. Resource allocation decisions and transportation and shortest route problems are regularly assigned and students can perform a number of sensitivity analyses on constraint variables and coefficients of the objective functions.

Some simulation and model building is also being done, but the interpretive nature of APL makes the execution of problems of this sort fairly costly if the number of iterations is high. It is in instances such as these that the quality of the coding becomes critical. Poorly or inefíiciently written programs can be intolerably expensive, while the same program carefully written to take full advantage of the power of APL can be much more cost effective.

## 5. Management Gaming.

Probably the most extensive use of APL is in connection with the playing of the general-purpose management game which is an integral part of the M. B. A. students' first year of study. Externally, it is quite similar to the IBM APL Business Simulation. internally, it is constructed rather differently. The availability of the APL Plus-batch file interface permits the best of toth worlds.

In almost all business games which involve more than two teams. the inputs (in the form of various management decisions) must be provided by all teams tefore the game can be run for the next period. This is intrinsically a batch operation. On the other hand, it is very helpfu! if each team can prepare input, and analyze output, in an interactive mode.

There are 72 teams divided into 12 industries of 6 firms each. The teams prepare irput at the APL terminals, making use of whatever tools they find helpful: resource allocation models; pro forma income projections; forecasts based upon regression techniques: and. in a few cases, specially-prepared simulation models of the industry and the competition (i.e.. a simulation of a simulation).

Each of the teams then stores its decision in a specially-accessed-and protected-APL Plus file. When all the decisions are in. they are passed to a temporary batch file. From here they are input into a FORTRAN-coded bateh program which actually executes the game for the next peried of play. The results of this exccution are printed on the high-speed remote printer in the School as well as being returned to each team's APL stored workspace; there they can analyze the results for the next round of competition.

Application Questionnaire and Cover Letter
c:madeate schod of mancerment I.OS ANGELES, CALIIORNIA 90024

Thank you for your interest in our program, Interactive Computing for Management Educators, to be held here at UCLA during the period June 29 - July 11, 1975. The response has been such that we expect to have many more applicants than we have openings. For this reason, we will be forced to select from among those expressing interest in order to obtain the desired class size of 24 . As stated in the descriptive brochures, it is our desire "to obtain a broad cross section of disciplines, functional areas, and representation from among AACSB member schools."

Toward this end, I am enclosing an application questionnaire which I would like for you to fill out and return to me by April 5 th. I know this questionnaire may appear formidable, but only in this way can we obtain the broad base of information we need in order to make intelligent decisions. Therefore, I beg for your indulgence.

As of the writing of this letter, it appears that there will be approximately five applicants for every one opening. On the surface, this may discourage you from completing the questionnaire, especially when you see the questions relating to computing background. You may assume that because you have little or no experience, your chances are correspondingly lower. Actually, if anything, the reverse is true. As stated in the brochure "there is no need to have had any previous experience in computing." Also, "it is the intention of this program...to make the transition from non-use [emphasis added] to informed use as easy and painless as possible."

A second reason for completing and submitting the questionnaire - even if you are not selected - is that your application, together with others who were unable to be accepted, will form a "data base" of evidence of the widespread interest for programs such as this. Hopefully, such a large list of individuals would move IBM or some other sponsoring organization to underwrite a second or third offering. Of course, there is no guarantee of this, but I would be remise if I did not mention it as a possibility.

Therefore, may I enlist your care and assistance in completing the application questionnaire and returning it to me here at UCLA. All applicants will be notified of the final selections by the second week in April. Thanks again for your interest and help.

Sincerely,

EPHRAIM R. McLEAN
Assistant Professor of Information Systems
Director, Center for
Information Studies

ERM/mc
Enclosure

# INTERACTIVE COMPUTING FOR MANAGEMENT EDUCATORS 

Graduate School of Management<br>University of California<br>Los Angeles, California 90024

29 June - 11 July 1975

## Application Questionnaire

Please fill out this questionnaire as completely as possible and mail to the address below by April 5, 1975.

Professor Ephraim R. McLean
Graduate School of Management
University of California
Los Angeles, California 90024

## I. Information Concerning Applicant

1. Full Name $\qquad$
2. Present Title
3. Institution $\qquad$
4. Address (include ZIP Code):
a. Business $\qquad$



Telephone $\qquad$
b. Home $\qquad$
$\qquad$ $\ldots$

Telephone $\qquad$
5. Date of Birth Birth Place
6. Citizenship $\qquad$ 7. Soc. Security \#
8. Education:
Type of
Degree
Date
Obtained
Institution
Where Obtained
a) Undergraduate:
b) Graduate:
9. Discipline or Area of Soecialization:
10. List the three courses which you teach most regularly:

Title
Topic (if not clear from title)
a.
b.
c. $\qquad$
In which of these courses do you anticipate making the greatest use of interactiv, computing? a. $\qquad$ b. $\qquad$ $c$.
If some other course, please describe: $\qquad$
II. Information Concerning Applicant's Computor Background (if any).

1. Have you ever written a computer program or taken a course in computer programming?

No: $\qquad$ If no, please go on to Question II. 3. below. Yes: $\qquad$ If yes, please state in which language(s) these programs were written
$\qquad$
$\qquad$
2. List the computer courses you have taken (do not list more than 5): Title Topic (if not clear from title)
a. $\qquad$
$\qquad$
b. $\qquad$
c.
d. $\qquad$

e. $\qquad$
3. Have you ever used the computer in a conversational, interactive mode (e.g., APL, BASIC, TSO, etc.)?

No: $\qquad$
Yes: $\qquad$ If yes, please describe: $\qquad$
$\square$
$\qquad$
$\qquad$
4. Have you used the computer in any other way not described above?

No: $\qquad$ Yes: $\qquad$ If yes, please describe: $\qquad$
$\qquad$


III. Information Concerning Applicant's Institution

1. Number of Students Enrolled:
Business School
or Department

Total
Campus
a) Undergraduate:
b) Masters: $\qquad$

2. Year in which business school or department was founded: $\qquad$
3. Total number of faculty F.T.E.'s (Full Time Equivalents):
4. Type of computer most frequently used by business school faculty and students. (Please give manufacturer's name and model number. E.g. IBM 360/50, IBM 370/145, Burroughs 5700, Xerox Sigma 7, etc.):
$\qquad$
5. Computer available to business school faculty and students, if different from Question III.4. above. (Again, please give manufacturer's name and model number): $\qquad$
6. Does the business school currently have a terminal-based interactive computing service available to it on a regular basis?
No: $\qquad$ If no, please go on to Question III.9. below. Yes: $\qquad$
7. What type of interactive service is available?

| BASIC | APL (Burroughs) |
| :---: | :---: |
| APL/360 | APL/CMS |
| APL * PLUS | APL/SV |
| APL (UNIVAC): | APL (Xerox) |

Other (please describe): $\qquad$
8. Number of computer terminals available for student and faculty use:
9. What plans are there for the future with regards to acquiring or enhancing the interactive computing capability for the business school and/or the campus as a whole (please be as specific as you can)? $\qquad$
 ___

## IV. Information Concerning Use of Interactive Computing

1. Do business school students currently take a required course in computing?

No: $\qquad$ If yes, please describe this course: $\qquad$
2. Are there other courses in the curriculum which make use of the computer? No: $\qquad$
Yes:___If yes, please list them (if more than 5, list only those closest to your discipline or area of specialization):

Title
a.
b.
c.

e. $\qquad$
3. As part of the program, Interactive Computing for Mana gement Educators, each participant will be required to develop and program (in APL) an application relating to his or her discipline. If selected, describe what your application would be:
4. Recongizing that there may be many more applicants than there are openings in this program, please make a bricf statement as to why you wish to attend and what you bclieve you will be able to do with the experience once you return to your own campus:
5. Although all expenses while at UCLA will be covered by the sponsoring grant from IBM, travel to and from Los Angeles will not be covered. Please indicate the source of such travel funds:

School or university sources:
From your own pocket:
Other (please describe):
6. If you are unable to get into the June 29 th program because of the limited number of openings, would you be interested in attending this program at some later date (assuming that additional support could be obtained)?

No:
Yes: $\qquad$ If yes, please indicate your preference as to time:

Late July 1975
Mid-August 1975:
Summer 1976
Other


Thank you for your care and patience in completing this application questionnaire.
6.5

## Letter of Acceptance

## UNIVERSITY Og CALIFORNIA, LOS ANGELES



> SANTA HABBAHA - SANTA CRUZ

Ghaduate school of manacement LOS ANGELES, CALIFORNIA 90024

On behalf of Ken Siler, Jim Schenck, and myself, I would like to take this opportunity to welcome you personally to the upcoming program "Interactive Computing for Management Educators" here at UCLA.

At final count, there were 105 faculty members who made application to the program and so the selection process proved to be very difficult indeed. I believe, however, that those who were selected represent a broad cross section in terms of disciplines, schools, and geographical distribution. I hope that the two weeks that you spend with them-and with us-will prove to be enjoyable as well as productive.

The program itself is described in a fair amount of detail in the announcement brochure and so $I$ won't repeat that information here. However, a few addjtional details may be helpful.

The program will open with a reception-cocktail party, followed by dinner, beginning at 6:00 P.M. on Sunday, June 29th, at the Holiday Inn of $\dot{H}$ estwood, 10740 Wilshire Boulevard, in West Los Angeles. A color brochure, describing the Holiday Inn is enclosed. We have made reservations for you at this Holicay Inn for the 12 nights, June 29th through July loth. If you wish to arrive earlier or stay later (at your expense), please let us know so that we may notify the Holiday Inn of your plans. All of the rooms will be double occupancy, but each room has two queen-sized beds and so $I$ am sure you will be quite comfortable.

The Inn is about 12 miles from Los Angeles International Airport and there is a bus which goes directly to the Inn from either Building 2 or Building 7 at the Airport. The fare is $\$ 1.70$ and the schedule is as follows:

| I. A. In | ional | Air |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Bldg. 2 | Bldg. | 7 | Holiday | Inn |
| 9:25 A.M. | 9:35 | A. M. | 10:00 | A.M. |
| 11:50 A.M. | 12:00 | A.M. | 12:30 | P.M. |
| 1:40 P.M. | 1:50 | P.M. | 2:20 | P.M. |
| 3:10 P.M. | 3:20 | P.M. | 4:00 | P.M. |
| 5:10 P.M. | 5:20 | P.M. | 5:45 | P.M. |

If you miss the bus, there is of course taxi service; the fare is approximately $\$ 6.00-\$ 7.00$.

Breakfasts will be at the Holiday Inn (just charge it to your room) and lunches at the UCLA Faculty Club. A cash stipend will be provided upon arrival so that you can have your choice of dinner at either the Inn or at one of the many restaurants in Vestwood. Laundry dry cleaning, or other personal expenses can also be charged to your room. A special bus will provide transportation between the Inn and the Graduate School of Management. Vestwood itself is within walking distance, so you will not require a car unless you wish to plan a trif on your own (e.g., a visit to Disneyland on the middle weekend). Naturally, such trips, as well as any other private entertainment, are not covered by the IBM grant.

The weather in Los Angeles is quite pleasant in June-July (mid-80's), and the dress for classes will be informal. However, the evenings can be cool and so you will probably want something warmer for evening wear.
C.asses will be Monday through Friday for both weeks (including the 4th of July), 8:30 A.M. to 5:30 P.M. We plan to finish the formal insiruction early in the second week and devote the balance of the time io working on your individual programs. As mentioned in the announcement, these APL programs are to be published in a monograph, and so we are most anxious that everyone have their program completed by Friday morning. Therefore, you may make plans to leave Los Angeles sometime Friday afternoon or evening. More information about the preparation for this programming assignment is covered on an enclosed sheet.

Finally, $\quad$ am enclosing a list of the course materials and a copy of one of the books we will be using: Marilyn Bohl's Information Processing. Although none of the participants are knowledgeable about Apl, several do have some background in computing. Therefore, in order that we all have the same vocabulary, I am sending this book in advance so that you can "come up to speed" on basic computer concepts prior to the beginning of the program. It is a well-written, straight-forward text and the enclosed book list indicates those pages
that will be most useful. If you do not have any previous background in computing, please read the assigned sections before June 30th.

I believe that $I$ have covered most of the key points of the program; however, if you have any questions between now and its beginning, please feel free to call Miss Maddie Contraras, the administrative assistant, at (213) 825-2001. The number for the Holiday Inn is (213) 475-37ll. I am looking forward to meeting you personally and to the two weeks we will be spending together.

Sincerely,

Ephraim R. McLean<br>Assistant Professor of<br>Information Systems<br>Director, Center for<br>Information Studies

ERM/kw

Enclosures (5)

INTERACTIVE COMPUTING FOR MANAGEMENT EDUCATORS
Graduate School of Manarrement University of California, Los Angeles

READING LIST

The following books and materials are to be us d in conjunction with the UCLA program on APL for management:
*Bohl, Marilyn, Information Processing, Chicagn: SRA, 1971.
Buckley, J. W., Nagaraj, M. R., Sharp, D. L., and Schenck, J. W., Managenent Problem-Solving with APL, Los Angeles: Melville Puílishing Co., 1974.

Gilman, L., and Rose, A. J., APL: An Interactive Approach (2nd Edition), New York: John Viley \& Sons, Inc., 1974.

Scientific Time Sharing Corporation, APL Plus $\triangle F M T$ Report Formatting Instruction Manual, Bethesca, Maryland: S'TSC, 1972 .

Scientific Time Sharing Corporation, Apl plus File Subsystem Instruction Manual, Bethesda, Maryland: STSC, 1971.

Scientific Time Sharing Corporation, APL Plus Time-Sharing Refercnce Data Card, Bethesda, Maryland: STSC, 1971.

* The Information Processing book is to be read prior to arrival. Although all of the book is informative and potentially useful, the most important parts are found on the following pages: 1-37, 49-93, 106-171, 189-220, 231-235, and 247-282. The other books and materials will be distributed at the beginning of the course.


## 6.6

## Program Evaluation Questionnaire

# INTERACTIVE COMPUTING FOR MANAGEMENT EDUCATORS 

Graduate School of Management University of California, Los Angeles

## Program Questionnaire

I. Accommodations

Poor Outstanding

1. Rooms at the Holiday Inn

2. Meals

Breakfasts at the Holiday In


Lunches at the UCLA Faculty Center


Arrangements for independent dinner dining
3. Transportation

4. Administrative and clerical support (Maddie Contreras)
5. Program support (Bob Biadspies)

6. Comments and/or general appraisal of housing, meals and other living arrangements:
II. Course

1. Text (Gilman \& Rose)

2. Other reading materials and handouts

3. Lecture content and sequencing
4. Lab assignments

5. Presentations by outsiders

$$
\text { Didn't } \Lambda \text { tend }
$$



Bill Bergquist ( )

7. Pace of presentation
8. What would you like to see added or expanded?
9. What would you like to see deleted or reduced?
10. Other suggested changes to the structure or content of the program:
11. Other suggestions or comments:
III. Instruction

1. Quality and effectiveness of classroom sessions

Eph McLean


Jim Schenck

2. Quality and offectiveness
of lab sessions (Jim Schenck)

3. Quality and effectiveness
of individual coaching and
assistance
Bob Bradspies
Eph McLean
Jim Schenck
Ken Siler

4. Comments and/or general appraisal of the quality of instruction:
IV. Summary

Poor Outstanding

1. Your overall evaluation of the program as a whole $1 / 1 / 1 / 1 / 1$
2. A brief statement summarizing your overall appraisal of the program:
3. Any other suggestions for improvement?
6.7

Post Conference Follow-Up Letter

UNIVERSITY OF CALIFORNIA, LOS ANGELES

chaduate scmool of manacemfent I.OS ANGELES, CAIMFORNIA 90024

Now that a week or so has past since the end of the program, I hope you have had a chance to recuperate from the rigors of our two weeks together. It was a demanding experionce for all concerned; but $I$, for one, thoroughly enjoyed myself. I hope you did too.

Jim, Ken, and $I$ are in the process of reviewing the programs that were left with us. On the attached sheet is a checklist of the materials that we have from you. If you want-or need-to worl on your program, merely go to one of the APL terminals on your campus and then dial into our system here at UCLA. The numbers apain are as follows: 213-825-0911, -0921, 0931, -0941, and -0721. Naturally, you will have to identify to the system the type of terminal you are using (e.g., Al) or AO) for $1 B M$ 2741's), just as you did here at UCLA. After that, use your APL number and password and then go to town:

The numbers will be kept active until Monday, August l8th. At that time we hope to have everyone's work in hand and will then begin the detailed editing. If you have any questions or problems, don't hesitate to give one of us a call.

| Eph Mclean | $213-325-1449$ |
| :--- | :--- |
| Ken Siler | $213-325-1252$ |
| Jim Schenck | $213-825-4196$ or $213-825-2870$ |

I hope that the balance of the summer will be pleasant for you and that you will be able to put your newly acquired APL skills to use in the Fall.

Sincerely,

EPHRATM R. MCIFAN
Associate Professor of Information Systems

Attachment


[^0]:    Edgar P. Hickman
    Professor and Program Director of Management Science College of Business Administration University of South Carolina Columbia, South Carolina 29208

[^1]:    1 See T. H. Naylor, J. L. Balintfy, D. S. Burdick, and Kong Chu, Computer Simulation Techniques, John Wiley and Sons, New York, 1966, pp. 197-98 and 234.

[^2]:    WOULD YOU LIKE A PLOT OF the above data?
    YES

[^3]:    1 See FORTRAN Applications in Business Administration, Vol. II, edited by Thomas J. Schriber and Laurence A. Madeo, The University of Michigan, Ann Arbor, Michigan, 1971, pp. 385-422.
    2 See Simulation Using GPSS, by Thomas J. Schriber, John Wiley \& Sons, Inc., New York, 1974, pp. 112-120.
    3 See SIMULETTER, Vol. 5, No. 3, April 1974, pp. 75-76.

[^4]:    1. Meier, Robeft C., William T. Newell, Harold L. Pazar, Simulation in Business and Economics, Prentice-Hall, Inc., Englewood Cliffs, $\overline{N e w}$ Jersey, 1969 , pp. 313 ff .
